### The law of reflection



A ray departing from P in the direction  $\theta$ with respect to the mirror normal is reflected symmetrically at the same angle  $\theta$ .

This is because the symmetric path POP' has minimum length.

Compare, for example, the alternative  $P\tilde{O}P'$ . Clearly,  $|PO| + |OP'| < |P\tilde{O}| + |\tilde{O}P'|$ .

> Consider the continuation of OP' backwards through the mirror. To an observer in the direction of P', the ray will appear to have originated at P''.





### The law of refraction (Snell's Law)



NUS Without Halametry History

# Snell's Law as minimum time principle



Which path should the lifeguard follow to reach the drowning person in minimum time?









 $n_c \sin \theta_c = 1$ 

at critical angle, the refracted light propagates parallel to the interface

the result is called a "surface wave"

at angles of incidence higher than critical, the light is totally internally reflected almost as if the glass-air interface were a mirror

in both cases of surface wave and TIR. there is an exponential tail of electric field leaking into the medium of lower optical density; this is called the evanescent wave.

Typically, the evanescent wave is a few wavelengths long but it can be much longer near the critical angle We will learn more about evanescent waves after we cover the electromagnetic nature of light



## **Frustrated Total Internal Reflection (FTIR)**



If another dielectric approaches within a few distant constants from the TIR interface, the tail of the exponentially evanescent wave becomes propagating; *i.e.* the light couples out of the medium. This situation is known as *Frustrated Total Internal Reflection (FTIR)*. In quantum mechanics, there is an analogous effect known as *tunneling*. We will compute the amount of energy coupled out of the medium of incidence later, after we study the electromagnetic nature of light.









## Numerical Aperture (NA) of a waveguide

NA is the sine of the largest angle that is waveguided



# **GRadient INdex (GRIN) waveguide**







### **GRIN** waveguides in nature: insect eyes



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#### **Dispersion measures**

Reference color lines C (H-  $\lambda$ =656.3nm, red), D (Na-  $\lambda$ =589.2nm, yellow), F (H-  $\lambda$ =486.1nm, blue)

e.g., crown glass has

 $n_{\rm F} = 1.52933$   $n_{\rm D} = 1.52300$   $n_{\rm C} = 1.52042$ 

Dispersive power 
$$V = \frac{n_{\rm F} - n_{\rm C}}{n_{\rm D} - 1}$$
  
Dispersive index  $v = \frac{1}{V} = \frac{n_{\rm D} - 1}{n_{\rm F} - n_{\rm C}}$  aka Abbe's number

e.g. for crown glass: V=0.01704 or v=58.698



# Paraboloidal reflector: perfect focusing



What should the shape function s(x) be in order for the incoming parallel ray bundle to come to perfect focus?

The easiest way to find the answer is to invoke Fermat's principle: since the rays from infinity follow the *minimum* path before they meet at *P*, it follows that they must follow the *same* path.

$$2f = f - s + \sqrt{x^2 + (f - s)^2}$$
$$f + s = \sqrt{x^2 + (f - s)^2}$$
$$x^2 = (f + s)^2 - (f - s)^2 \Rightarrow$$
$$= 4sf \Rightarrow$$
$$s(x) = \frac{x^2}{4f}$$

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