

Outline of the Topics

1. Trends in the periodic table.
2. Introduction: Heavy Fermions and the Kondo Lattice.
3. From Anderson to Kondo
4. Kondo Insulators: the simplest heavy fermions.
5. Oshikawa's Theorem.
6. Large N expansion for the Kondo Lattice
7. Heavy Fermion Superconductivity
8. Topological Kondo Insulators
9. Co-existing magnetism and the Kondo Effect.

Please ask questions!

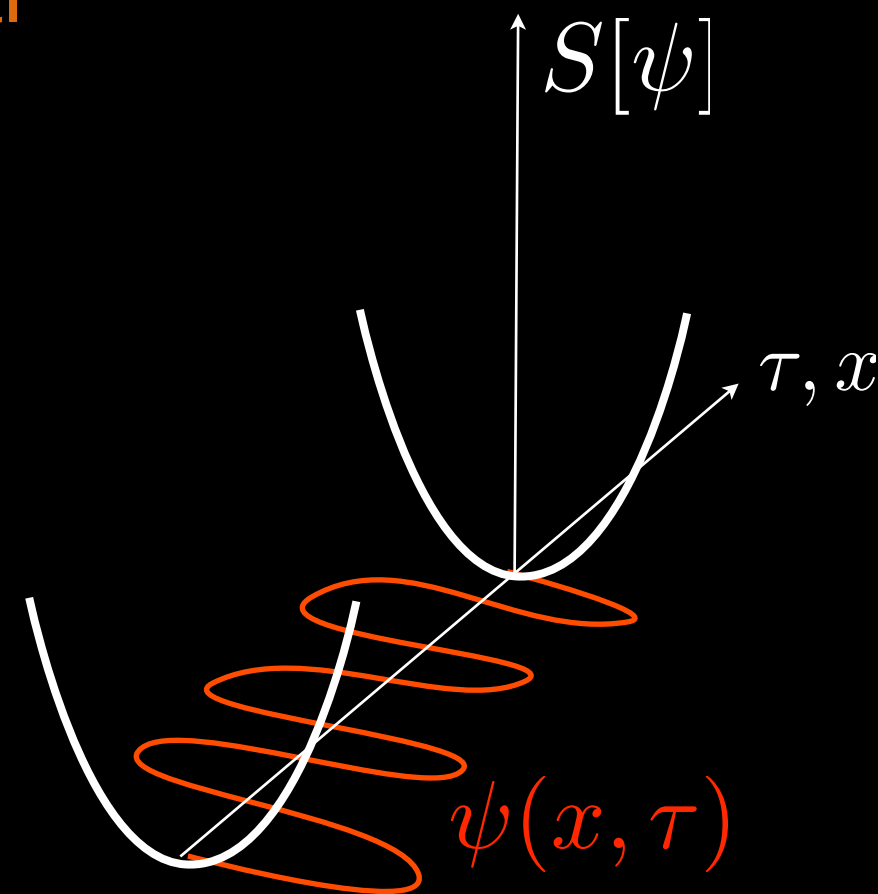
$$H = \sum_{\mathbf{k}} \epsilon_{\mathbf{k}} c_{\mathbf{k}\sigma}^{\dagger} c_{\mathbf{k}\sigma} + J \sum_j c_a^{\dagger}(j) c_b(j) S^{ba}(j)$$

Local Wannier state:

$$c_{\sigma}^{\dagger}(j) = \frac{1}{\sqrt{V}} \sum_{\mathbf{k}} c_{\mathbf{k}\sigma} e^{i\mathbf{k} \cdot \mathbf{R}_j}$$

Doniach 77, Lacroix and Cyrot 79, Coleman 83, Read and Newns 83, Auerbach and Levin 86.

$$Z = \int \text{Fields} e^{-S[\psi]} \quad \text{Path Integral}$$



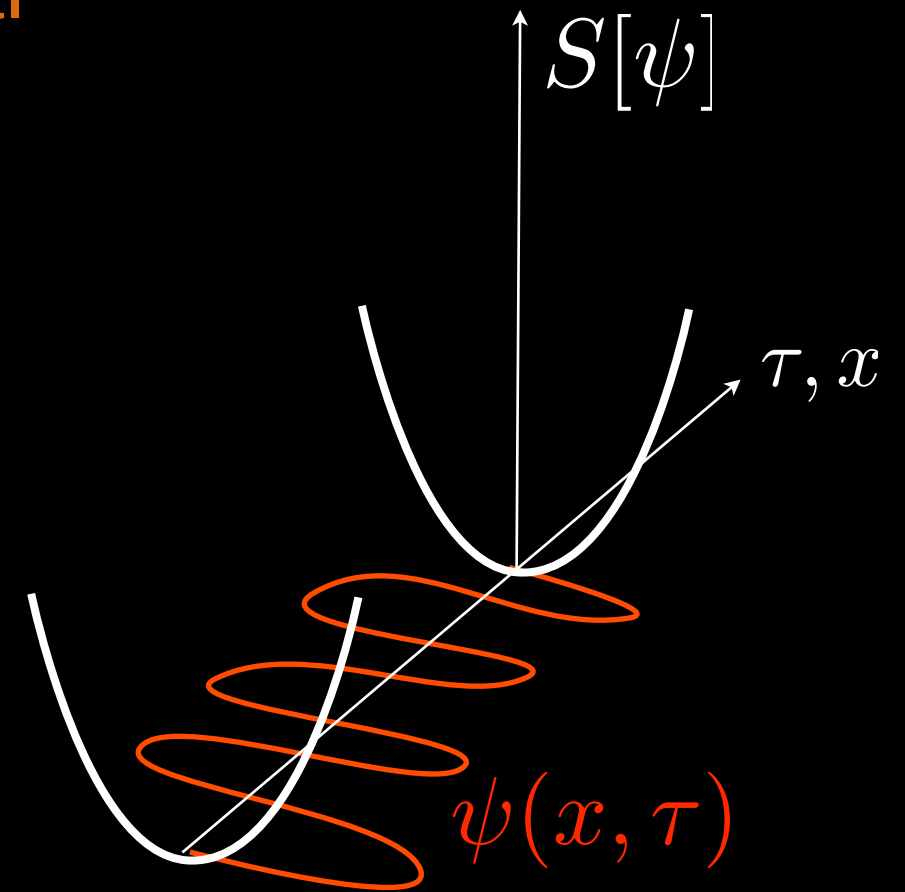
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Path Integral

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Wild quantum fluctuations!

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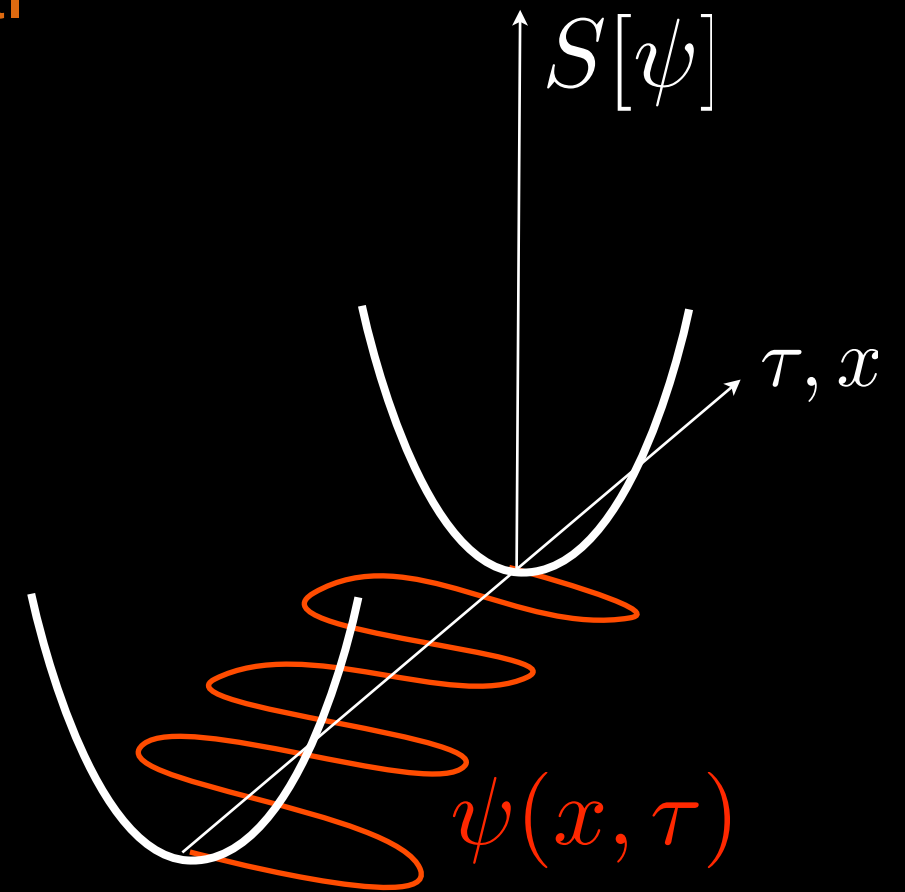
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How can we tame the wild Quantum fluctuations?

Path Integral

$$Z = \int \text{Fields} e^{-S[\psi]}$$



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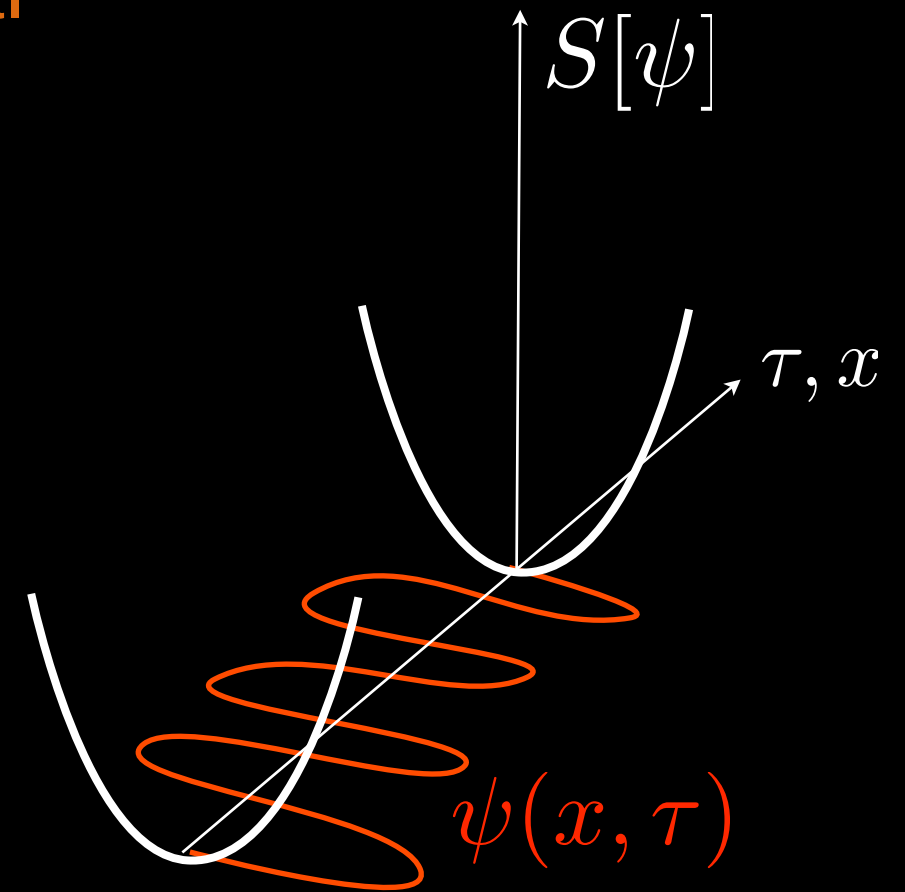
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Large N expansion.

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Path Integral



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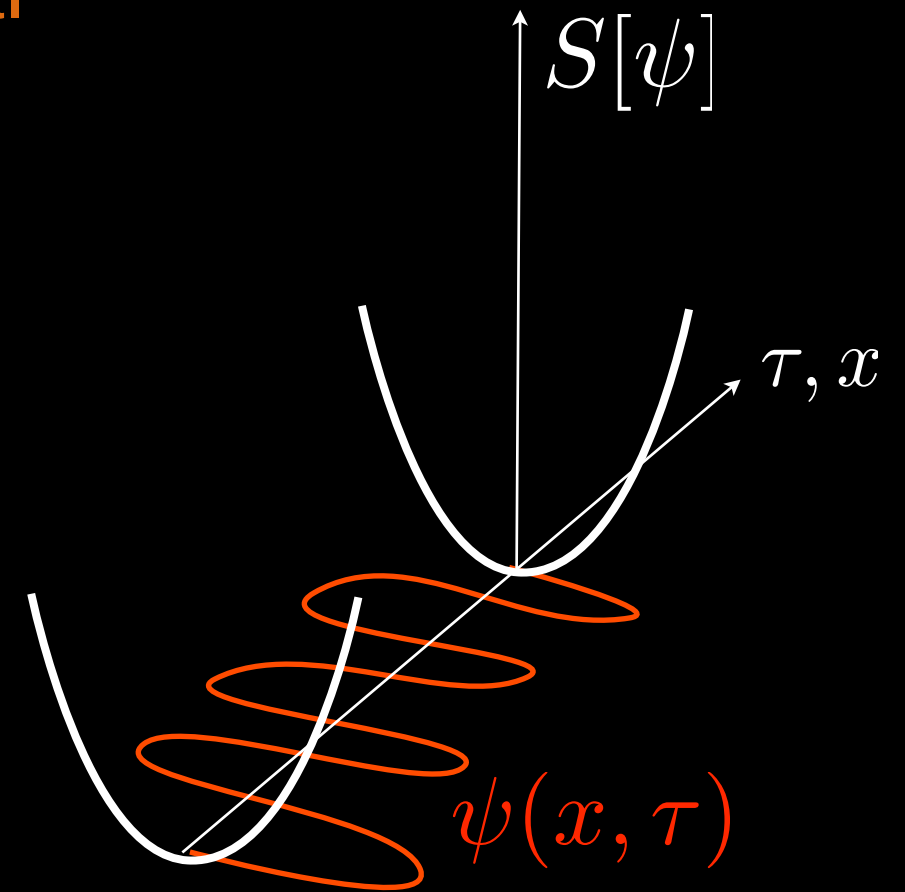
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Large N expansion.

Path Integral

$$Z = \int \text{Fields} e^{-S[\psi]}$$



$$\sigma \in \left(-\frac{1}{2}, \frac{1}{2}\right) \longrightarrow \left(-\frac{N}{2}, \frac{N}{2}\right)$$

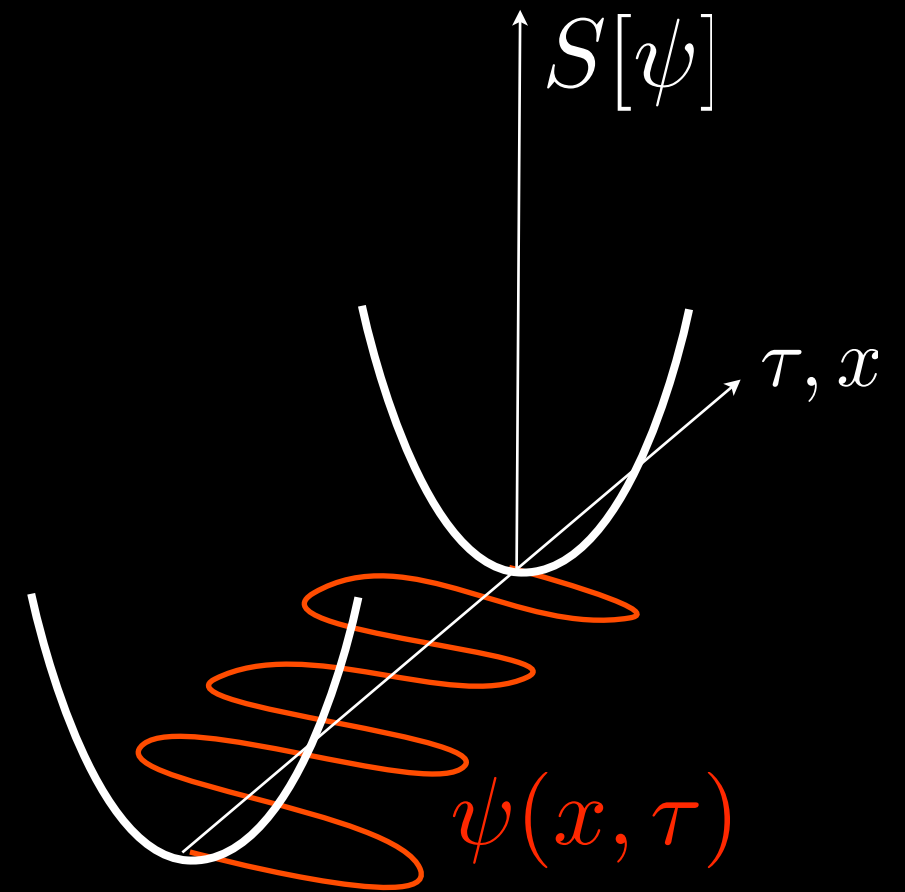
$$H = \sum_{\mathbf{k}} \epsilon_{\mathbf{k}} c_{\mathbf{k}\sigma}^{\dagger} c_{\mathbf{k}\sigma} + \frac{J}{N} \sum_j c_a^{\dagger}(j) c_b(j) S^{ba}(j)$$

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Large N expansion.

$$Z = \int \text{Fields} e^{-N S[\psi]}$$



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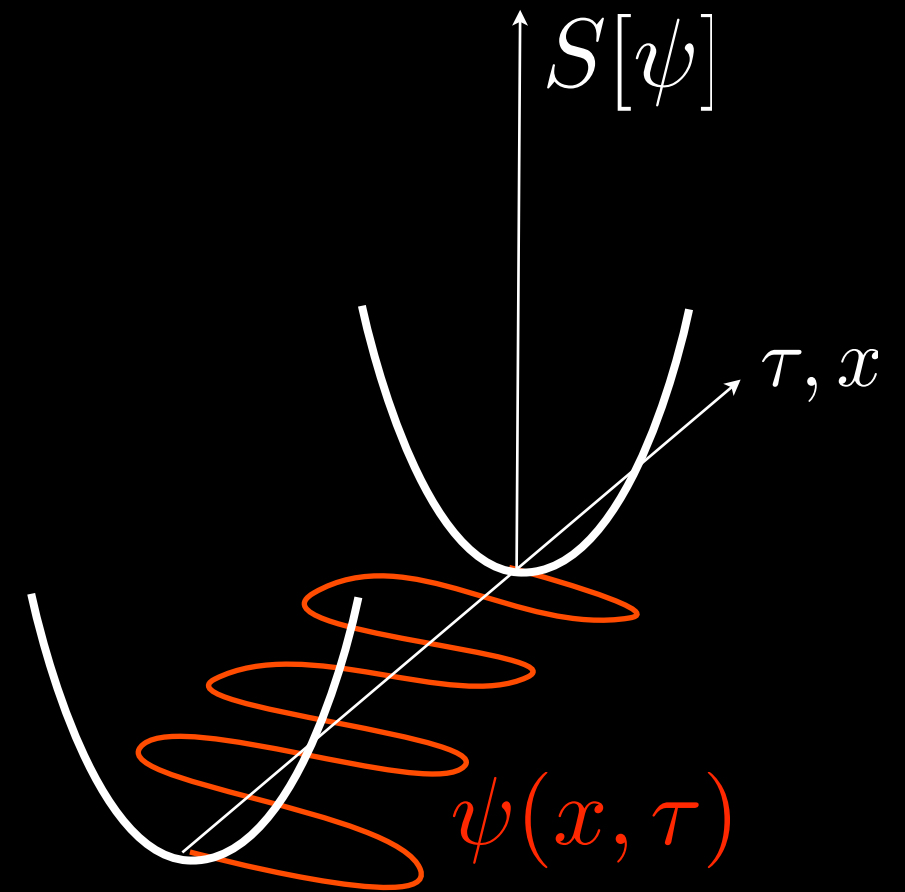
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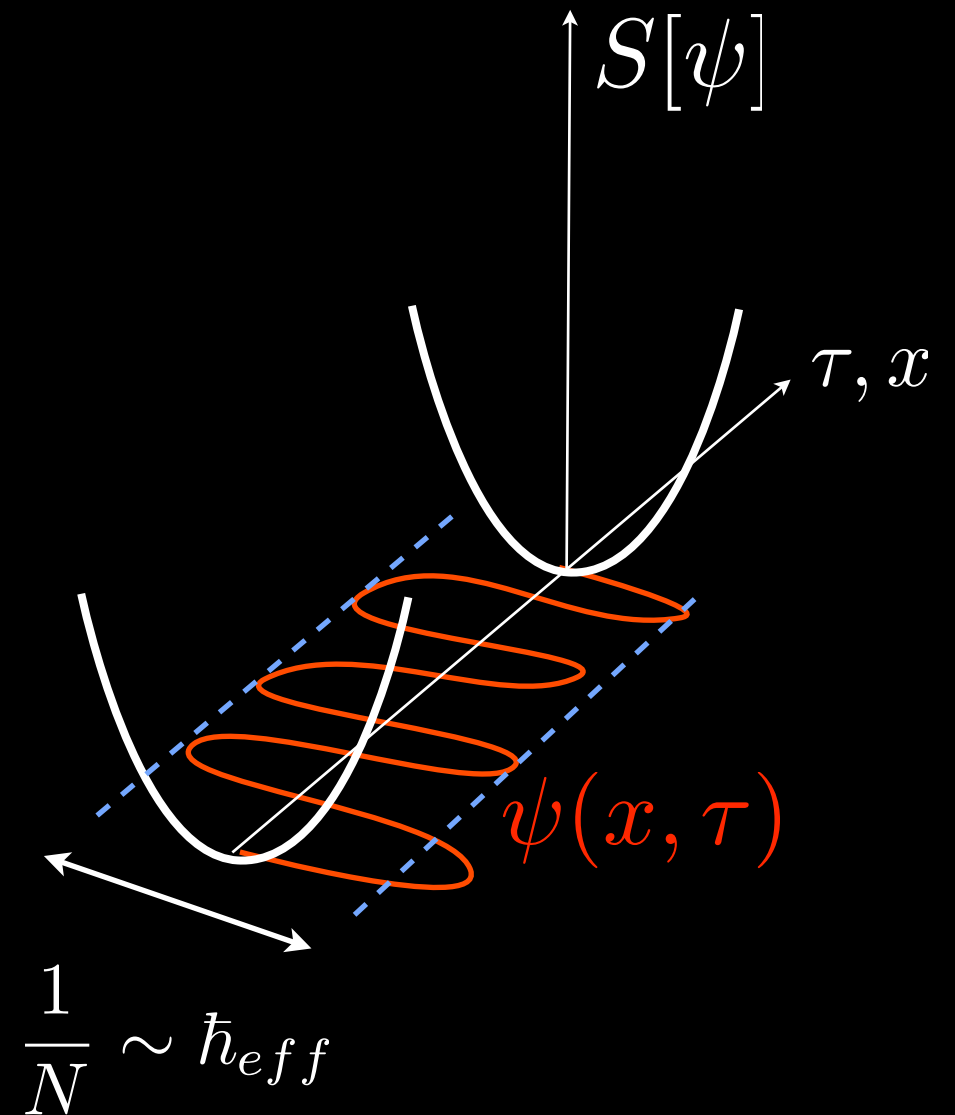
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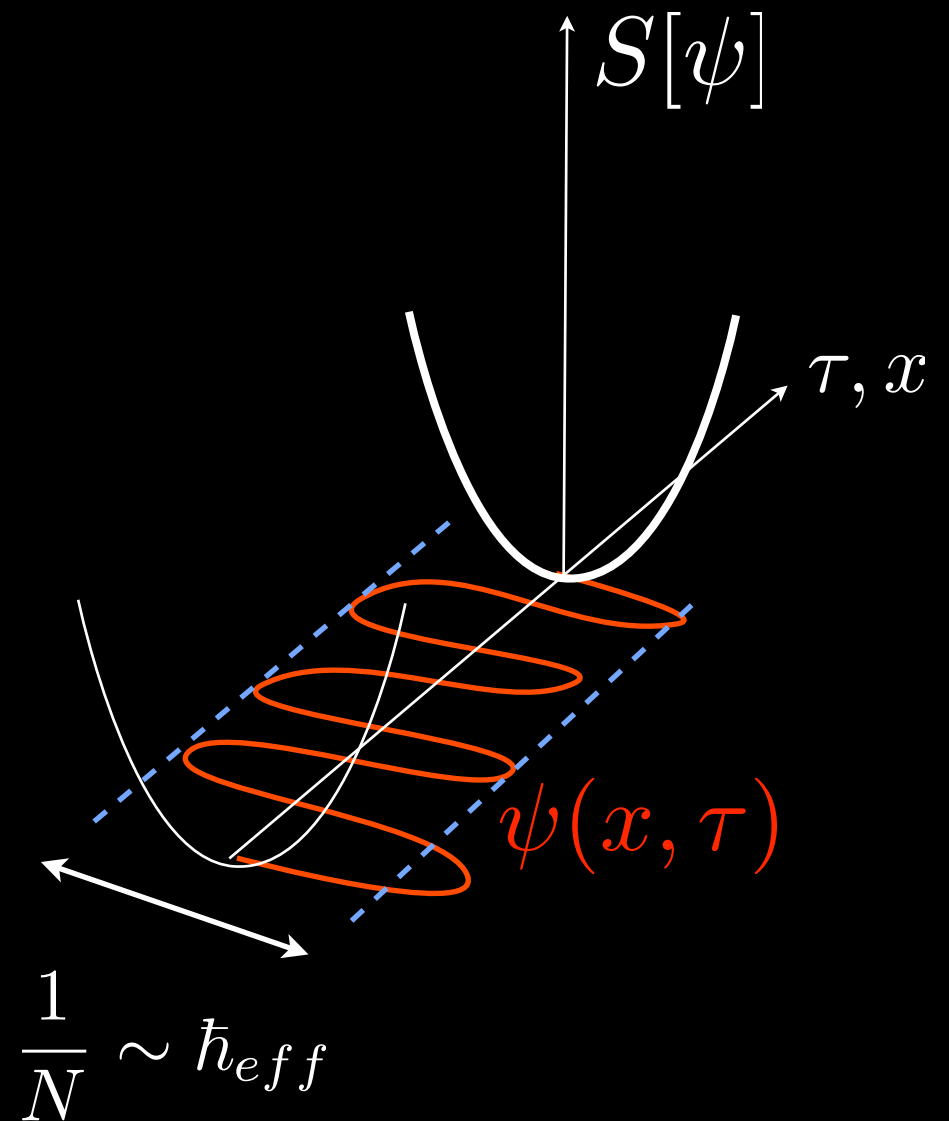
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$$N \rightarrow \infty$$



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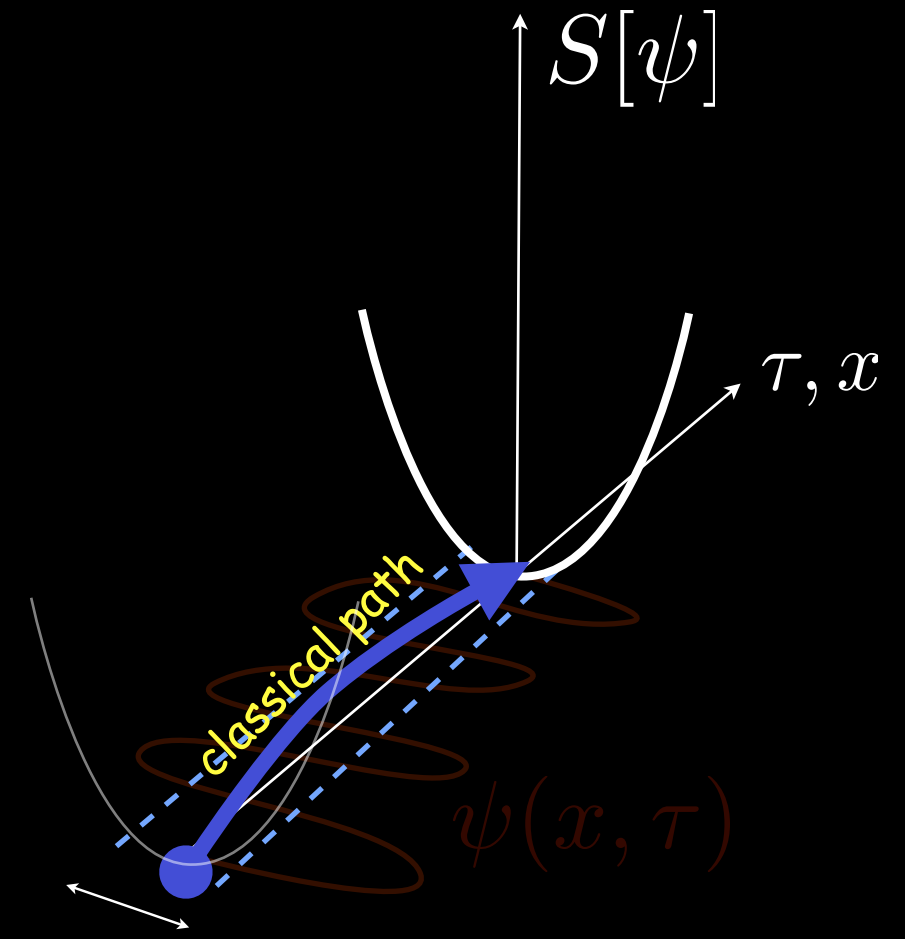
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Large N expansion.

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$$N \rightarrow \infty$$



$$\frac{1}{N} \sim \hbar_{eff}$$

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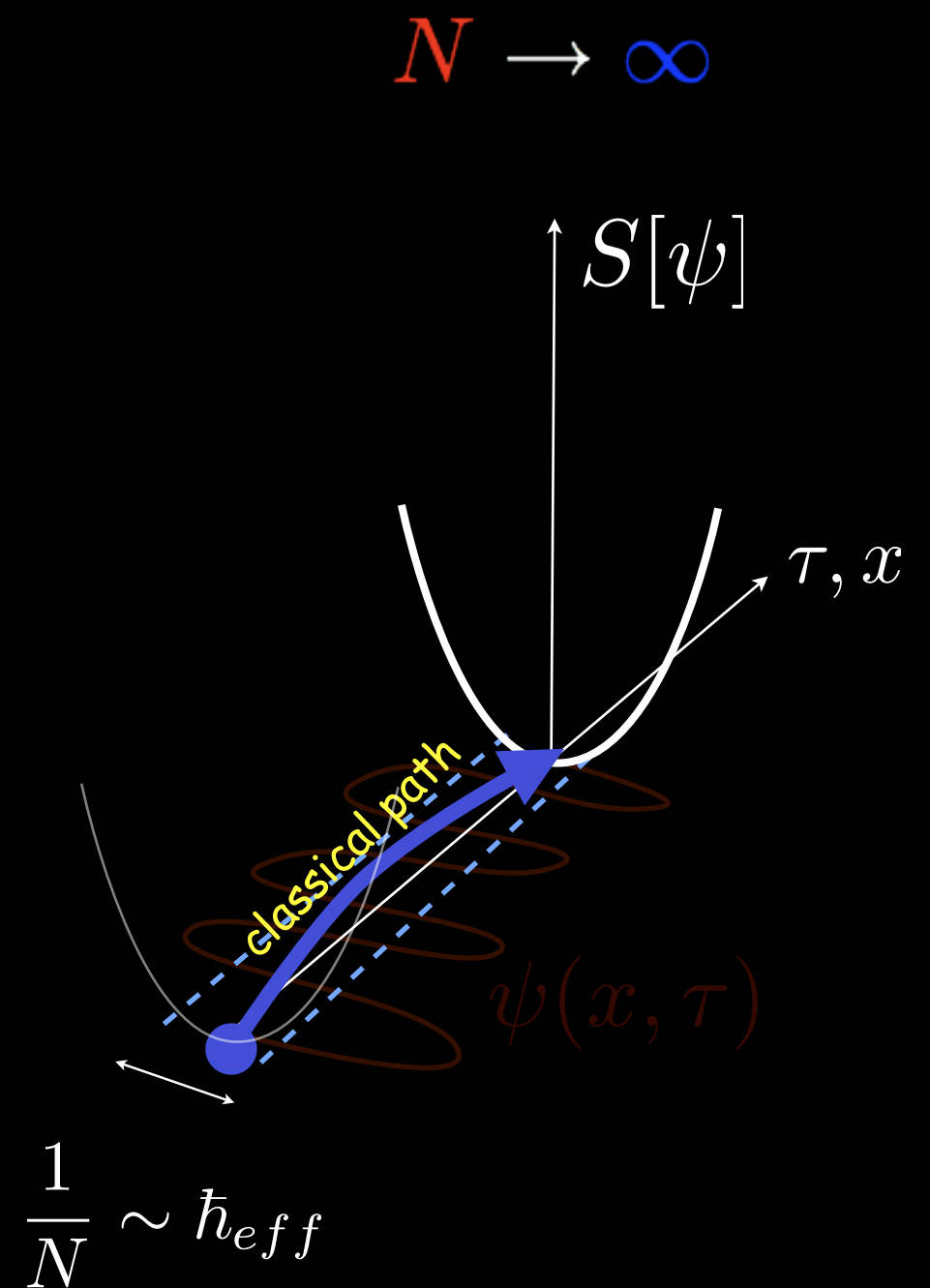
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Large N expansion.

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Large N expansion.

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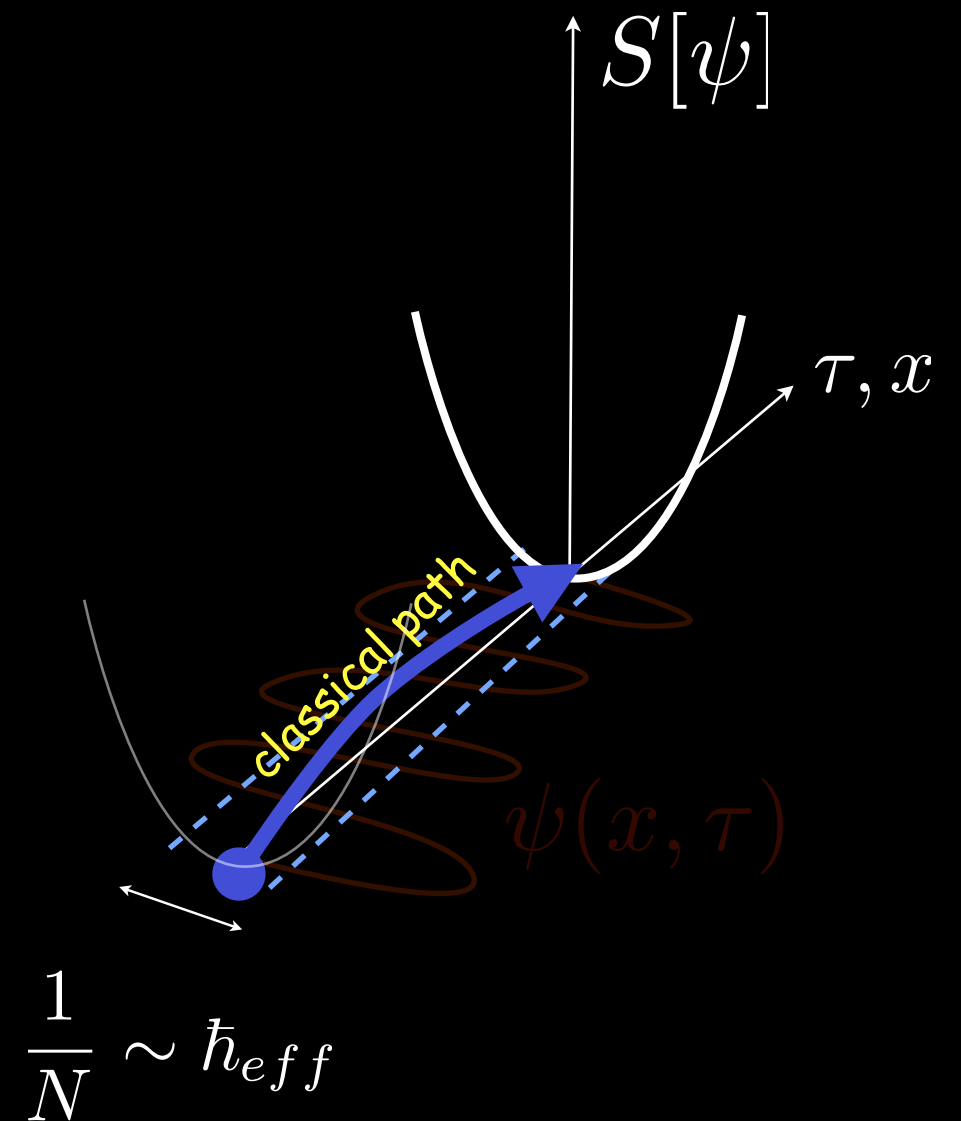
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$$H_I \rightarrow -\frac{J}{N} (f_{j\alpha}^\dagger c_{j\alpha}) (c_{j\beta}^\dagger f_{j\beta})$$

$$\rightarrow \bar{V} (c_{j\beta}^\dagger f_{j\beta}) + (f_{j\alpha}^\dagger c_{j\alpha}) V + N \frac{\bar{V}V}{J}$$

$$H = \sum_{\mathbf{k}} \epsilon_{\mathbf{k}} c_{\mathbf{k}\sigma}^\dagger c_{\mathbf{k}\sigma} + \frac{J}{N} \sum_j c_a^\dagger(j) c_b(j) S^{ba}(j)$$



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Large N Approach.

Read and Newns '83.

$$H = \sum_{\mathbf{k}\sigma} \epsilon_{\mathbf{k}} c_{\mathbf{k}\sigma}^\dagger c_{\mathbf{k}\sigma} + \sum_j H_I(j)$$

$$H_I(j) = -\frac{J}{N} \left(c_{j\beta}^\dagger f_{j\beta} \right) \left(f_{j\alpha}^\dagger c_{j\alpha} \right)$$

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$$c_{j\alpha}^{\dagger} = \frac{1}{\sqrt{\mathcal{N}_s}} \sum_{\mathbf{k}} c_{\mathbf{k}\alpha}^{\dagger} e^{-i\mathbf{k}\cdot\vec{R}_j}$$

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Constraint $n_f = Q=qN$
all terms extensive in N

Large N Approach.

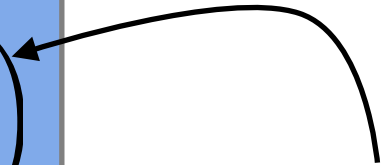
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$$-gA^\dagger A \rightarrow A^\dagger V + \bar{V} A + \frac{\bar{V}V}{g}$$

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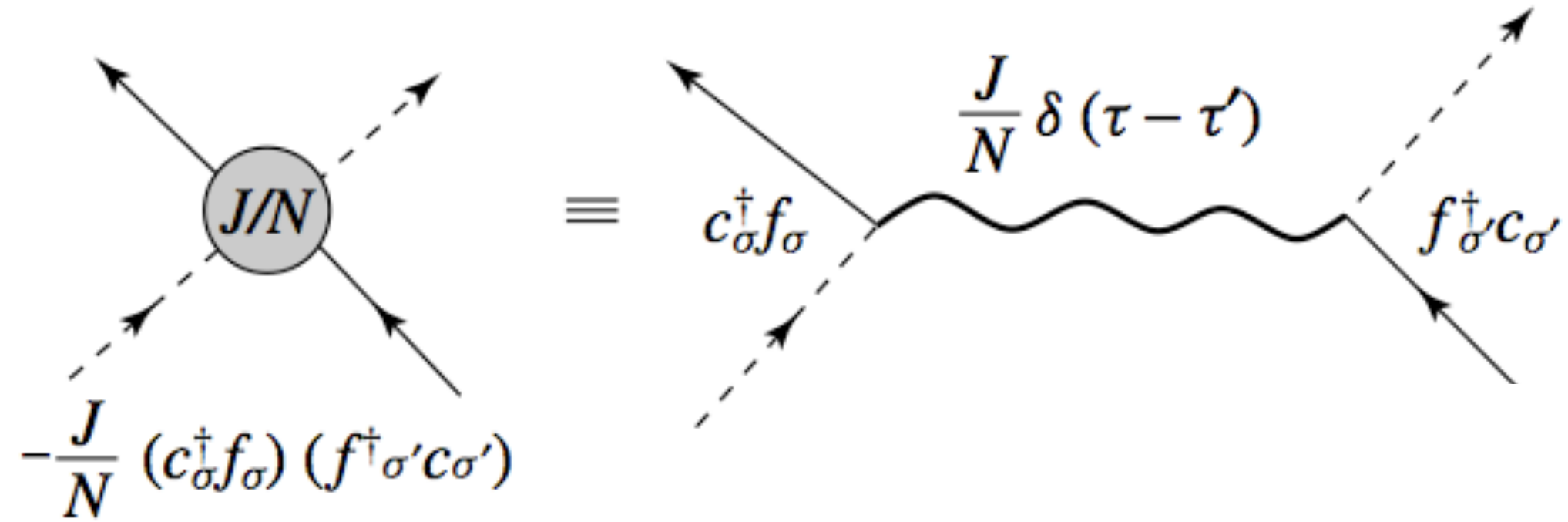
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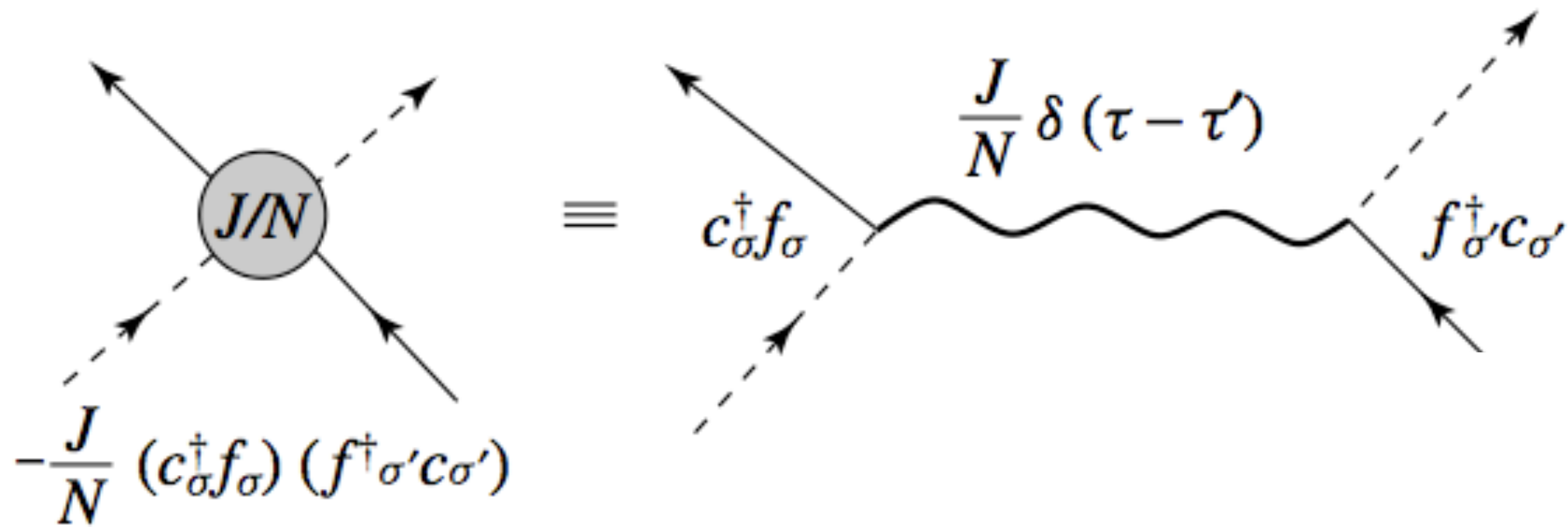
$$-gA^\dagger A \rightarrow A^\dagger V + \bar{V} A + \frac{\bar{V}V}{g}$$

$$H_I(j) \rightarrow H_I[V, j] = \bar{V}_j \left(c_{j\alpha}^\dagger f_{j\alpha} \right) + \left(f_{j\alpha}^\dagger c_{j\alpha} \right) V_j + N \frac{\bar{V}_j V_j}{J}.$$



Large N Approach

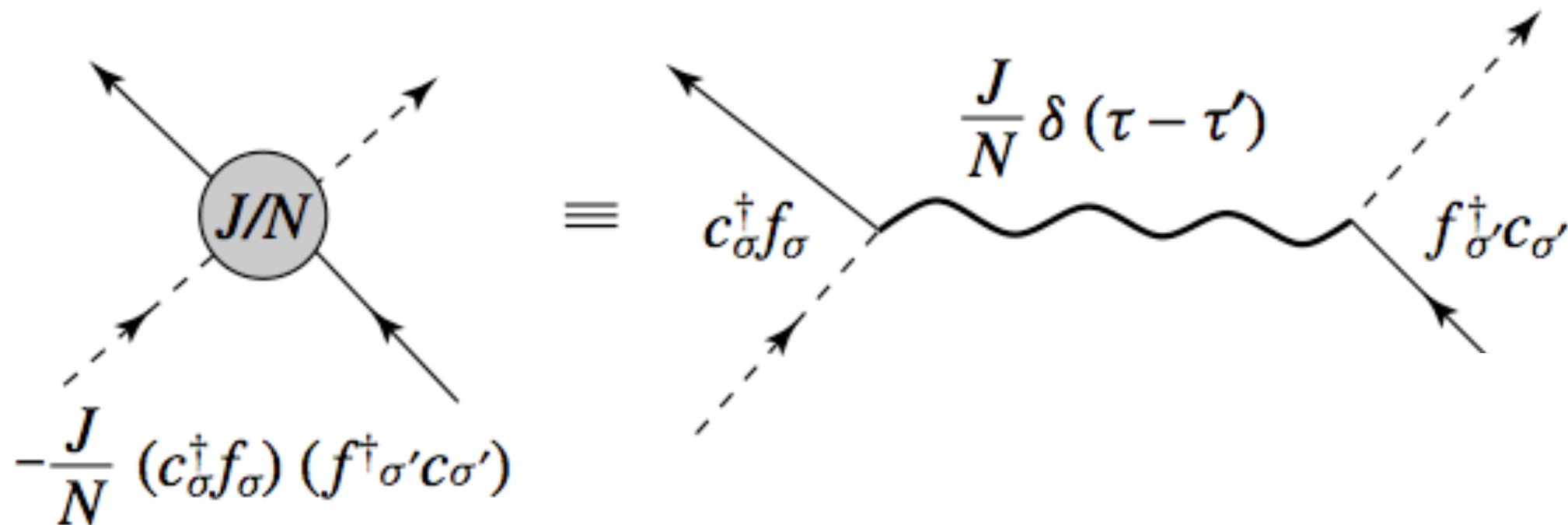
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Large N Approach

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$$H[V, \lambda] = \sum_{\mathbf{k}\sigma} \epsilon_{\mathbf{k}} c_{\mathbf{k}\sigma}^\dagger c_{\mathbf{k}\sigma} + \sum_j (H_I[V_j, j] + \lambda_j [n_f(j) - Q]),$$
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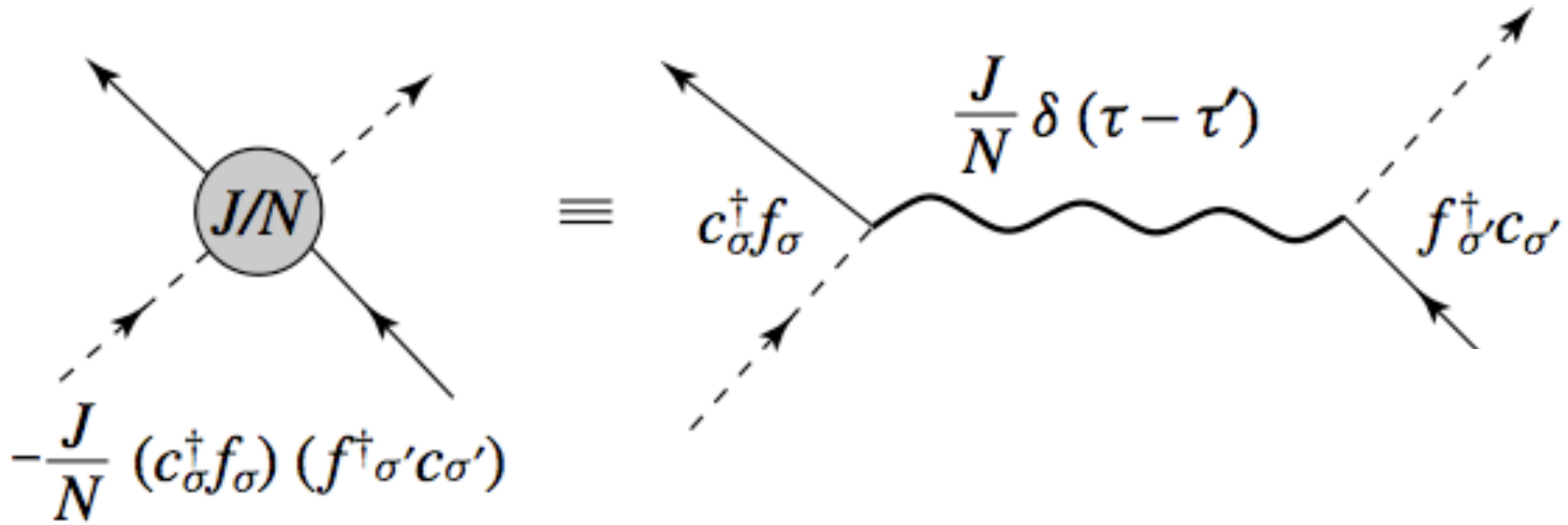
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U(1) constraint: note $n_f = Q = (qN)$



Large N Approach

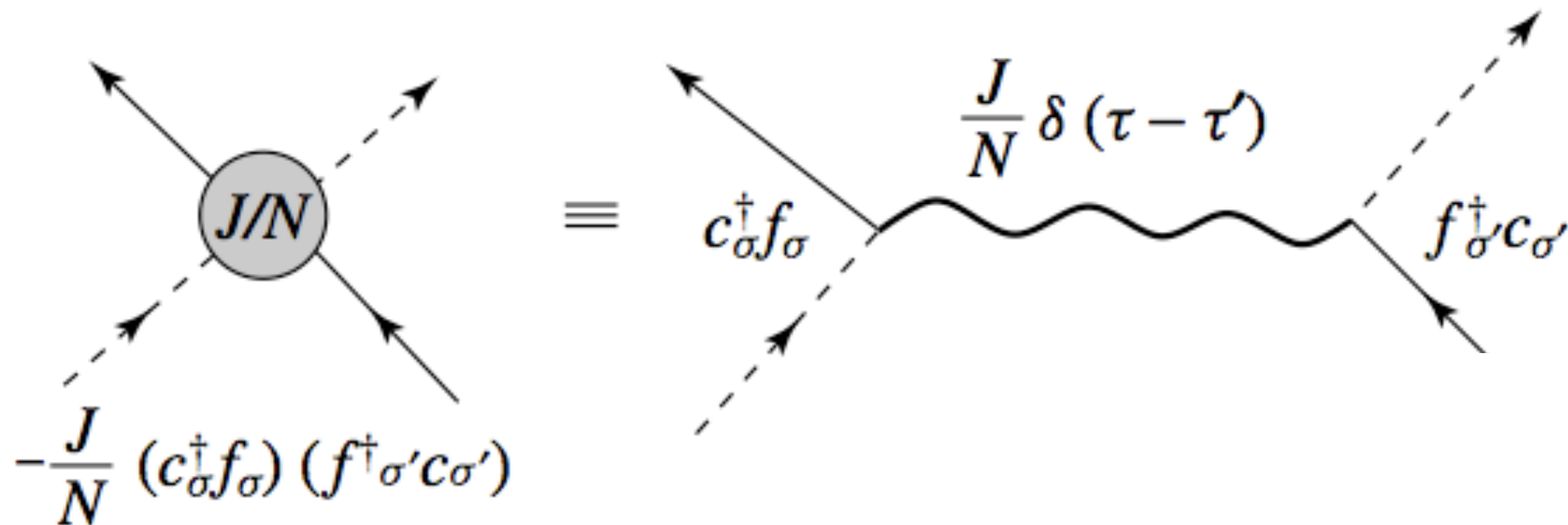
Read and Newns '83.

$$Z = \int \mathcal{D}[V, \lambda] \int \mathcal{D}[c, f] \exp \left[- \int_0^\beta \left(\sum_{k\sigma} c_{k\sigma}^\dagger \partial_\tau c_{k\sigma} + \sum_{j\sigma} f_{j\sigma}^\dagger \partial_\tau f_{j\sigma} + H[V, \lambda] \right) \right] = \text{Tr} \left[T \exp \left(- \int_0^\beta H[V, \lambda] d\tau \right) \right]$$

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Large N Approach

Read and Newns '83.

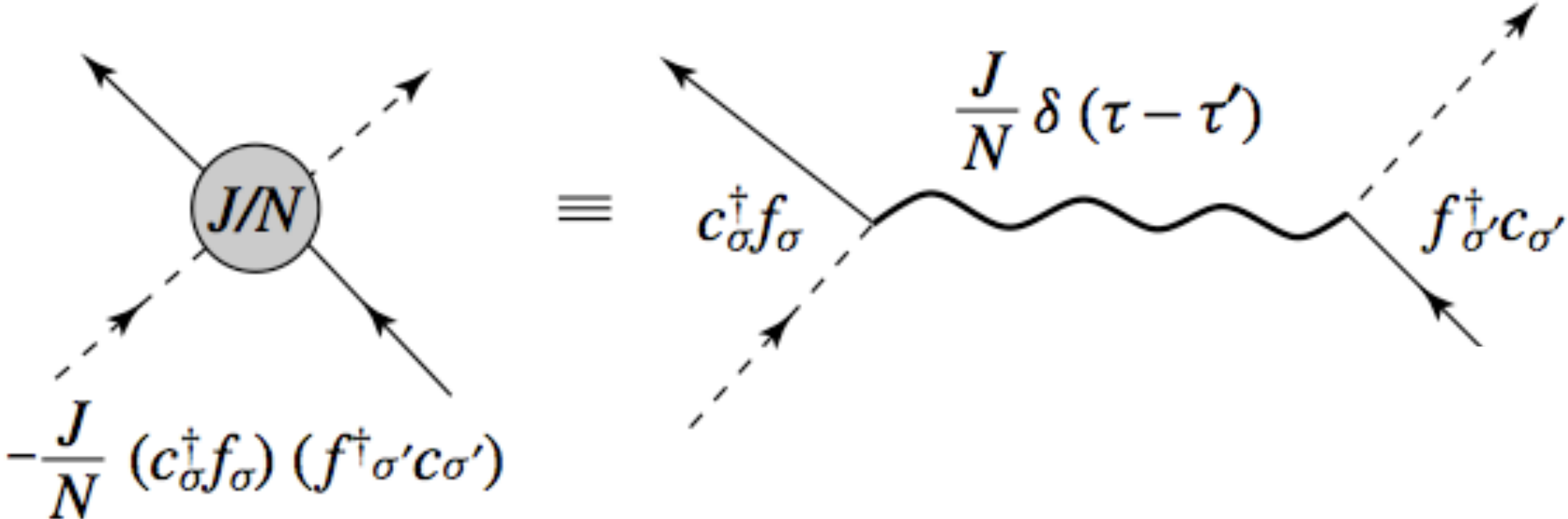
$=\text{Tr} \left[T \exp \left(- \int_0^\beta H[V, \lambda] d\tau \right) \right]$ Extensive in N

$$Z = \int \mathcal{D}[V, \lambda] \int \mathcal{D}[c, f] \exp \left[- \int_0^\beta \left(\sum_{k\sigma} c_{k\sigma}^\dagger \partial_\tau c_{k\sigma} + \sum_{j\sigma} f_{j\sigma}^\dagger \partial_\tau f_{j\sigma} + H[V, \lambda] \right) \right]$$

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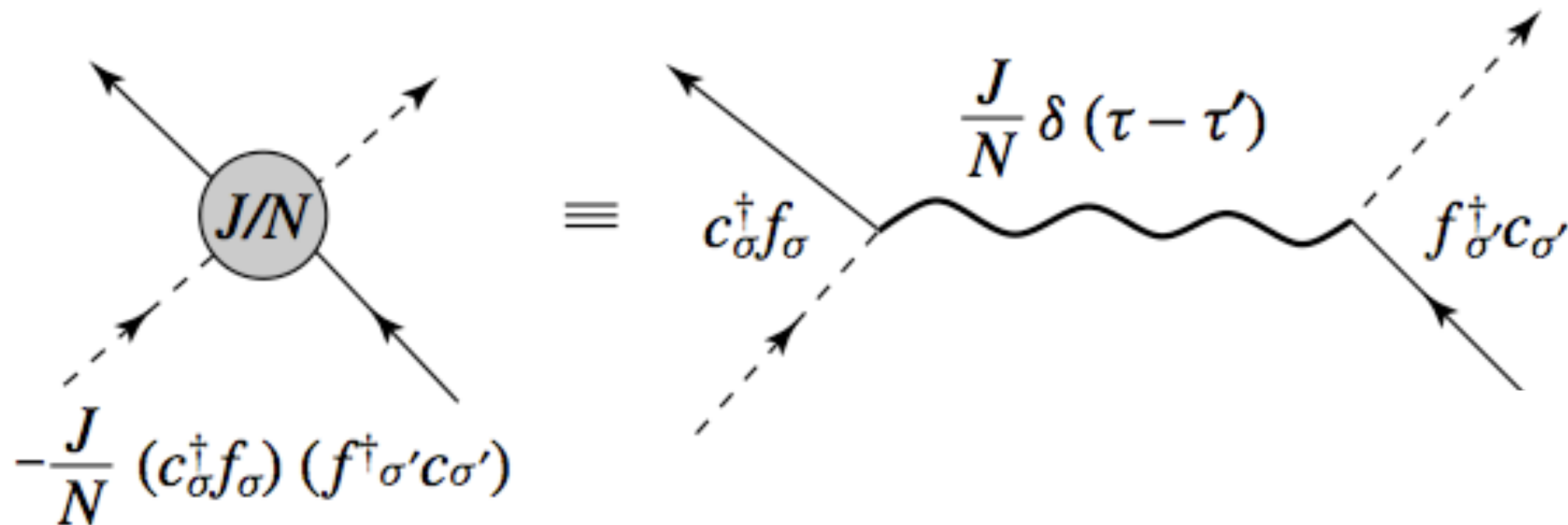
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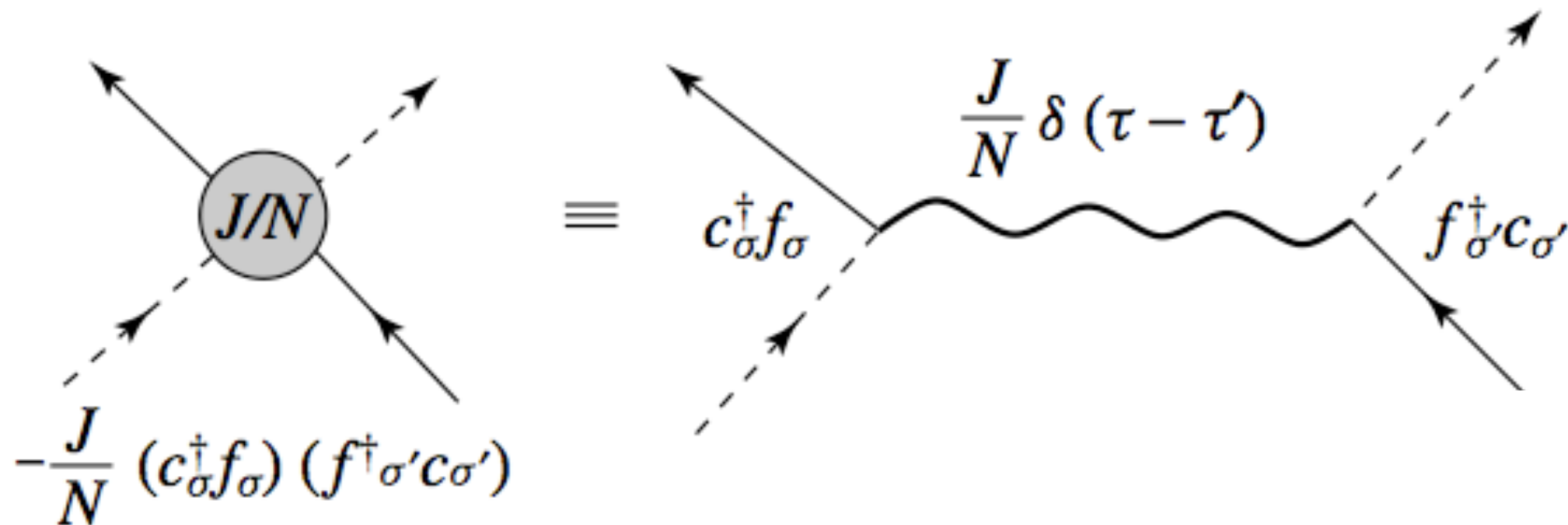


Large N Approach.

Read and Newns '83.

$$Z = \text{Tr} e^{-\beta H_{MFT}}, \quad (N \rightarrow \infty)$$

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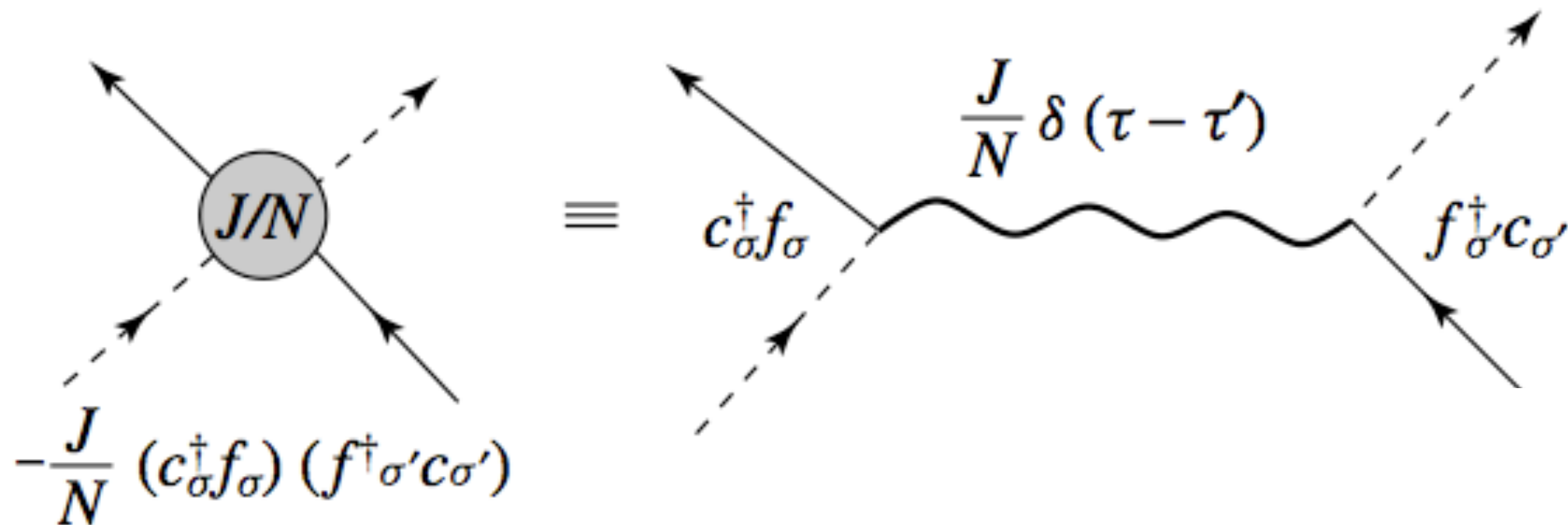


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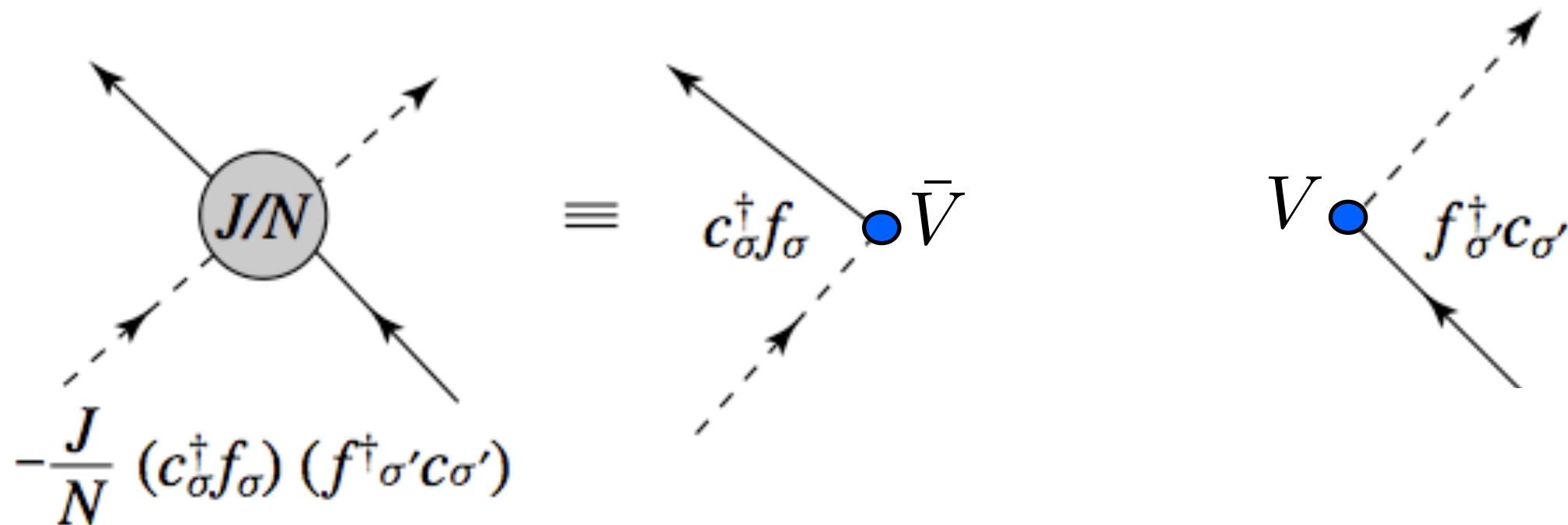
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$$Z = \text{Tr} e^{-\beta H_{MFT}}, \quad (N \rightarrow \infty)$$

$V_j = V$
at each site

$$H[V, \lambda] = \sum_{\mathbf{k}\sigma} \epsilon_{\mathbf{k}} c_{\mathbf{k}\sigma}^\dagger c_{\mathbf{k}\sigma} + \sum_j (H_I[V_j, j] + \lambda_j [n_f(j) - Q]),$$
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Detailed calcn.

$$\begin{aligned} H_{MFT} &= \sum_{\mathbf{k}\sigma} (c_{\mathbf{k}\sigma}^\dagger, f_{\mathbf{k}\sigma}^\dagger) \overbrace{\begin{pmatrix} \epsilon_{\mathbf{k}} & V \\ \bar{V} & \lambda \end{pmatrix}}^{h(\mathbf{k})} \begin{pmatrix} c_{\mathbf{k}\sigma} \\ f_{\mathbf{k}\sigma} \end{pmatrix} + N\mathcal{N}_s \left(\frac{|V|^2}{J} - \lambda q \right) \\ &= \sum_{\mathbf{k}\sigma} \psi_{\mathbf{k}\sigma}^\dagger \underline{h}(\mathbf{k}) \psi_{\mathbf{k}\sigma} + N\mathcal{N}_s \left(\frac{|V|^2}{J} - \lambda q \right). \end{aligned}$$

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$$f_{\vec{k}\sigma}^\dagger = \frac{1}{\sqrt{n}} \sum_j f_{j\sigma}^\dagger e^{i\vec{k}\cdot\vec{R}_j}$$

Detailed calcn.

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 &= \sum_{\mathbf{k}\sigma} \psi_{\mathbf{k}\sigma}^\dagger \underline{h}(\mathbf{k}) \psi_{\mathbf{k}\sigma} + N\mathcal{N}_s \left(\frac{|V|^2}{J} - \lambda q \right).
 \end{aligned}$$

$$f_{\vec{k}\sigma}^\dagger = \frac{1}{\sqrt{n}} \sum_j f_{j\sigma}^\dagger e^{i\vec{k}\cdot\vec{R}_j}$$

$$H_{MFT} = \sum_{\mathbf{k}\sigma} (a_{\mathbf{k}\sigma}^\dagger, b_{\mathbf{k}\sigma}^\dagger) \begin{pmatrix} E_{\mathbf{k}^+} & 0 \\ 0 & E_{\mathbf{k}^-} \end{pmatrix} \begin{pmatrix} a_{\mathbf{k}\sigma} \\ b_{\mathbf{k}\sigma} \end{pmatrix} + Nn \left(\frac{\bar{V}V}{J} - \lambda q \right).$$

Detailed calcn.

$$\begin{aligned}
 H_{MFT} &= \sum_{\mathbf{k}\sigma} (c_{\mathbf{k}\sigma}^\dagger, f_{\mathbf{k}\sigma}^\dagger) \overbrace{\begin{pmatrix} \epsilon_{\mathbf{k}} & V \\ \bar{V} & \lambda \end{pmatrix}}^{h(\mathbf{k})} \begin{pmatrix} c_{\mathbf{k}\sigma} \\ f_{\mathbf{k}\sigma} \end{pmatrix} + N\mathcal{N}_s \left(\frac{|V|^2}{J} - \lambda q \right) \\
 &= \sum_{\mathbf{k}\sigma} \psi_{\mathbf{k}\sigma}^\dagger \underline{h}(\mathbf{k}) \psi_{\mathbf{k}\sigma} + N\mathcal{N}_s \left(\frac{|V|^2}{J} - \lambda q \right).
 \end{aligned}$$

$$f_{\vec{k}\sigma}^\dagger = \frac{1}{\sqrt{n}} \sum_j f_{j\sigma}^\dagger e^{i\vec{k}\cdot\vec{R}_j}$$

$$H_{MFT} = \sum_{\mathbf{k}\sigma} (a_{\mathbf{k}\sigma}^\dagger, b_{\mathbf{k}\sigma}^\dagger) \begin{pmatrix} E_{\mathbf{k}^+} & 0 \\ 0 & E_{\mathbf{k}^-} \end{pmatrix} \begin{pmatrix} a_{\mathbf{k}\sigma} \\ b_{\mathbf{k}\sigma} \end{pmatrix} + Nn \left(\frac{\bar{V}V}{J} - \lambda q \right).$$

$$\text{Det} \left[E_{\mathbf{k}\pm}^\pm 1 - \begin{pmatrix} \epsilon_{\mathbf{k}} & V \\ \bar{V} & \lambda \end{pmatrix} \right] = (E_{\mathbf{k}\pm} - \epsilon_{\mathbf{k}})(E_{\mathbf{k}\pm} - \lambda) - |V|^2 = 0,$$

Detailed calcn.

$$\begin{aligned}
 H_{MFT} &= \sum_{\mathbf{k}\sigma} (c_{\mathbf{k}\sigma}^\dagger, f_{\mathbf{k}\sigma}^\dagger) \overbrace{\begin{pmatrix} \epsilon_{\mathbf{k}} & V \\ \bar{V} & \lambda \end{pmatrix}}^{h(\mathbf{k})} \begin{pmatrix} c_{\mathbf{k}\sigma} \\ f_{\mathbf{k}\sigma} \end{pmatrix} + N\mathcal{N}_s \left(\frac{|V|^2}{J} - \lambda q \right) \\
 &= \sum_{\mathbf{k}\sigma} \psi_{\mathbf{k}\sigma}^\dagger \underline{h}(\mathbf{k}) \psi_{\mathbf{k}\sigma} + N\mathcal{N}_s \left(\frac{|V|^2}{J} - \lambda q \right).
 \end{aligned}$$

$$f_{\vec{k}\sigma}^\dagger = \frac{1}{\sqrt{n}} \sum_j f_{j\sigma}^\dagger e^{i\vec{k}\cdot\vec{R}_j}$$

$$H_{MFT} = \sum_{\mathbf{k}\sigma} (a_{\mathbf{k}\sigma}^\dagger, b_{\mathbf{k}\sigma}^\dagger) \begin{pmatrix} E_{\mathbf{k}^+} & 0 \\ 0 & E_{\mathbf{k}^-} \end{pmatrix} \begin{pmatrix} a_{\mathbf{k}\sigma} \\ b_{\mathbf{k}\sigma} \end{pmatrix} + Nn \left(\frac{\bar{V}V}{J} - \lambda q \right).$$

$$\text{Det} \left[E_{\mathbf{k}\pm} 1 - \begin{pmatrix} \epsilon_{\mathbf{k}} & V \\ \bar{V} & \lambda \end{pmatrix} \right] = (E_{\mathbf{k}\pm} - \epsilon_{\mathbf{k}})(E_{\mathbf{k}\pm} - \lambda) - |V|^2 = 0,$$

$$E_{\mathbf{k}\pm} = \frac{\epsilon_{\mathbf{k}} + \lambda}{2} \pm \left[\left(\frac{\epsilon_{\mathbf{k}} - \lambda}{2} \right)^2 + |V|^2 \right]^{\frac{1}{2}},$$

Detailed calcn.

$$\begin{aligned}
 H_{MFT} &= \sum_{\mathbf{k}\sigma} (c_{\mathbf{k}\sigma}^\dagger, f_{\mathbf{k}\sigma}^\dagger) \overbrace{\begin{pmatrix} \epsilon_{\mathbf{k}} & V \\ \bar{V} & \lambda \end{pmatrix}}^{h(\mathbf{k})} \begin{pmatrix} c_{\mathbf{k}\sigma} \\ f_{\mathbf{k}\sigma} \end{pmatrix} + N\mathcal{N}_s \left(\frac{|V|^2}{J} - \lambda q \right) \\
 &= \sum_{\mathbf{k}\sigma} \psi_{\mathbf{k}\sigma}^\dagger \underline{h}(\mathbf{k}) \psi_{\mathbf{k}\sigma} + N\mathcal{N}_s \left(\frac{|V|^2}{J} - \lambda q \right).
 \end{aligned}$$

$$f_{\vec{k}\sigma}^\dagger = \frac{1}{\sqrt{n}} \sum_j f_{j\sigma}^\dagger e^{i\vec{k}\cdot\vec{R}_j}$$

$$H_{MFT} = \sum_{\mathbf{k}\sigma} (a_{\mathbf{k}\sigma}^\dagger, b_{\mathbf{k}\sigma}^\dagger) \begin{pmatrix} E_{\mathbf{k}^+} & 0 \\ 0 & E_{\mathbf{k}^-} \end{pmatrix} \begin{pmatrix} a_{\mathbf{k}\sigma} \\ b_{\mathbf{k}\sigma} \end{pmatrix} + Nn \left(\frac{\bar{V}V}{J} - \lambda q \right).$$

$$\text{Det} \left[E_{\mathbf{k}\pm} - \begin{pmatrix} \epsilon_{\mathbf{k}} & V \\ \bar{V} & \lambda \end{pmatrix} \right] = (E_{\mathbf{k}\pm} - \epsilon_{\mathbf{k}})(E_{\mathbf{k}\pm} - \lambda) - |V|^2 = 0,$$

$$E_{\mathbf{k}\pm} = \frac{\epsilon_{\mathbf{k}} + \lambda}{2} \pm \left[\left(\frac{\epsilon_{\mathbf{k}} - \lambda}{2} \right)^2 + |V|^2 \right]^{\frac{1}{2}},$$

Detailed calcn.

$$E_{\mathbf{k}\pm} = \frac{\epsilon_{\mathbf{k}} + \lambda}{2} \pm \left[\left(\frac{\epsilon_{\mathbf{k}} - \lambda}{2} \right)^2 + |V|^2 \right]^{\frac{1}{2}},$$

Detailed calcn.

$$E_{\mathbf{k}\pm} = \frac{\epsilon_{\mathbf{k}} + \lambda}{2} \pm \left[\left(\frac{\epsilon_{\mathbf{k}} - \lambda}{2} \right)^2 + |V|^2 \right]^{\frac{1}{2}},$$

Detailed calcn.

$$E_{\mathbf{k}\pm} = \frac{\epsilon_{\mathbf{k}} + \lambda}{2} \pm \left[\left(\frac{\epsilon_{\mathbf{k}} - \lambda}{2} \right)^2 + |V|^2 \right]^{\frac{1}{2}},$$

$$a_{\mathbf{k}\sigma}^\dagger = u_{\mathbf{k}} c_{\mathbf{k}\sigma}^\dagger + v_{\mathbf{k}} f_{\mathbf{k}\sigma}^\dagger$$

$$b_{\mathbf{k}\sigma}^\dagger = -v_{\mathbf{k}} c_{\mathbf{k}\sigma}^\dagger + u_{\mathbf{k}} f_{\mathbf{k}\sigma}^\dagger$$

Detailed calcn.

$$E_{\mathbf{k}\pm} = \frac{\epsilon_{\mathbf{k}} + \lambda}{2} \pm \left[\left(\frac{\epsilon_{\mathbf{k}} - \lambda}{2} \right)^2 + |V|^2 \right]^{\frac{1}{2}},$$

$$\begin{aligned} a_{\mathbf{k}\sigma}^\dagger &= u_{\mathbf{k}} c_{\mathbf{k}\sigma}^\dagger + v_{\mathbf{k}} f_{\mathbf{k}\sigma}^\dagger \\ b_{\mathbf{k}\sigma}^\dagger &= -v_{\mathbf{k}} c_{\mathbf{k}\sigma}^\dagger + u_{\mathbf{k}} f_{\mathbf{k}\sigma}^\dagger \end{aligned} \quad \left\{ \begin{array}{c} u_{\mathbf{k}} \\ v_{\mathbf{k}} \end{array} \right\} = \left[\frac{1}{2} \pm \frac{(\epsilon_{\mathbf{k}} - \lambda)/2}{2 \sqrt{\left(\frac{\epsilon_{\mathbf{k}} - \lambda}{2}\right)^2 + |V|^2}} \right]^{\frac{1}{2}}.$$

Detailed calcn.

$$E_{\mathbf{k}\pm} = \frac{\epsilon_{\mathbf{k}} + \lambda}{2} \pm \left[\left(\frac{\epsilon_{\mathbf{k}} - \lambda}{2} \right)^2 + |V|^2 \right]^{\frac{1}{2}},$$

$$|MF\rangle = \prod_{|\mathbf{k}| < k_F, \sigma} b_{\mathbf{k}\sigma}^\dagger = \prod_{|\mathbf{k}| < k_F, \sigma} (-v_{\mathbf{k}} c_{\mathbf{k}\sigma}^\dagger + u_{\mathbf{k}} f_{\mathbf{k}\sigma}^\dagger) |0\rangle$$

$$\begin{aligned} a_{\mathbf{k}\sigma}^\dagger &= u_{\mathbf{k}} c_{\mathbf{k}\sigma}^\dagger + v_{\mathbf{k}} f_{\mathbf{k}\sigma}^\dagger \\ b_{\mathbf{k}\sigma}^\dagger &= -v_{\mathbf{k}} c_{\mathbf{k}\sigma}^\dagger + u_{\mathbf{k}} f_{\mathbf{k}\sigma}^\dagger \end{aligned} \quad \left\{ \begin{array}{c} u_{\mathbf{k}} \\ v_{\mathbf{k}} \end{array} \right\} = \left[\frac{1}{2} \pm \frac{(\epsilon_{\mathbf{k}} - \lambda)/2}{2 \sqrt{\left(\frac{\epsilon_{\mathbf{k}} - \lambda}{2}\right)^2 + |V|^2}} \right]^{\frac{1}{2}}$$

Detailed calcn.

$$E_{\mathbf{k}\pm} = \frac{\epsilon_{\mathbf{k}} + \lambda}{2} \pm \left[\left(\frac{\epsilon_{\mathbf{k}} - \lambda}{2} \right)^2 + |V|^2 \right]^{\frac{1}{2}},$$

$$\begin{aligned} a_{\mathbf{k}\sigma}^\dagger &= u_{\mathbf{k}} c_{\mathbf{k}\sigma}^\dagger + v_{\mathbf{k}} f_{\mathbf{k}\sigma}^\dagger \\ b_{\mathbf{k}\sigma}^\dagger &= -v_{\mathbf{k}} c_{\mathbf{k}\sigma}^\dagger + u_{\mathbf{k}} f_{\mathbf{k}\sigma}^\dagger \end{aligned} \quad \left\{ \begin{array}{l} u_{\mathbf{k}} \\ v_{\mathbf{k}} \end{array} \right\} = \left[\frac{1}{2} \pm \frac{(\epsilon_{\mathbf{k}} - \lambda)/2}{2 \sqrt{\left(\frac{\epsilon_{\mathbf{k}} - \lambda}{2}\right)^2 + |V|^2}} \right]^{\frac{1}{2}}$$

$$|MF\rangle = \prod_{|\mathbf{k}| < k_F, \sigma} b_{\mathbf{k}\sigma}^\dagger = \prod_{|\mathbf{k}| < k_F, \sigma} (-v_{\mathbf{k}} c_{\mathbf{k}\sigma}^\dagger + u_{\mathbf{k}} f_{\mathbf{k}\sigma}^\dagger) |0\rangle$$

$$|GW\rangle = P_Q \prod_{|\mathbf{k}| < k_F, \sigma} (-v_{\mathbf{k}} c_{\mathbf{k}\sigma}^\dagger + u_{\mathbf{k}} f_{\mathbf{k}\sigma}^\dagger) |0\rangle$$

“Gutzwiller” wavefunction

Detailed calcn.

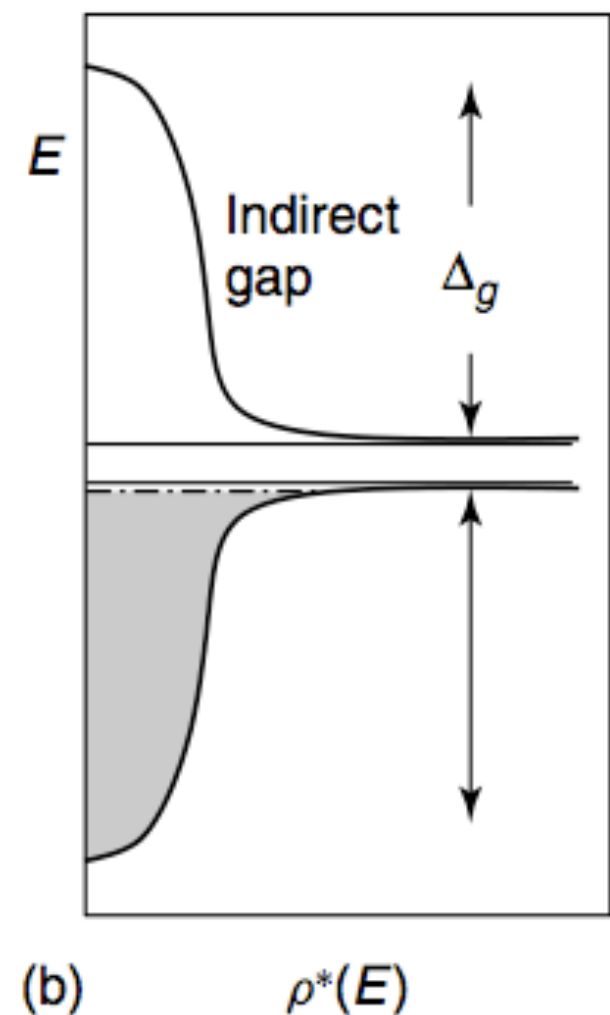
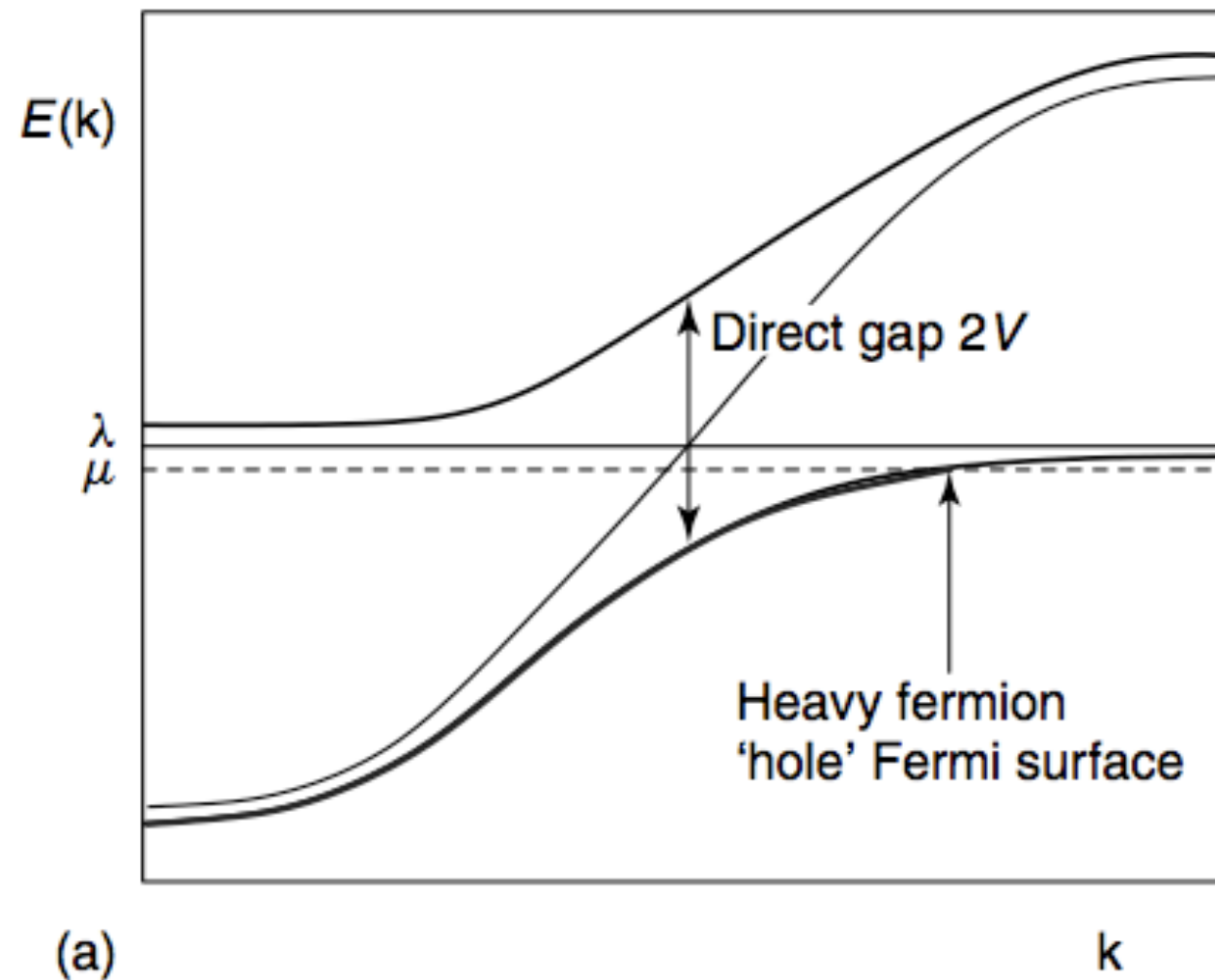
$$E_{\mathbf{k}\pm} = \frac{\epsilon_{\mathbf{k}} + \lambda}{2} \pm \left[\left(\frac{\epsilon_{\mathbf{k}} - \lambda}{2} \right)^2 + |V|^2 \right]^{\frac{1}{2}},$$

$$|MF\rangle = \prod_{|\mathbf{k}| < k_F, \sigma} b_{\mathbf{k}\sigma}^\dagger = \prod_{|\mathbf{k}| < k_F, \sigma} (-v_{\mathbf{k}} c_{\mathbf{k}\sigma}^\dagger + u_{\mathbf{k}} f_{\mathbf{k}\sigma}^\dagger) |0\rangle$$

$$\begin{aligned} a_{\mathbf{k}\sigma}^\dagger &= u_{\mathbf{k}} c_{\mathbf{k}\sigma}^\dagger + v_{\mathbf{k}} f_{\mathbf{k}\sigma}^\dagger \\ b_{\mathbf{k}\sigma}^\dagger &= -v_{\mathbf{k}} c_{\mathbf{k}\sigma}^\dagger + u_{\mathbf{k}} f_{\mathbf{k}\sigma}^\dagger \end{aligned} \quad \left\{ \begin{array}{l} u_{\mathbf{k}} \\ v_{\mathbf{k}} \end{array} \right\} = \left[\frac{1}{2} \pm \frac{(\epsilon_{\mathbf{k}} - \lambda)/2}{2 \sqrt{\left(\frac{\epsilon_{\mathbf{k}} - \lambda}{2}\right)^2 + |V|^2}} \right]^{\frac{1}{2}}$$

$$|GW\rangle = P_Q \prod_{|\mathbf{k}| < k_F, \sigma} (-v_{\mathbf{k}} c_{\mathbf{k}\sigma}^\dagger + u_{\mathbf{k}} f_{\mathbf{k}\sigma}^\dagger) |0\rangle$$

“Gutzwiller” wavefunction



Detailed calcn.

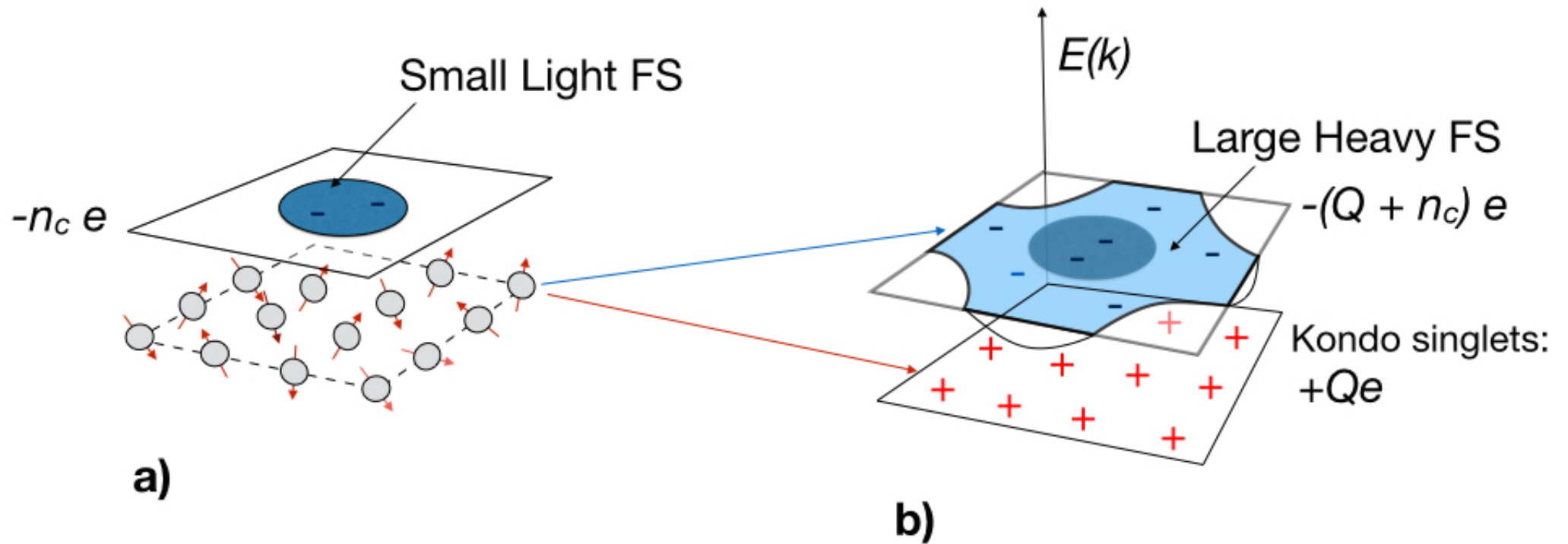
$$E_{\mathbf{k}\pm} = \frac{\epsilon_{\mathbf{k}} + \lambda}{2} \pm \left[\left(\frac{\epsilon_{\mathbf{k}} - \lambda}{2} \right)^2 + |V|^2 \right]^{\frac{1}{2}},$$

$$\begin{aligned} a_{\mathbf{k}\sigma}^\dagger &= u_{\mathbf{k}} c_{\mathbf{k}\sigma}^\dagger + v_{\mathbf{k}} f_{\mathbf{k}\sigma}^\dagger \\ b_{\mathbf{k}\sigma}^\dagger &= -v_{\mathbf{k}} c_{\mathbf{k}\sigma}^\dagger + u_{\mathbf{k}} f_{\mathbf{k}\sigma}^\dagger \end{aligned} \quad \left\{ \begin{array}{l} u_{\mathbf{k}} \\ v_{\mathbf{k}} \end{array} \right\} = \left[\frac{1}{2} \pm \frac{(\epsilon_{\mathbf{k}} - \lambda)/2}{2 \sqrt{\left(\frac{\epsilon_{\mathbf{k}} - \lambda}{2}\right)^2 + |V|^2}} \right]^{\frac{1}{2}}$$

$$|MF\rangle = \prod_{|\mathbf{k}| < k_F, \sigma} b_{\mathbf{k}\sigma}^\dagger = \prod_{|\mathbf{k}| < k_F, \sigma} (-v_{\mathbf{k}} c_{\mathbf{k}\sigma}^\dagger + u_{\mathbf{k}} f_{\mathbf{k}\sigma}^\dagger) |0\rangle$$

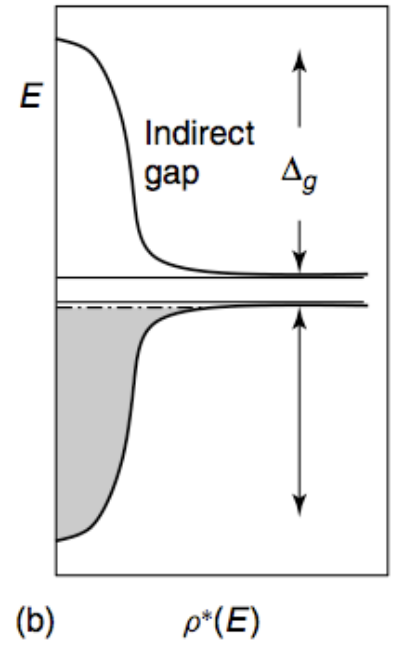
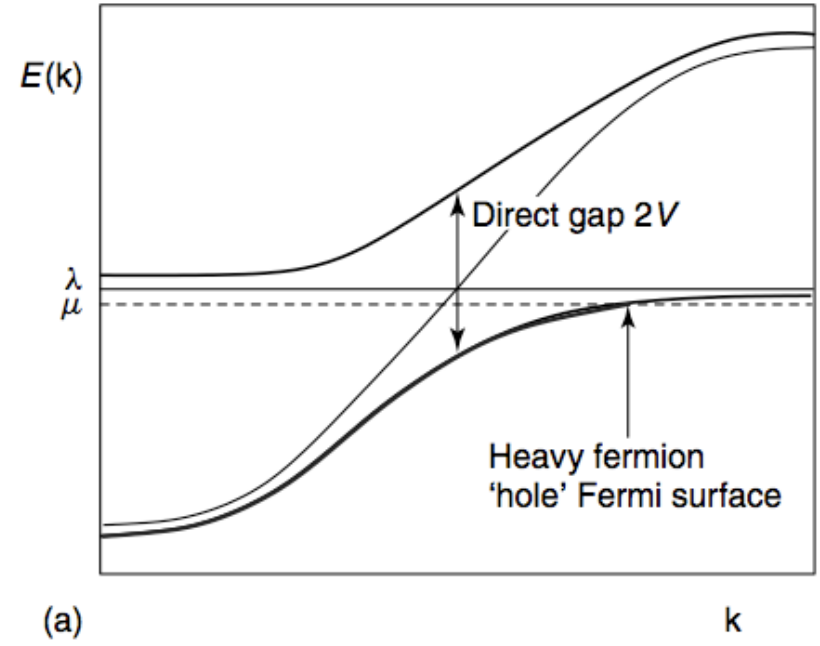
$$|GW\rangle = P_Q \prod_{|\mathbf{k}| < k_F, \sigma} (-v_{\mathbf{k}} c_{\mathbf{k}\sigma}^\dagger + u_{\mathbf{k}} f_{\mathbf{k}\sigma}^\dagger) |0\rangle$$

“Gutzwiller” wavefunction



Detailed calcn.

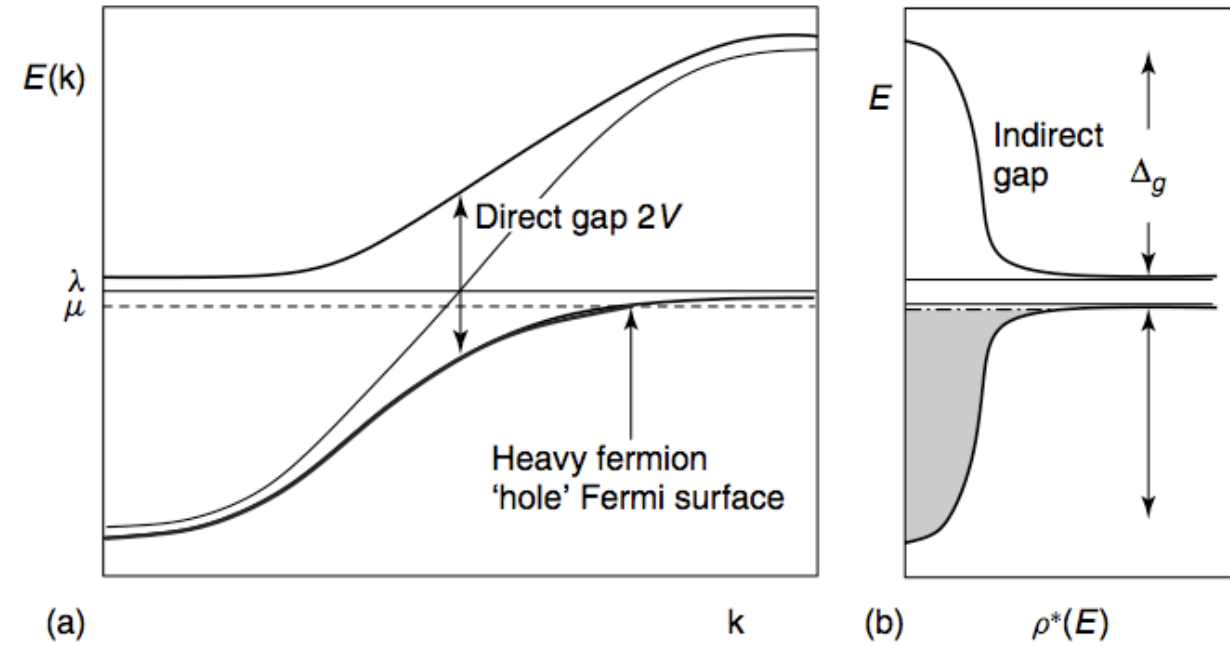
$$E_{\mathbf{k}\pm} = \frac{\epsilon_{\mathbf{k}} + \lambda}{2} \pm \left[\left(\frac{\epsilon_{\mathbf{k}} - \lambda}{2} \right)^2 + |V|^2 \right]^{\frac{1}{2}},$$



Detailed calcn.

$$E_{\mathbf{k}\pm} = \frac{\epsilon_{\mathbf{k}} + \lambda}{2} \pm \left[\left(\frac{\epsilon_{\mathbf{k}} - \lambda}{2} \right)^2 + |V|^2 \right]^{\frac{1}{2}},$$

$$\frac{F}{N} = -T \sum_{\mathbf{k}, \pm} \ln \left[1 + e^{-\beta E_{\mathbf{k}\pm}} \right] + \mathcal{N}_s \left(\frac{V^2}{J} - \lambda q \right).$$

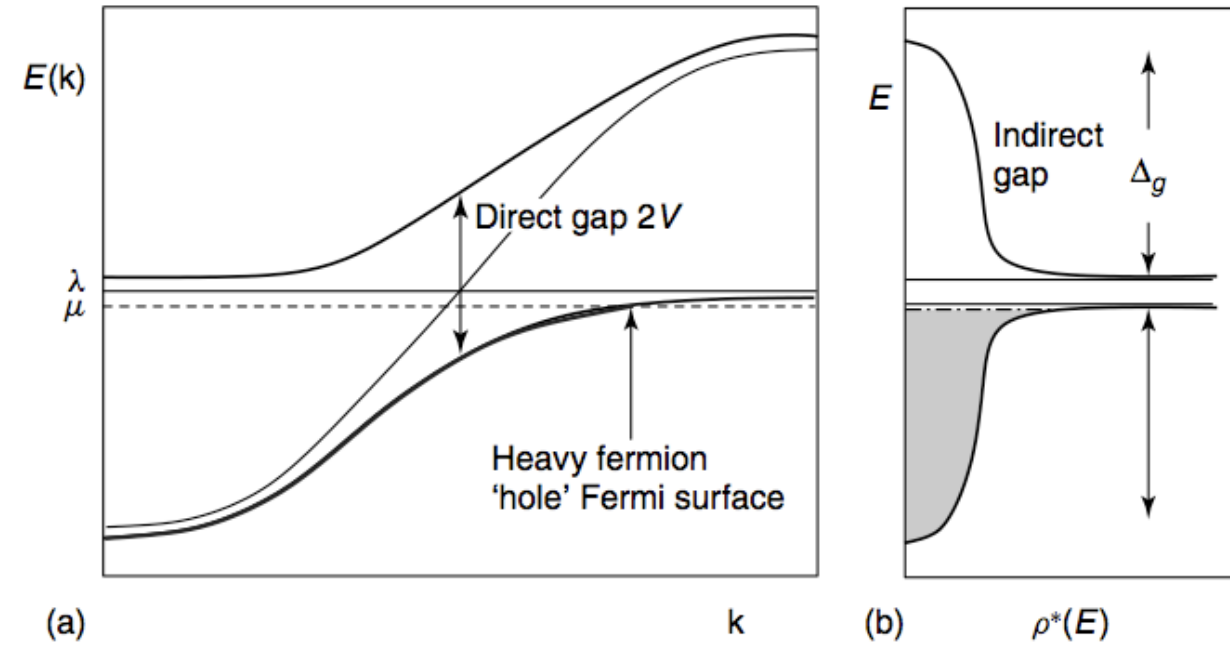


Detailed calcn.

$$E_{\mathbf{k}\pm} = \frac{\epsilon_{\mathbf{k}} + \lambda}{2} \pm \left[\left(\frac{\epsilon_{\mathbf{k}} - \lambda}{2} \right)^2 + |V|^2 \right]^{\frac{1}{2}},$$

$$\frac{F}{N} = -T \sum_{\mathbf{k}, \pm} \ln \left[1 + e^{-\beta E_{\mathbf{k}\pm}} \right] + \mathcal{N}_s \left(\frac{V^2}{J} - \lambda q \right).$$

$$\frac{E_o}{N \mathcal{N}_s} = \int_{-\infty}^0 dE \rho^*(E) E + \left(\frac{V^2}{J} - \lambda q \right)$$



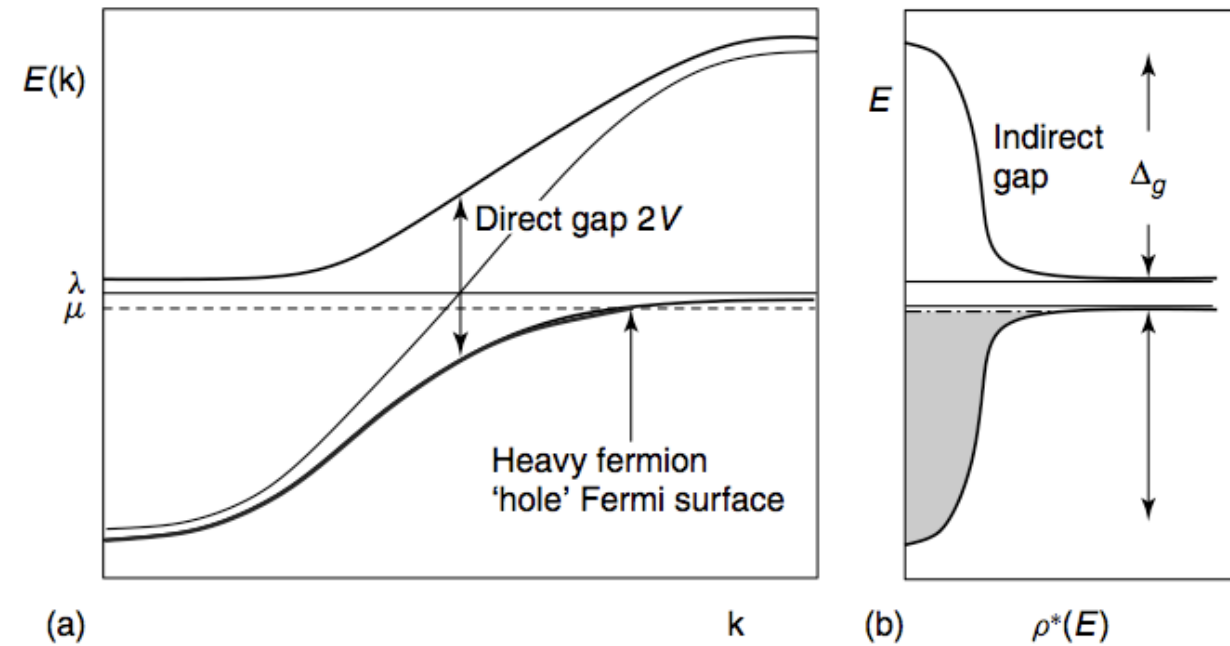
Detailed calcn.

$$E_{\mathbf{k}\pm} = \frac{\epsilon_{\mathbf{k}} + \lambda}{2} \pm \left[\left(\frac{\epsilon_{\mathbf{k}} - \lambda}{2} \right)^2 + |V|^2 \right]^{\frac{1}{2}},$$

$$\frac{F}{N} = -T \sum_{\mathbf{k}, \pm} \ln \left[1 + e^{-\beta E_{\mathbf{k}\pm}} \right] + \mathcal{N}_s \left(\frac{V^2}{J} - \lambda q \right).$$

$$\frac{E_o}{N \mathcal{N}_s} = \int_{-\infty}^0 dE \rho^*(E) E + \left(\frac{V^2}{J} - \lambda q \right)$$

$$E = \epsilon + \frac{V^2}{E - \lambda}$$



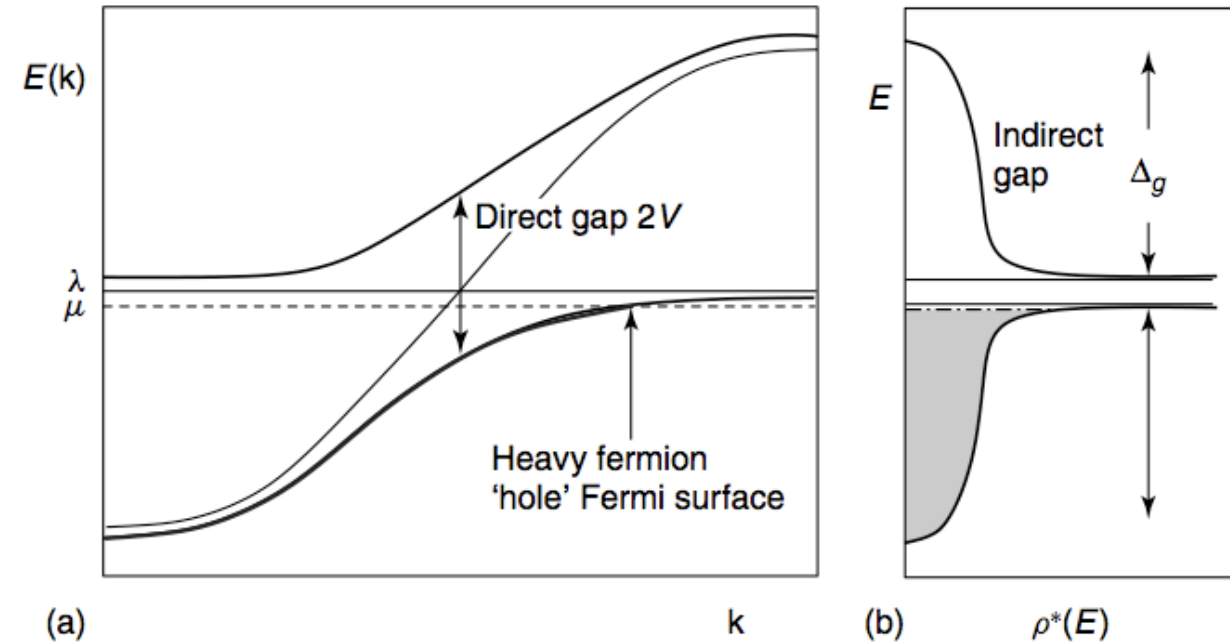
Detailed calcn.

$$E_{\mathbf{k}\pm} = \frac{\epsilon_{\mathbf{k}} + \lambda}{2} \pm \left[\left(\frac{\epsilon_{\mathbf{k}} - \lambda}{2} \right)^2 + |V|^2 \right]^{\frac{1}{2}},$$

$$\frac{F}{N} = -T \sum_{\mathbf{k}, \pm} \ln \left[1 + e^{-\beta E_{\mathbf{k}\pm}} \right] + \mathcal{N}_s \left(\frac{V^2}{J} - \lambda q \right).$$

$$\frac{E_o}{N \mathcal{N}_s} = \int_{-\infty}^0 dE \rho^*(E) E + \left(\frac{V^2}{J} - \lambda q \right)$$

$$E = \epsilon + \frac{V^2}{E - \lambda} \quad \rho^*(E) = \rho \frac{d\epsilon}{dE} = \rho \left(1 + \frac{V^2}{(E - \lambda)^2} \right)$$



Detailed calcn.

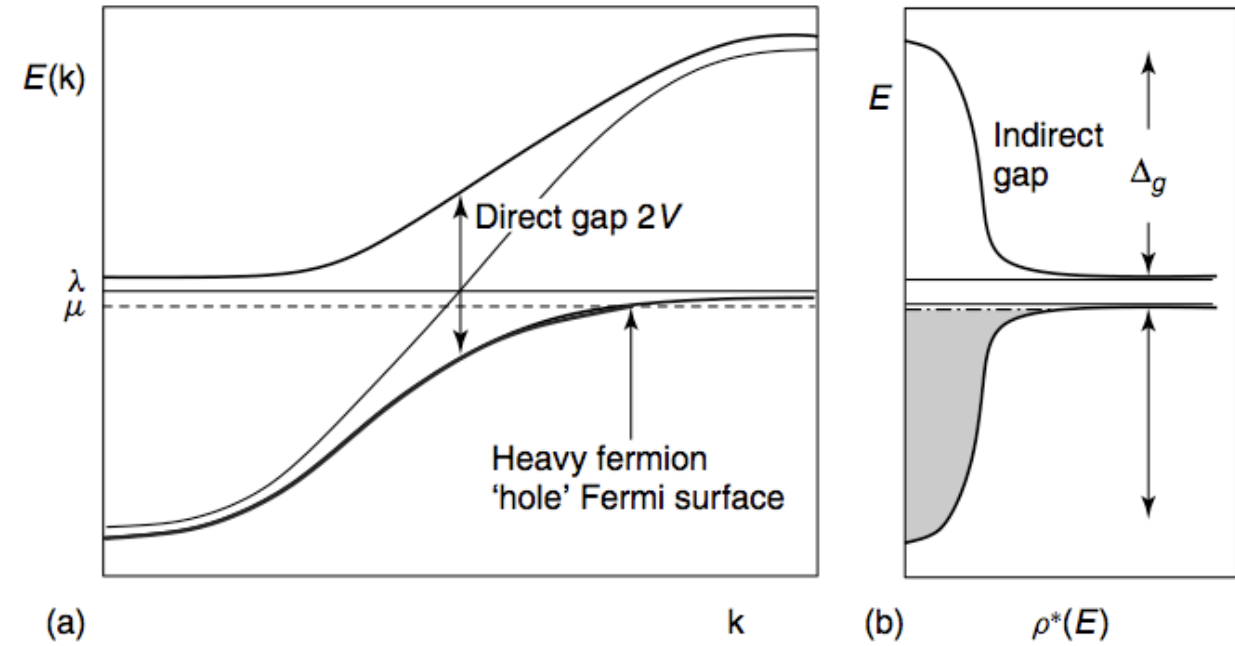
$$E_{\mathbf{k}\pm} = \frac{\epsilon_{\mathbf{k}} + \lambda}{2} \pm \left[\left(\frac{\epsilon_{\mathbf{k}} - \lambda}{2} \right)^2 + |V|^2 \right]^{\frac{1}{2}},$$

$$\frac{F}{N} = -T \sum_{\mathbf{k}, \pm} \ln \left[1 + e^{-\beta E_{\mathbf{k}\pm}} \right] + \mathcal{N}_s \left(\frac{V^2}{J} - \lambda q \right).$$

$$\frac{E_o}{N \mathcal{N}_s} = \int_{-\infty}^0 dE \rho^*(E) E + \left(\frac{V^2}{J} - \lambda q \right)$$

$$E = \epsilon + \frac{V^2}{E - \lambda} \quad \rho^*(E) = \rho \frac{d\epsilon}{dE} = \rho \left(1 + \frac{V^2}{(E - \lambda)^2} \right)$$

$$\frac{E_o}{N \mathcal{N}_s} = \rho \int_{-D-V^2/D}^0 dE E \left(1 + \frac{V^2}{(E - \lambda)^2} \right) + \left(\frac{V^2}{J} - \lambda q \right)$$



Detailed calcn.

$$E_{\mathbf{k}\pm} = \frac{\epsilon_{\mathbf{k}} + \lambda}{2} \pm \left[\left(\frac{\epsilon_{\mathbf{k}} - \lambda}{2} \right)^2 + |V|^2 \right]^{\frac{1}{2}},$$

$$\frac{F}{N} = -T \sum_{\mathbf{k}, \pm} \ln \left[1 + e^{-\beta E_{\mathbf{k}\pm}} \right] + \mathcal{N}_s \left(\frac{V^2}{J} - \lambda q \right).$$

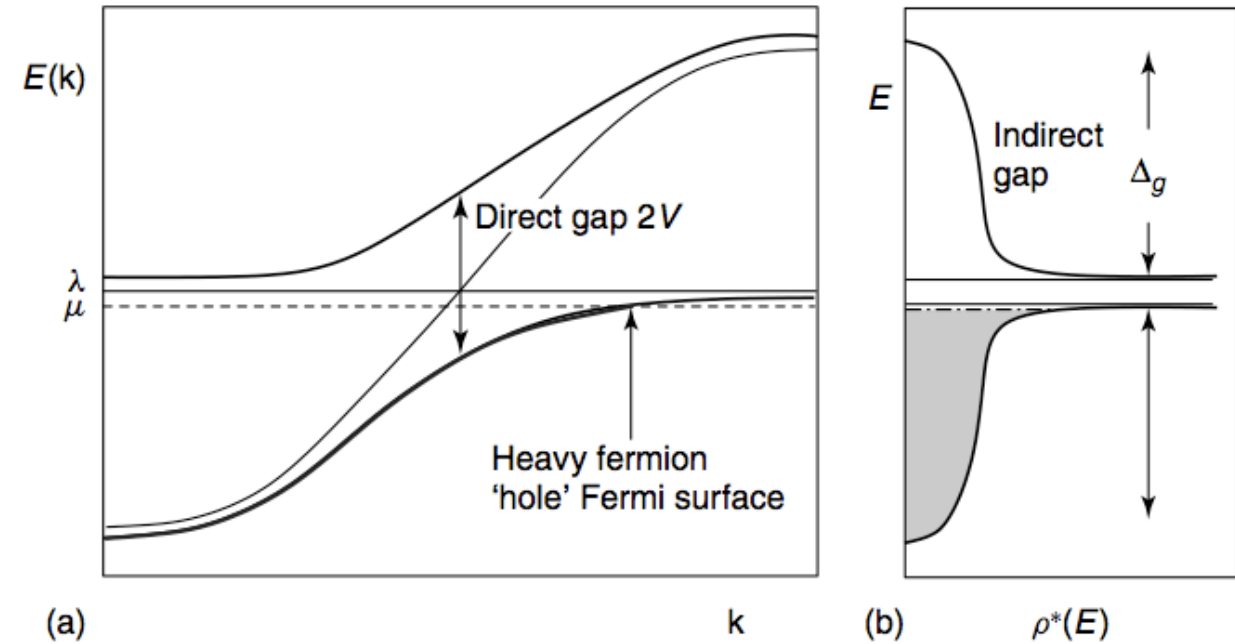
$$\frac{E_o}{N\mathcal{N}_s} = \int_{-\infty}^0 dE \rho^*(E) E + \left(\frac{V^2}{J} - \lambda q \right)$$

$$E = \epsilon + \frac{V^2}{E - \lambda} \quad \rho^*(E) = \rho \frac{d\epsilon}{dE} = \rho \left(1 + \frac{V^2}{(E - \lambda)^2} \right)$$

$$\frac{E_o}{N\mathcal{N}_s} = \rho \int_{-D-V^2/D}^0 dE E \left(1 + \frac{V^2}{(E - \lambda)^2} \right) + \left(\frac{V^2}{J} - \lambda q \right)$$

$$\begin{aligned} \frac{E_o}{N\mathcal{N}_s} &= -\frac{\rho}{2} \left(D + \frac{V^2}{D} \right)^2 + \frac{\Delta}{\pi} \int_{-D}^0 dE \left(\frac{1}{E - \lambda} + \frac{\lambda}{(E - \lambda)^2} \right) + \left(\frac{V^2}{J} - \lambda q \right) \\ &= -\frac{D^2 \rho}{2} + \frac{\Delta}{\pi} \ln \left(\frac{\lambda}{D} \right) + \left(\frac{V^2}{J} - \lambda q \right) \end{aligned}$$

$$(\Delta = \pi \rho |V|^2)$$



Detailed calcn.

$$E_{\mathbf{k}\pm} = \frac{\epsilon_{\mathbf{k}} + \lambda}{2} \pm \left[\left(\frac{\epsilon_{\mathbf{k}} - \lambda}{2} \right)^2 + |V|^2 \right]^{\frac{1}{2}},$$

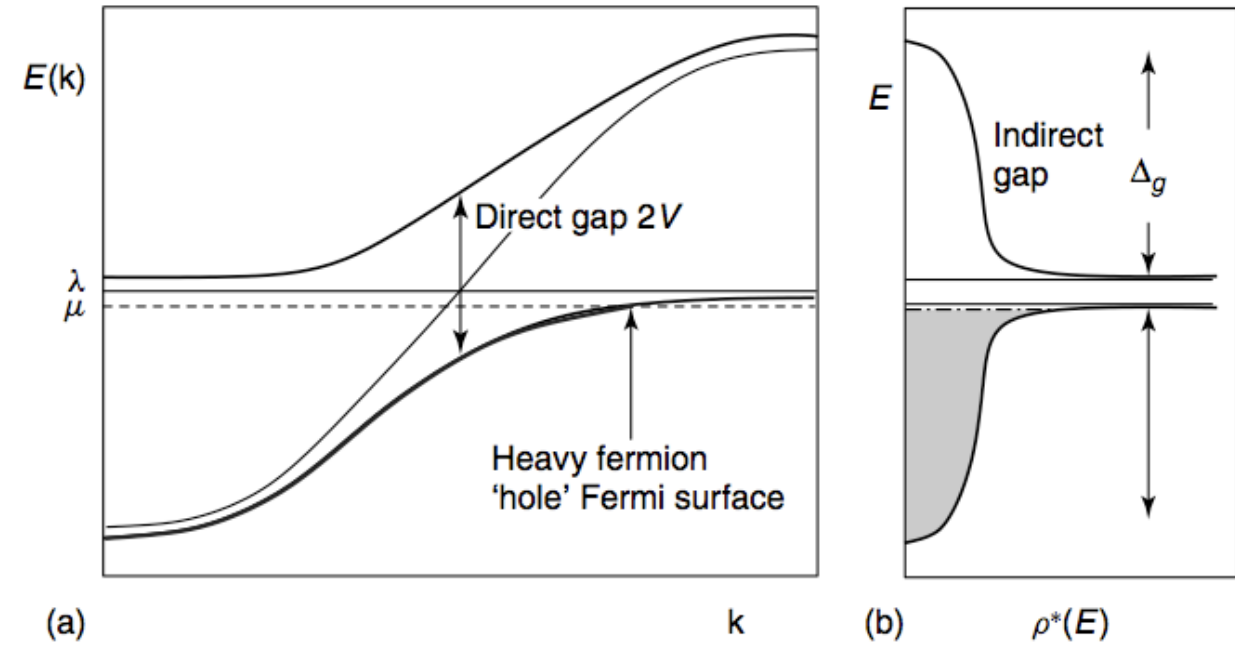
$$\frac{F}{N} = -T \sum_{\mathbf{k}, \pm} \ln \left[1 + e^{-\beta E_{\mathbf{k}\pm}} \right] + \mathcal{N}_s \left(\frac{V^2}{J} - \lambda q \right).$$

$$\frac{E_o}{N\mathcal{N}_s} = \int_{-\infty}^0 dE \rho^*(E) E + \left(\frac{V^2}{J} - \lambda q \right)$$

$$E = \epsilon + \frac{V^2}{E - \lambda} \quad \rho^*(E) = \rho \frac{d\epsilon}{dE} = \rho \left(1 + \frac{V^2}{(E - \lambda)^2} \right)$$

$$\frac{E_o}{N\mathcal{N}_s} = \rho \int_{-D-V^2/D}^0 dE E \left(1 + \frac{V^2}{(E - \lambda)^2} \right) + \left(\frac{V^2}{J} - \lambda q \right)$$

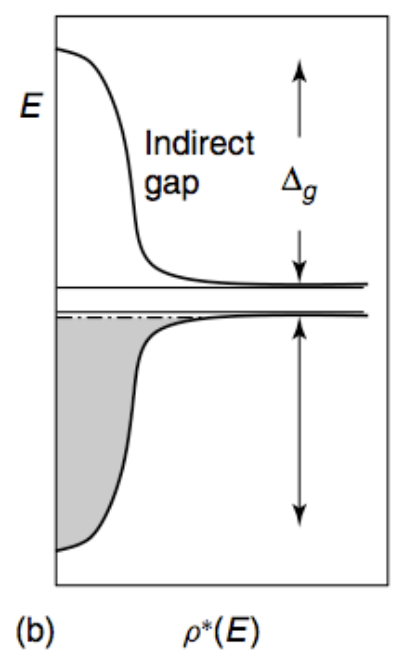
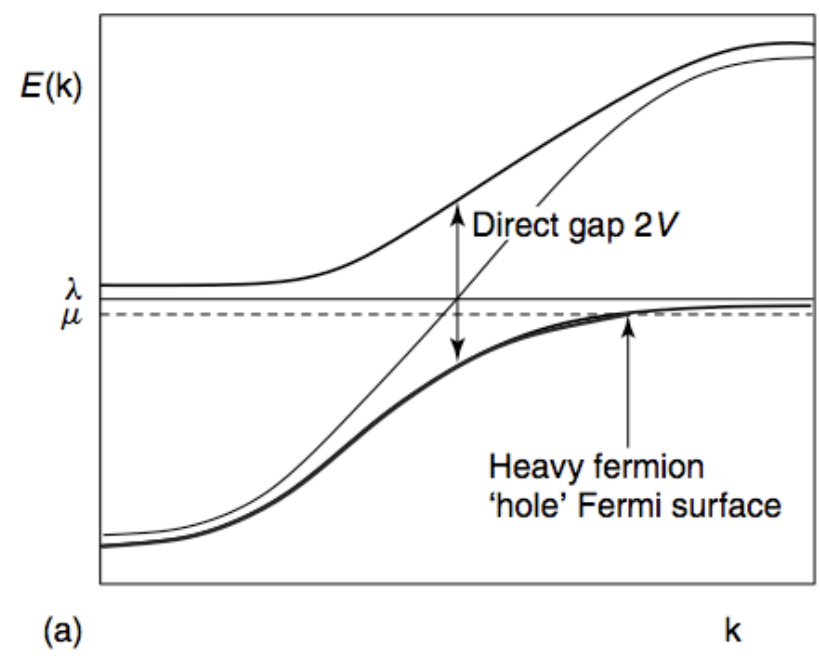
$$\begin{aligned} \frac{E_o}{N\mathcal{N}_s} &= -\frac{\rho}{2} \left(D + \frac{V^2}{D} \right)^2 + \frac{\Delta}{\pi} \int_{-D}^0 dE \left(\frac{1}{E - \lambda} + \frac{\lambda}{(E - \lambda)^2} \right) + \left(\frac{V^2}{J} - \lambda q \right) \\ &= -\frac{D^2 \rho}{2} + \frac{\Delta}{\pi} \ln \left(\frac{\lambda}{D} \right) + \left(\frac{V^2}{J} - \lambda q \right) \end{aligned}$$



Detailed calcn

$$\frac{E_F}{NN_s} - \frac{V^2}{2} \left(\frac{1}{D} + \frac{V^2}{D} \right)^2 + \frac{\Delta}{\pi} \int_{-D}^0 dE \left(\frac{1}{E - \lambda} + \frac{\lambda}{(E - \lambda)^2} \right) + \left(\frac{V^2}{J} - \lambda q \right)$$

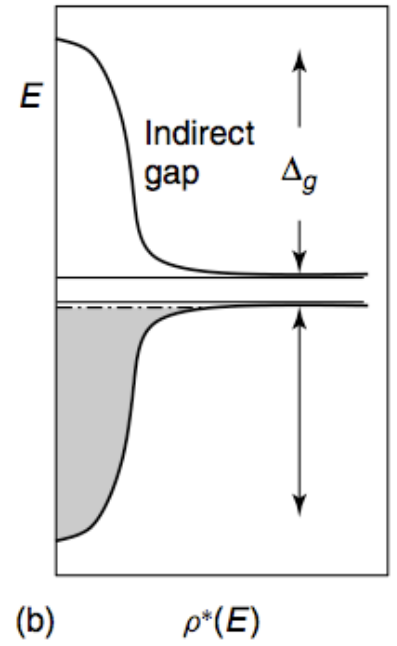
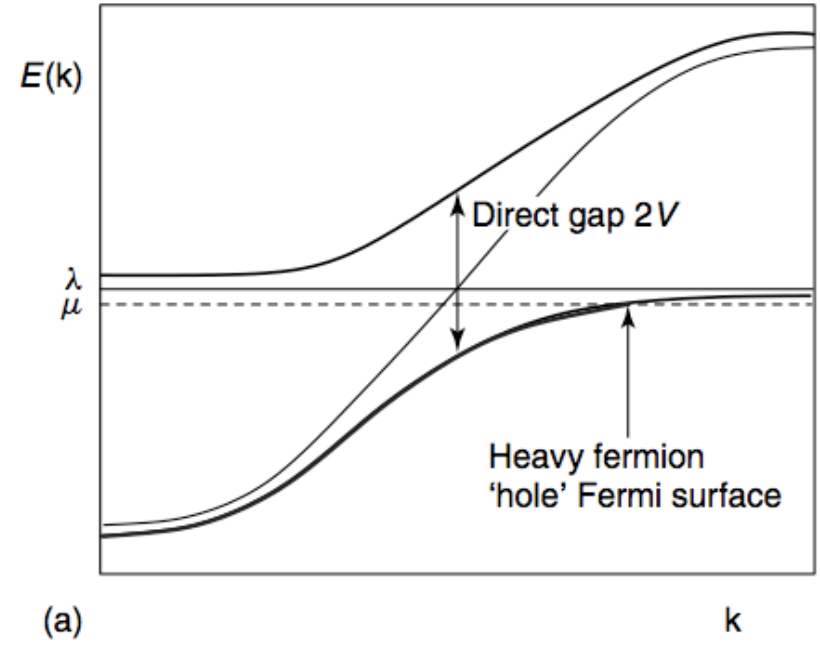
$$= -\frac{D^2 \rho}{2} + \frac{\Delta}{\pi} \ln \left(\frac{\lambda}{D} \right) + \left(\frac{V^2}{J} - \lambda q \right)$$



Detailed calcn.

$$(\Delta = \pi\rho|V|^2)$$

$$\frac{E_0}{N\mathcal{N}_s} = -\frac{D^2\rho}{2} + \frac{\Delta}{\pi} \ln\left(\frac{\lambda}{D}\right) + \left(\frac{\pi\rho V^2}{\pi\rho J} - \lambda q\right)$$

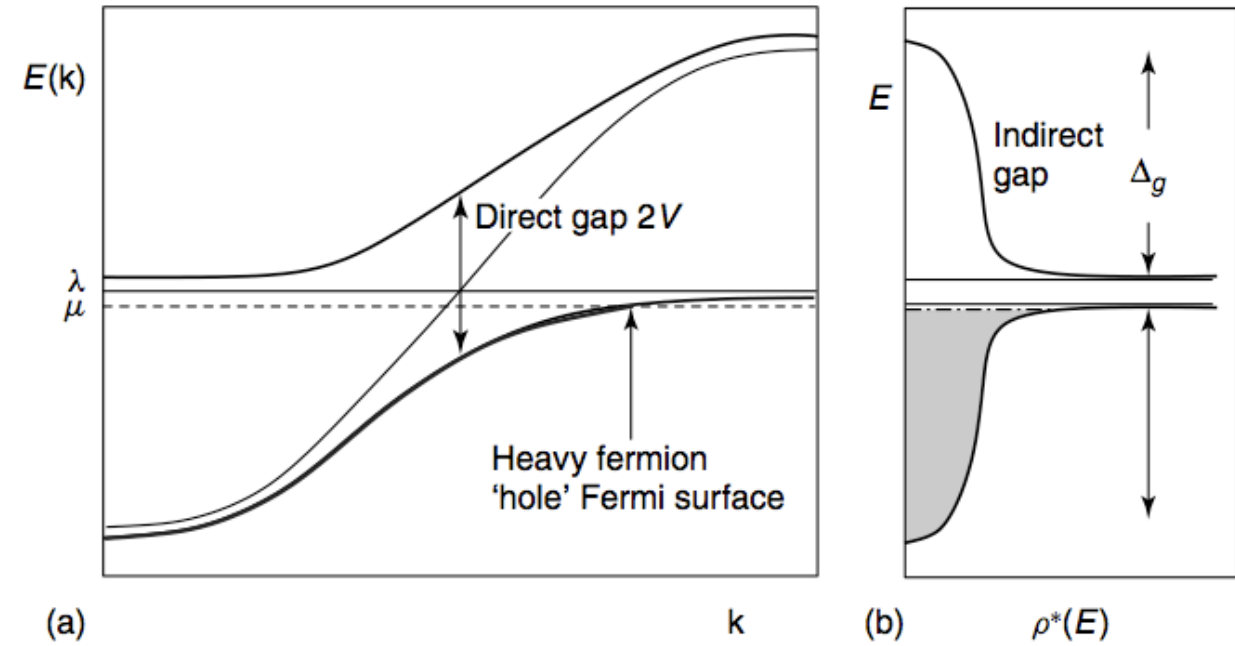


Detailed calcn.

$$(\Delta = \pi\rho|V|^2)$$

$$\begin{aligned} \frac{E_0}{N\mathcal{N}_s} &= -\frac{D^2\rho}{2} + \frac{\Delta}{\pi} \ln\left(\frac{\lambda}{D}\right) + \left(\frac{\pi\rho V^2}{\pi\rho J} - \lambda q\right) \\ &= -\frac{D^2\rho}{2} + \frac{\Delta}{\pi} \ln\left(\frac{\lambda}{D}\right) + \left(\frac{\Delta}{\pi\rho J} - \lambda q\right) \\ &= -\frac{D^2\rho}{2} + \frac{\Delta}{\pi} \ln\left(\frac{\lambda}{De^{-\frac{1}{J\rho}}}\right) - \lambda q \\ &= -\frac{D^2\rho}{2} + \frac{\Delta}{\pi} \ln\left(\frac{\lambda}{T_K}\right) - \lambda q. \end{aligned}$$

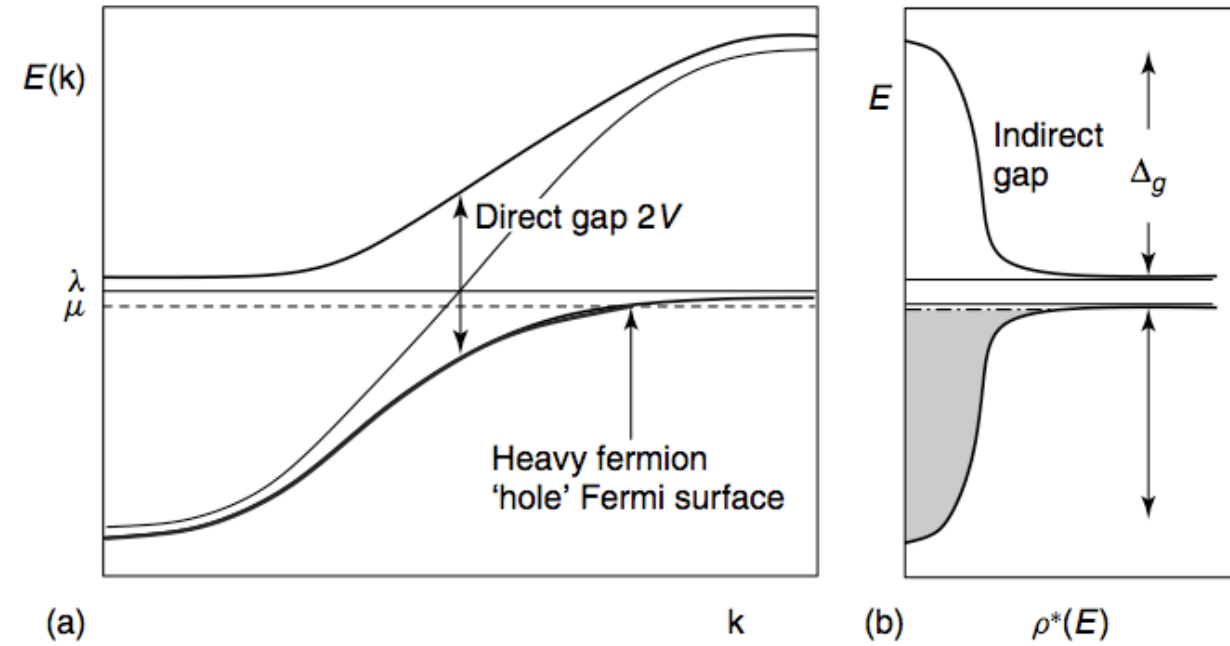
$$T_K = De^{-\frac{1}{J\rho}}$$



Detailed calcn.

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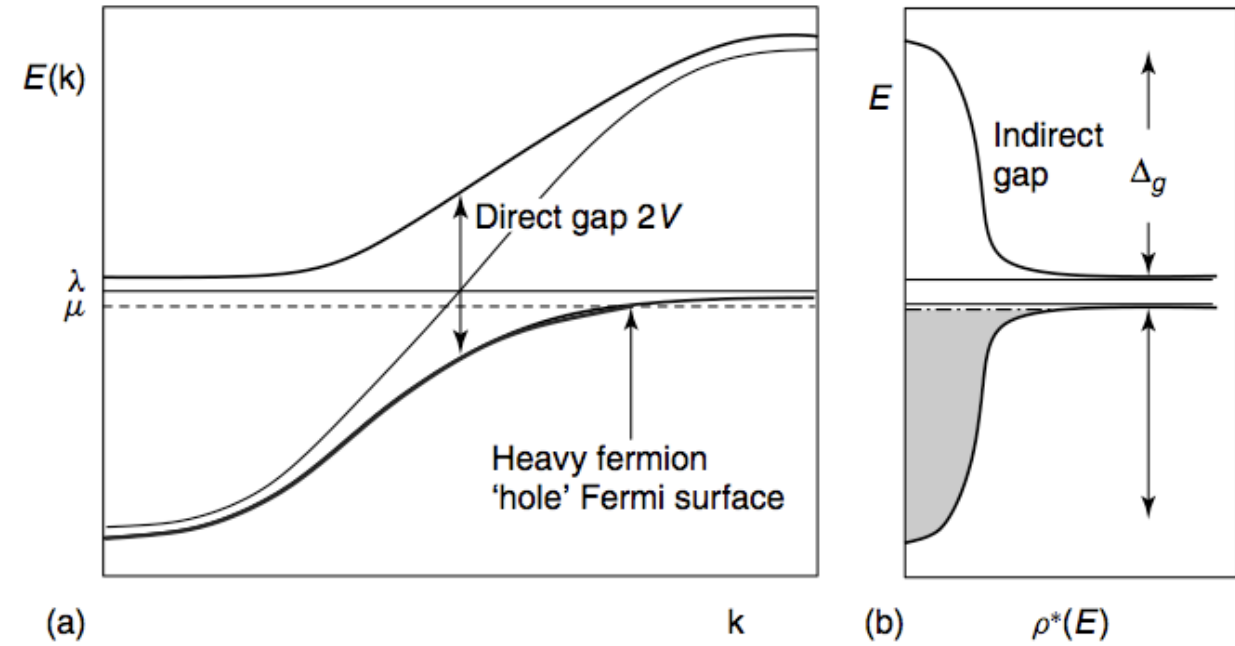
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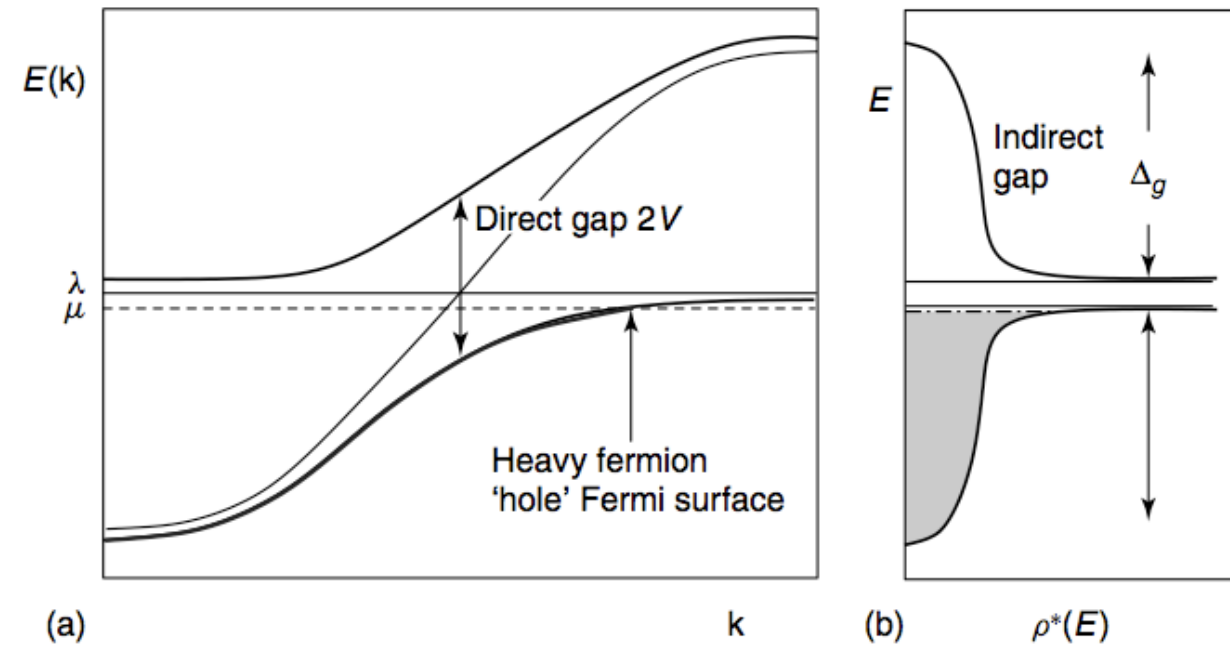
$$\frac{\partial E_0}{\partial \lambda} = \langle n_f \rangle - Q = 0 \quad \frac{\Delta}{\pi\lambda} - q = 0$$

$$\frac{E_o(V)}{N\mathcal{N}_s} = \frac{\Delta}{\pi} \ln\left(\frac{\Delta}{\pi q e T_K}\right) - \frac{D^2\rho}{2},$$

Detailed calcn.

$$(\Delta = \pi\rho|V|^2)$$

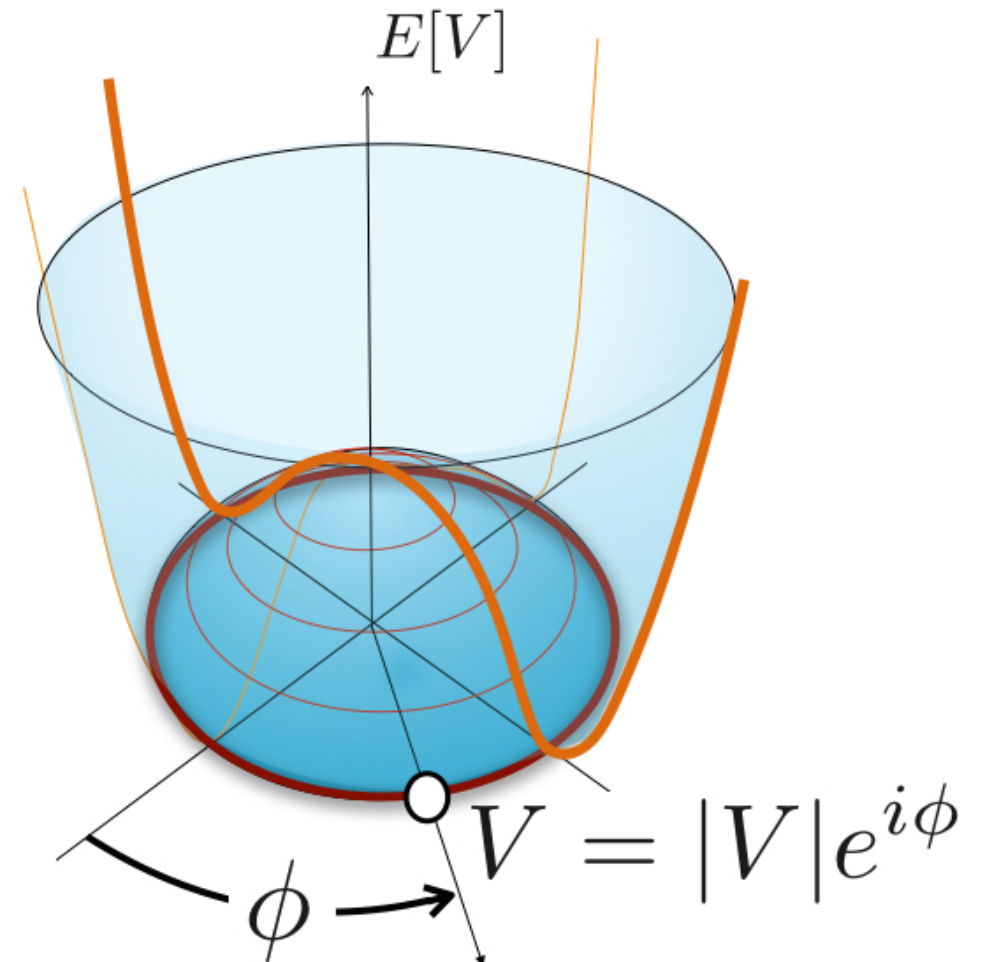
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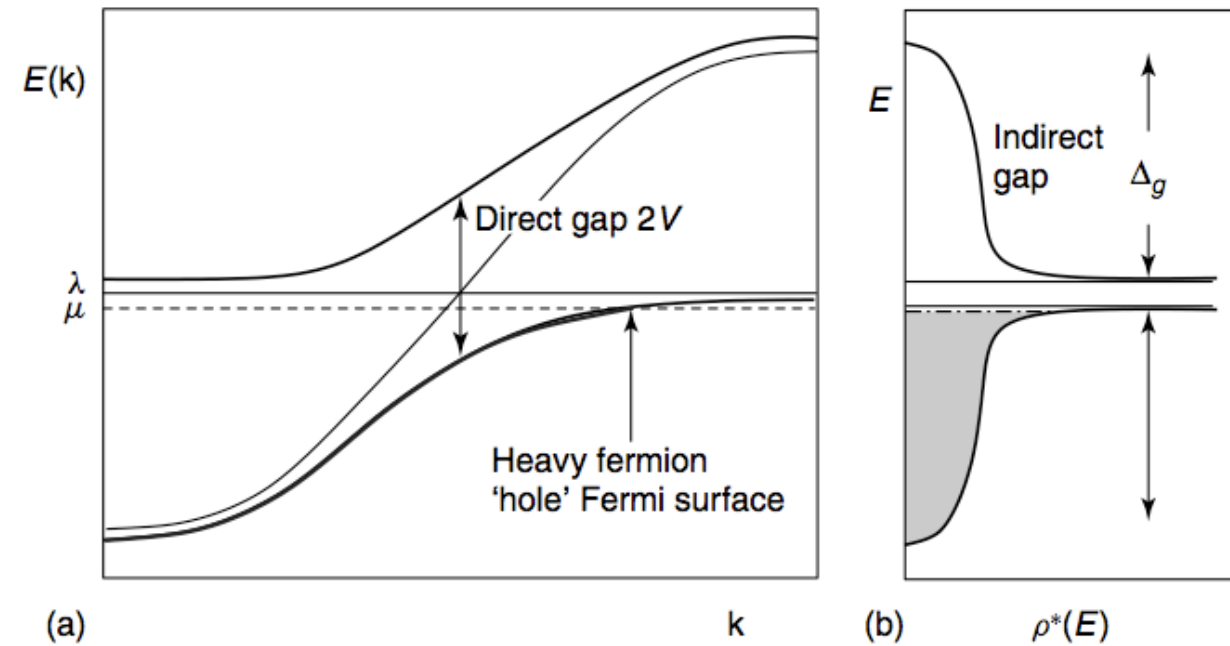
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Detailed calcn.

$$(\Delta = \pi\rho|V|^2)$$

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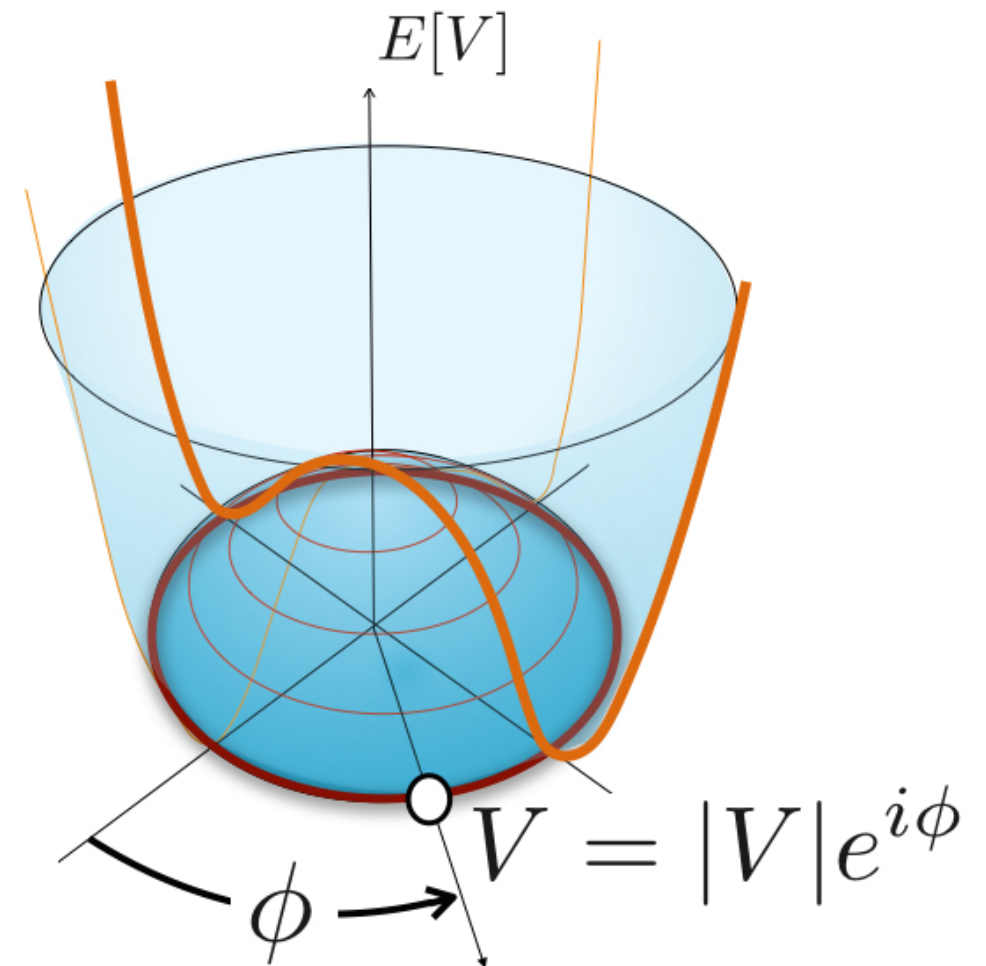
$$\frac{\partial E_0}{\partial \lambda} = \langle n_f \rangle - Q = 0 \quad T_K = De^{-\frac{1}{J\rho}}$$

$$\frac{\Delta}{\pi\lambda} - q = 0$$

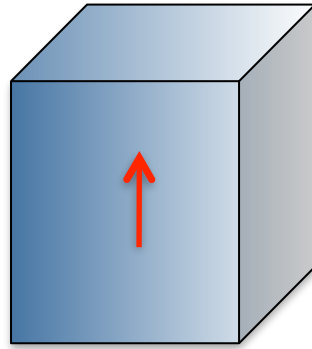
$$\frac{E_o(V)}{N\mathcal{N}_s} = \frac{\Delta}{\pi} \ln\left(\frac{\Delta}{\pi q e T_K}\right) - \frac{D^2\rho}{2},$$

$$\frac{\partial E_0}{\partial \Delta} = 0 \quad 0 = \frac{1}{\pi} \ln\left(\frac{\Delta e^2}{\pi q T_K}\right)$$

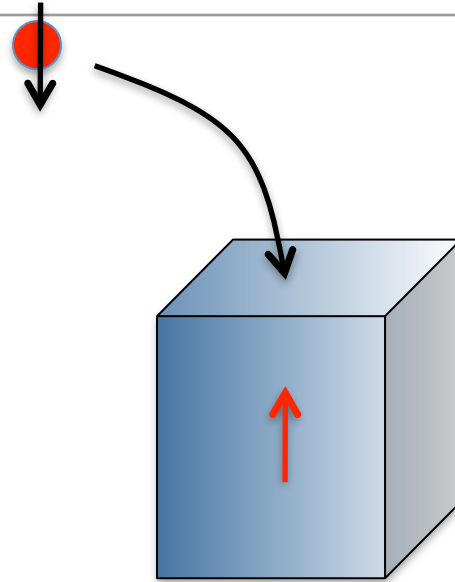
$$\Delta = \frac{\pi q}{e^2} T_K$$



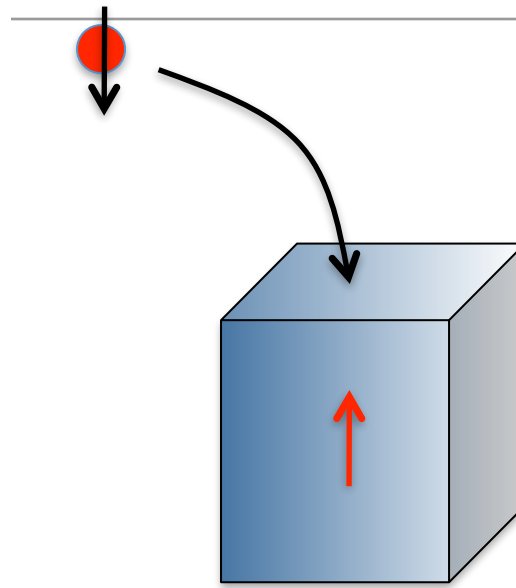
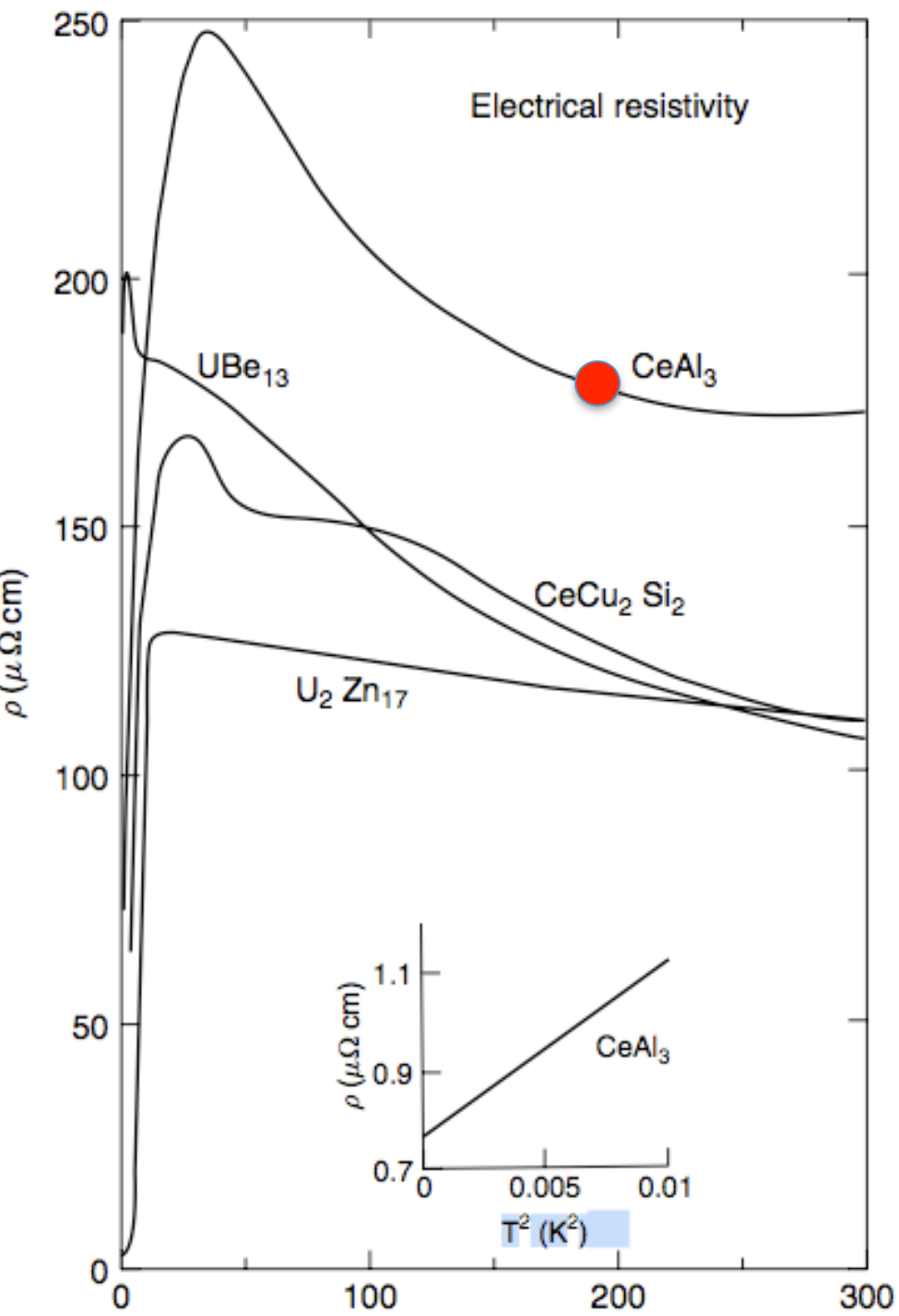
Coherence and composite fermions



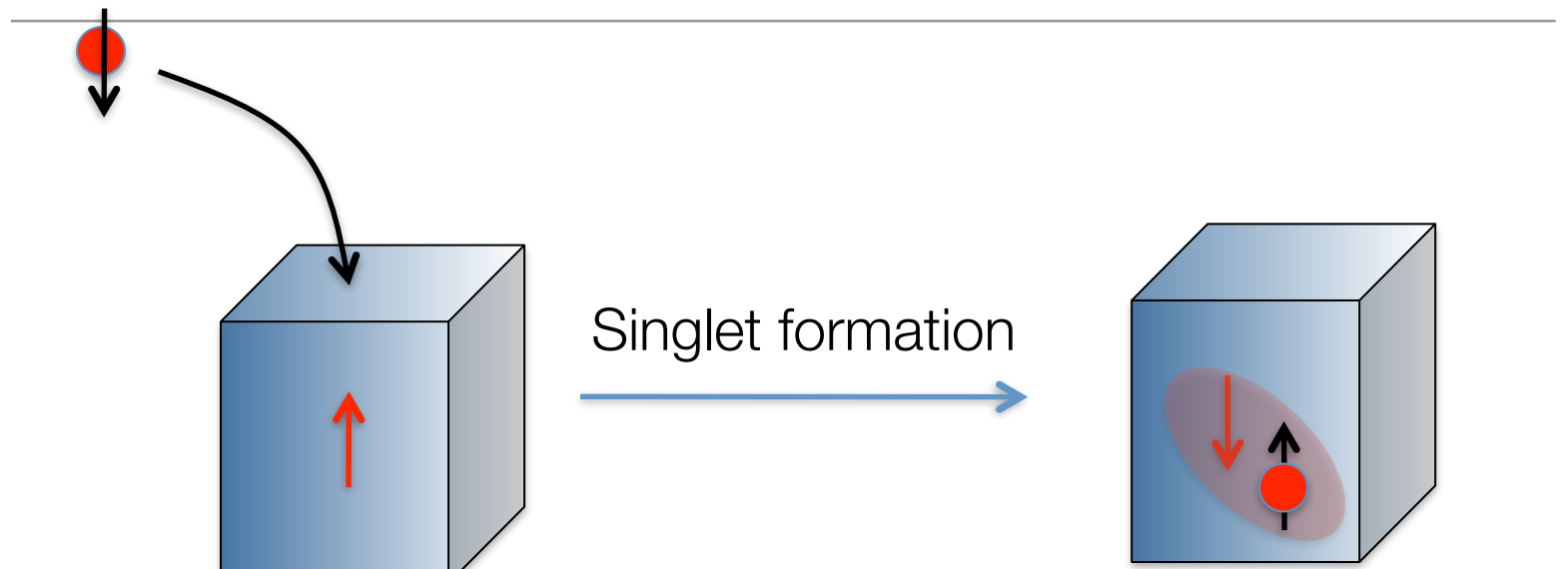
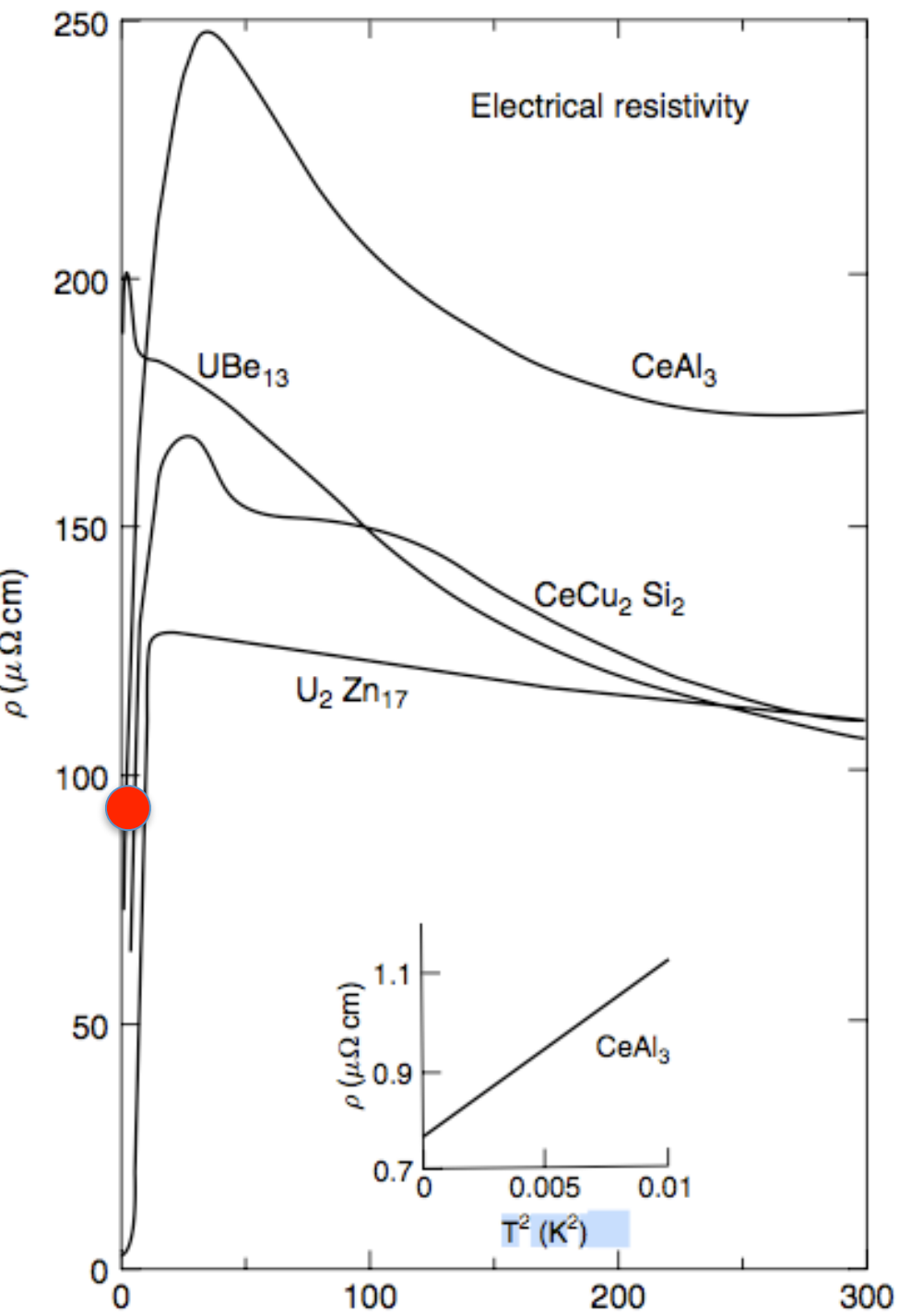
Coherence and composite fermions



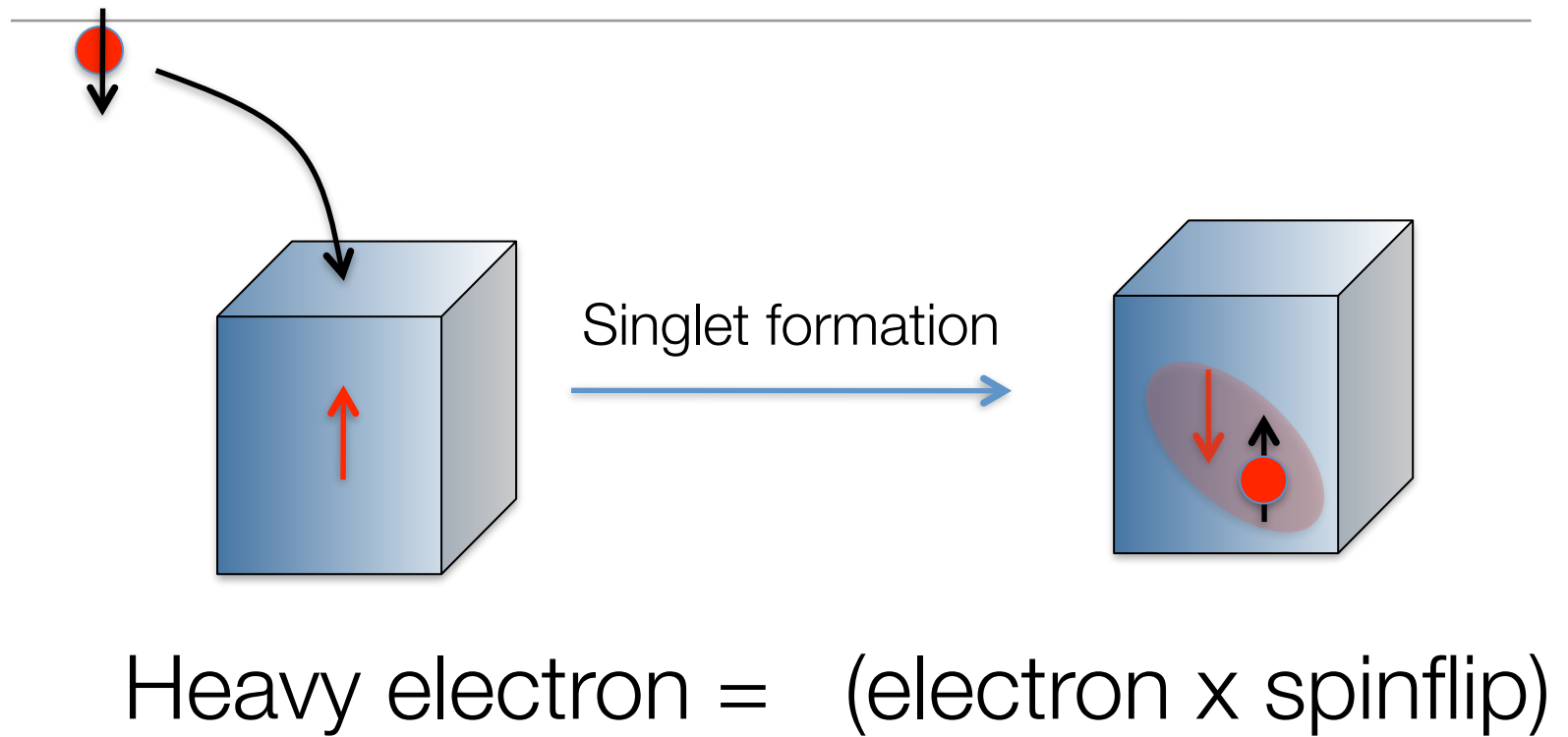
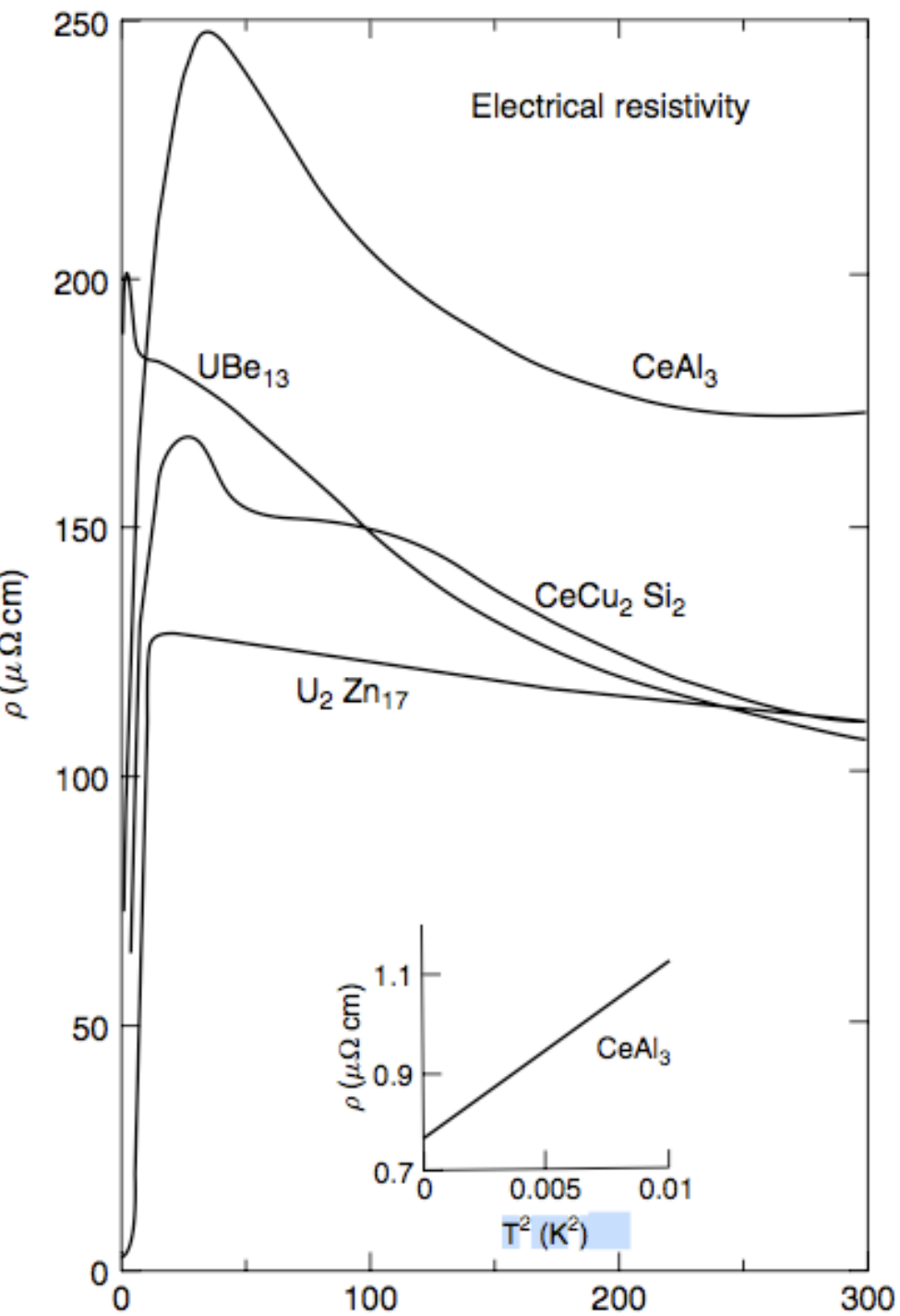
Coherence and composite fermions



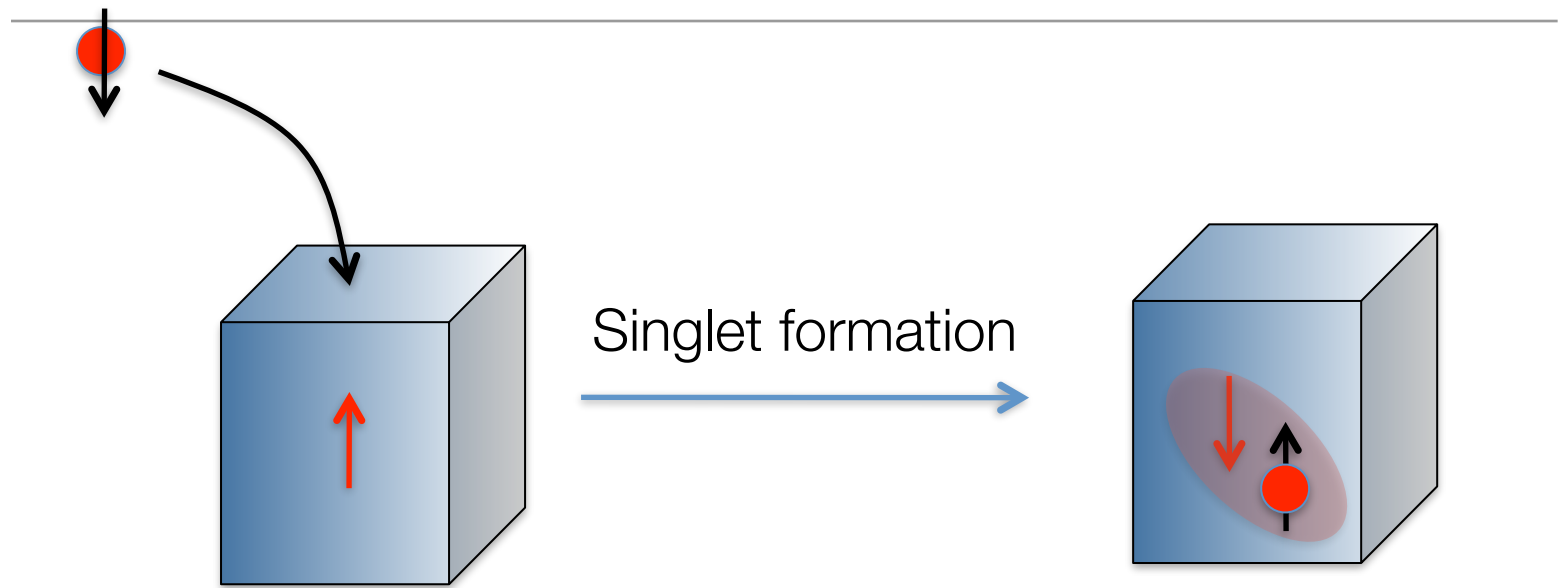
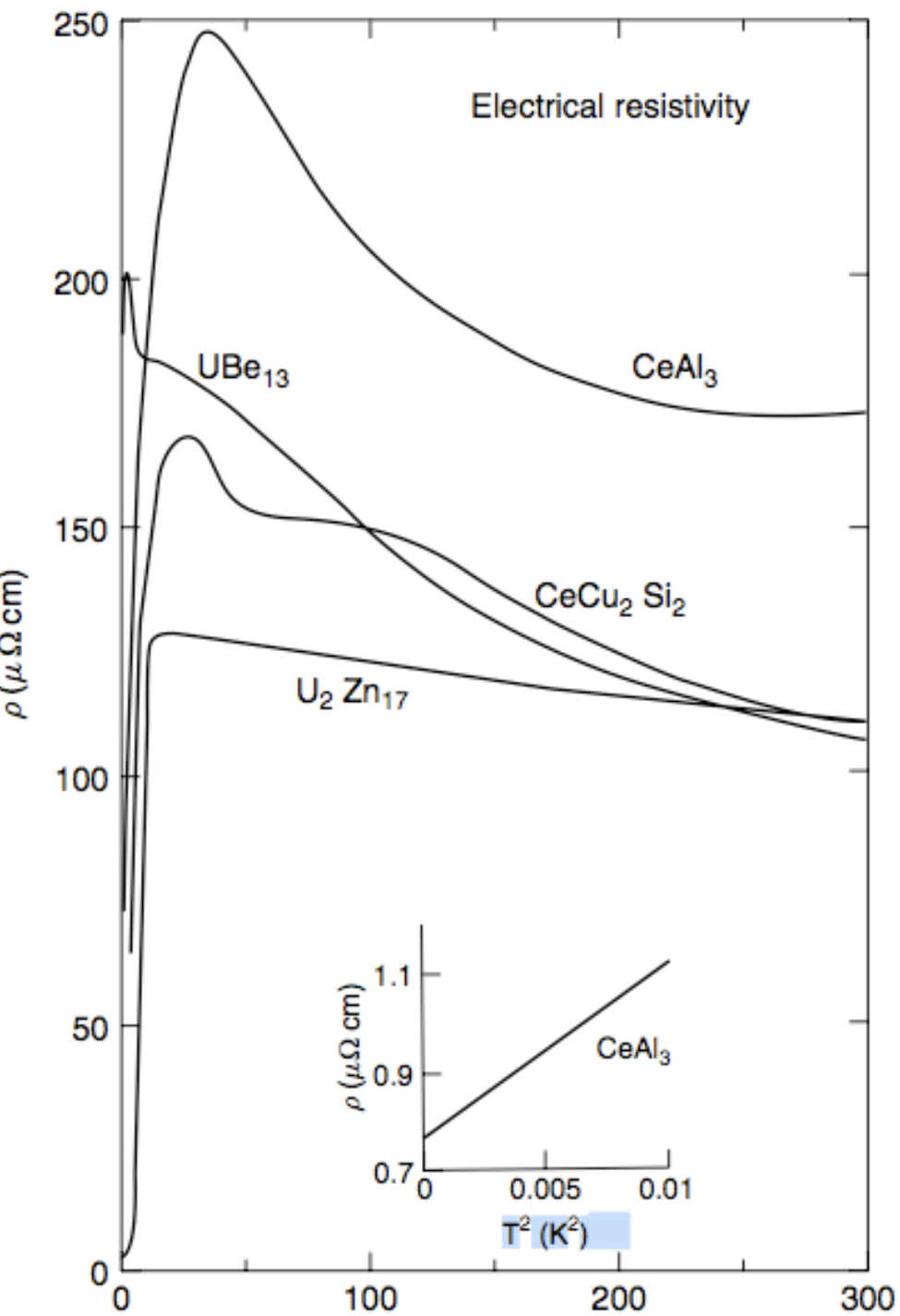
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Coherence and composite fermions



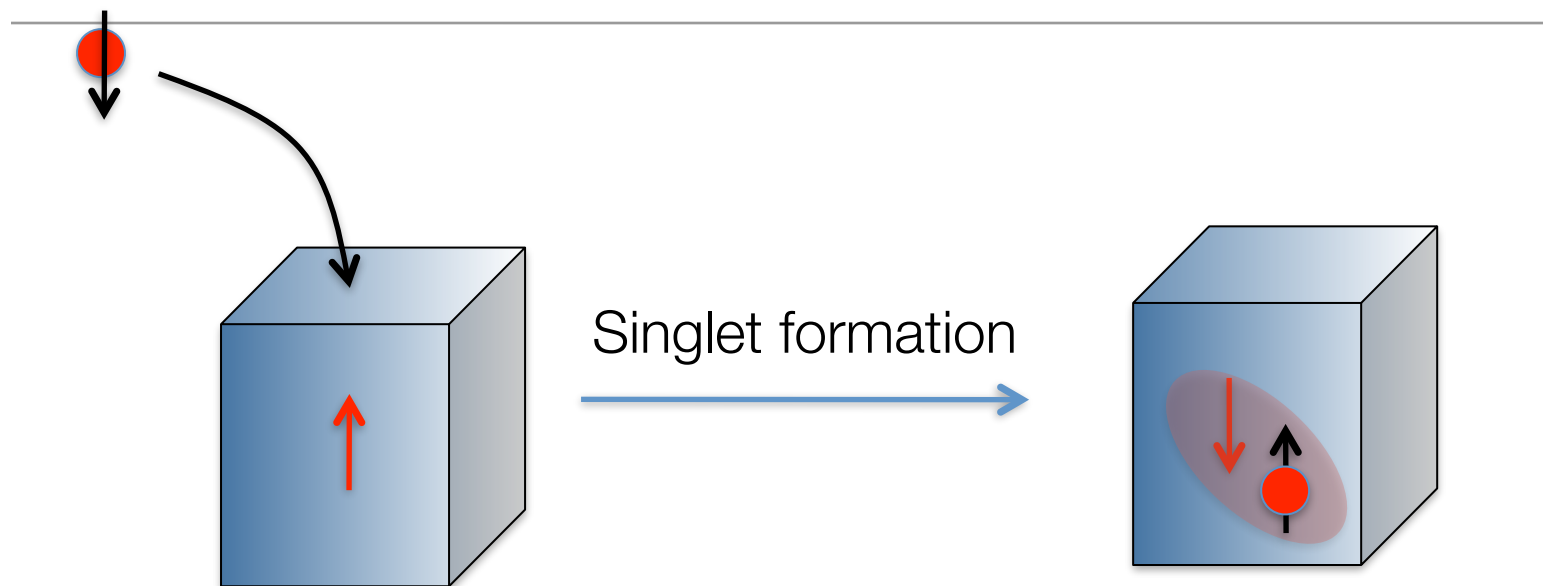
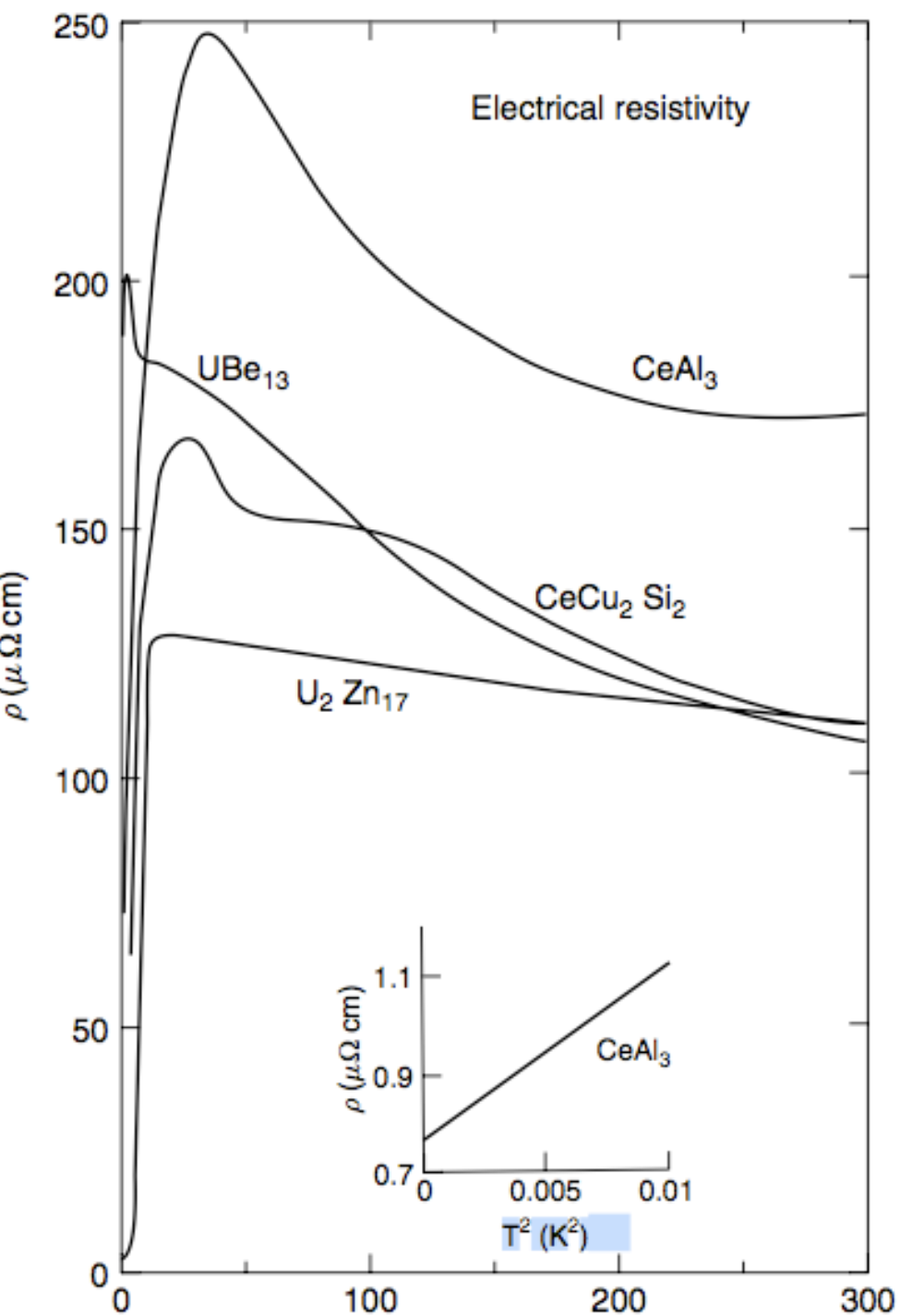
Coherence and composite fermions



Heavy electron = (electron x spinflip)

- The large N approach to the Kondo lattice.
Spin x conduction = composite fermion

Coherence and composite fermions

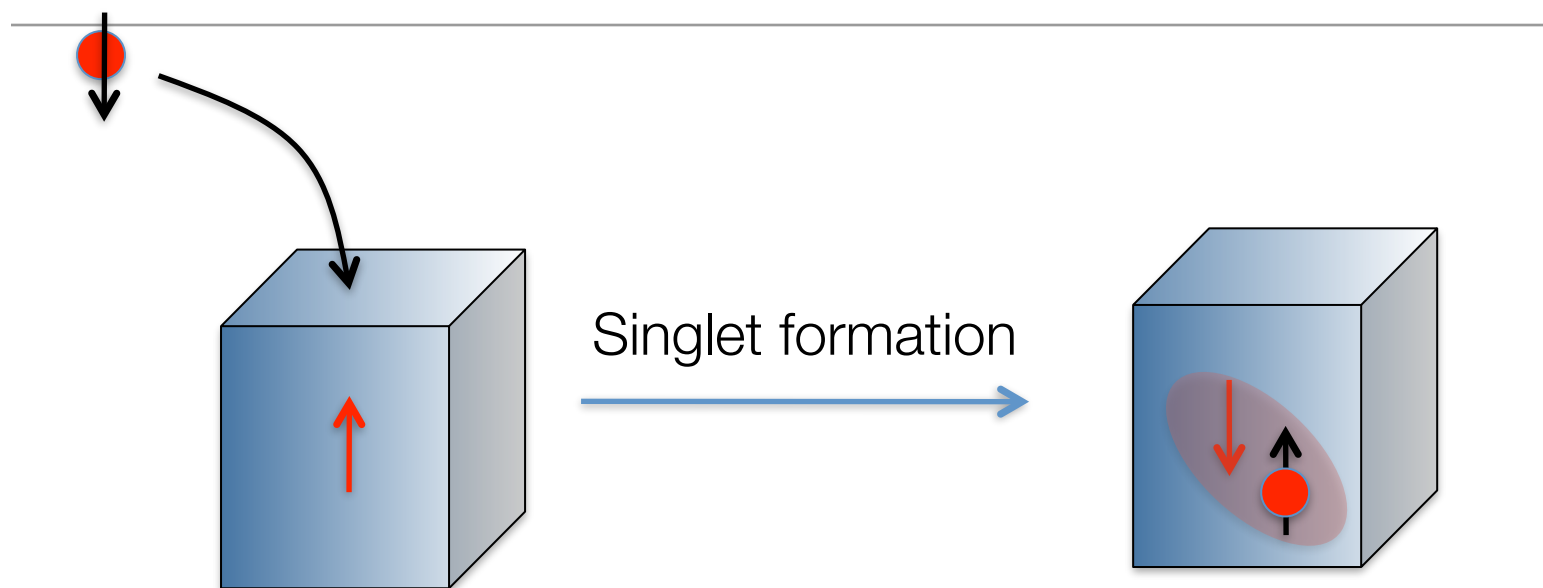
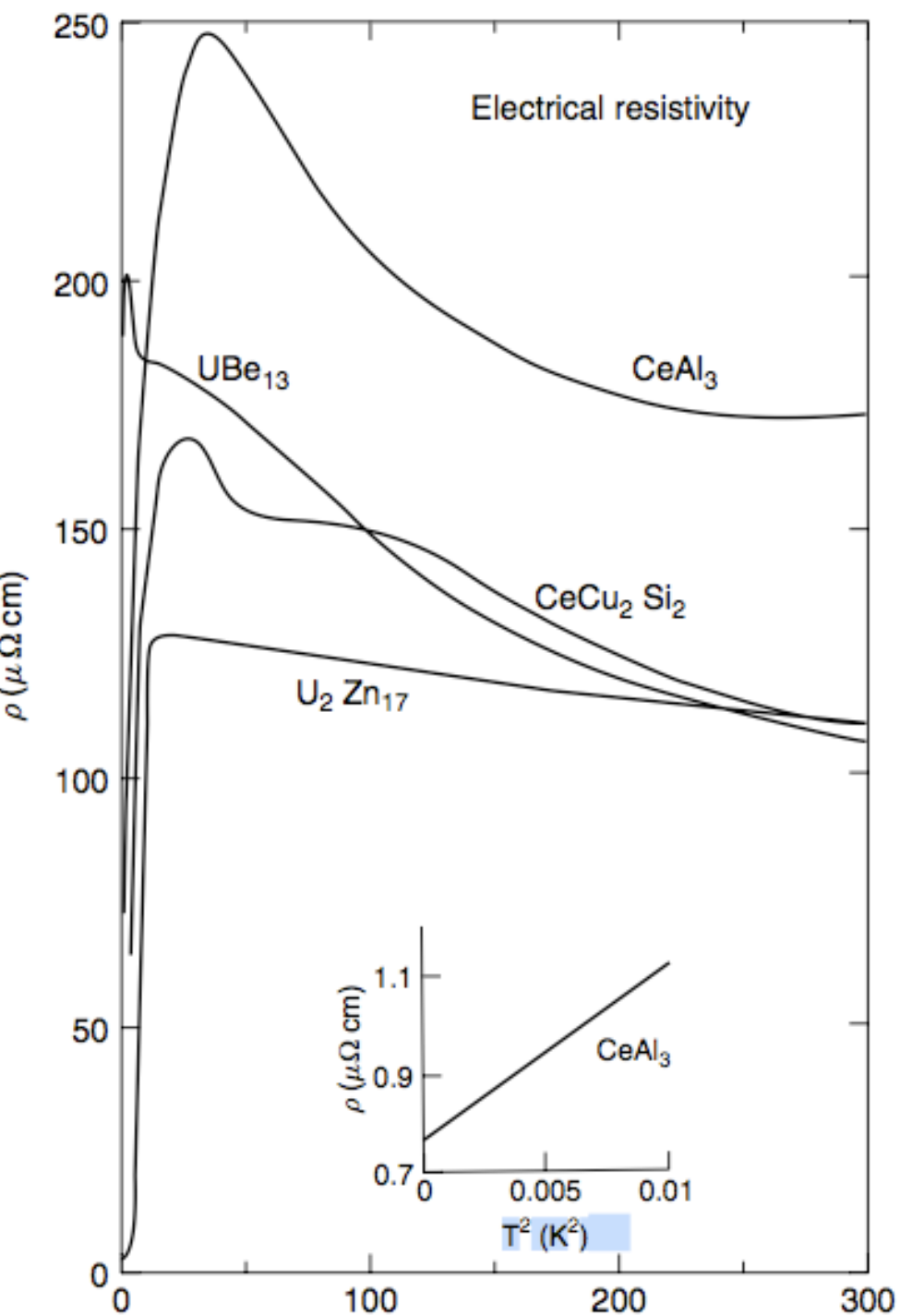


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$$\frac{J}{N} c^\dagger_\beta S_{\alpha\beta} c_\alpha \rightarrow \bar{V} (c^\dagger_\alpha f_\alpha) + (f^\dagger_\alpha c_\alpha) V + N \frac{\bar{V}V}{J},$$

Coherence and composite fermions



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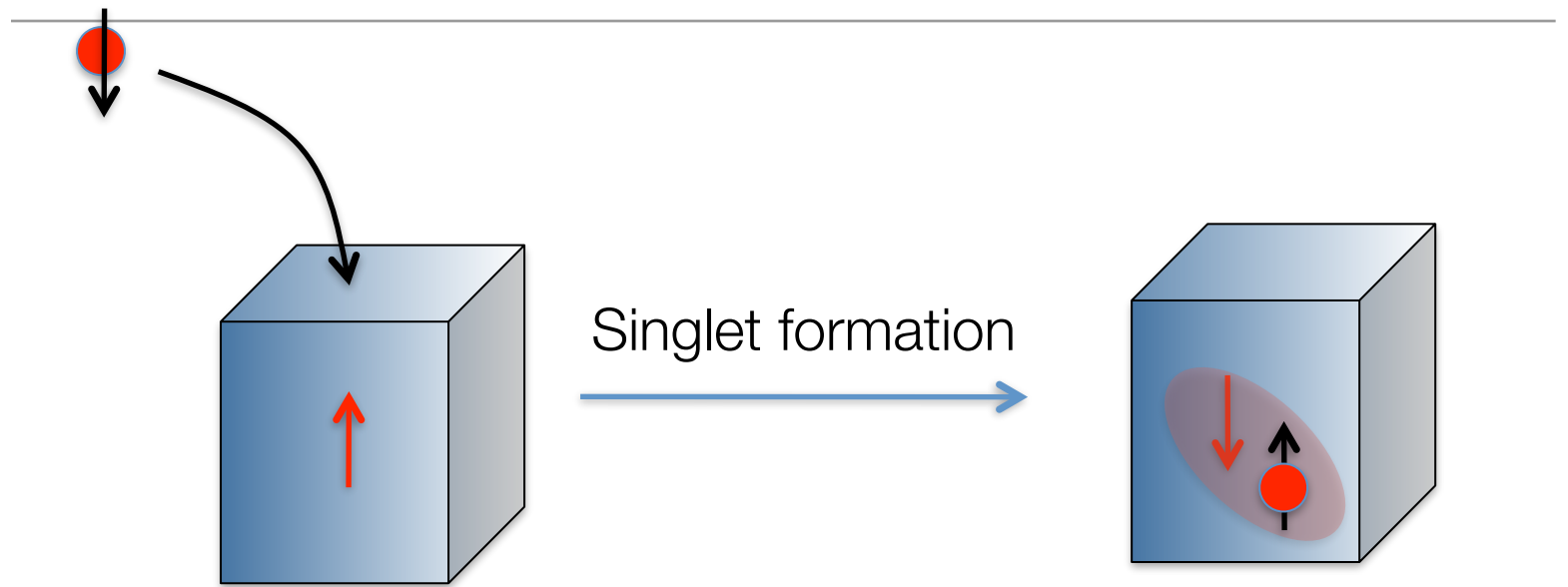
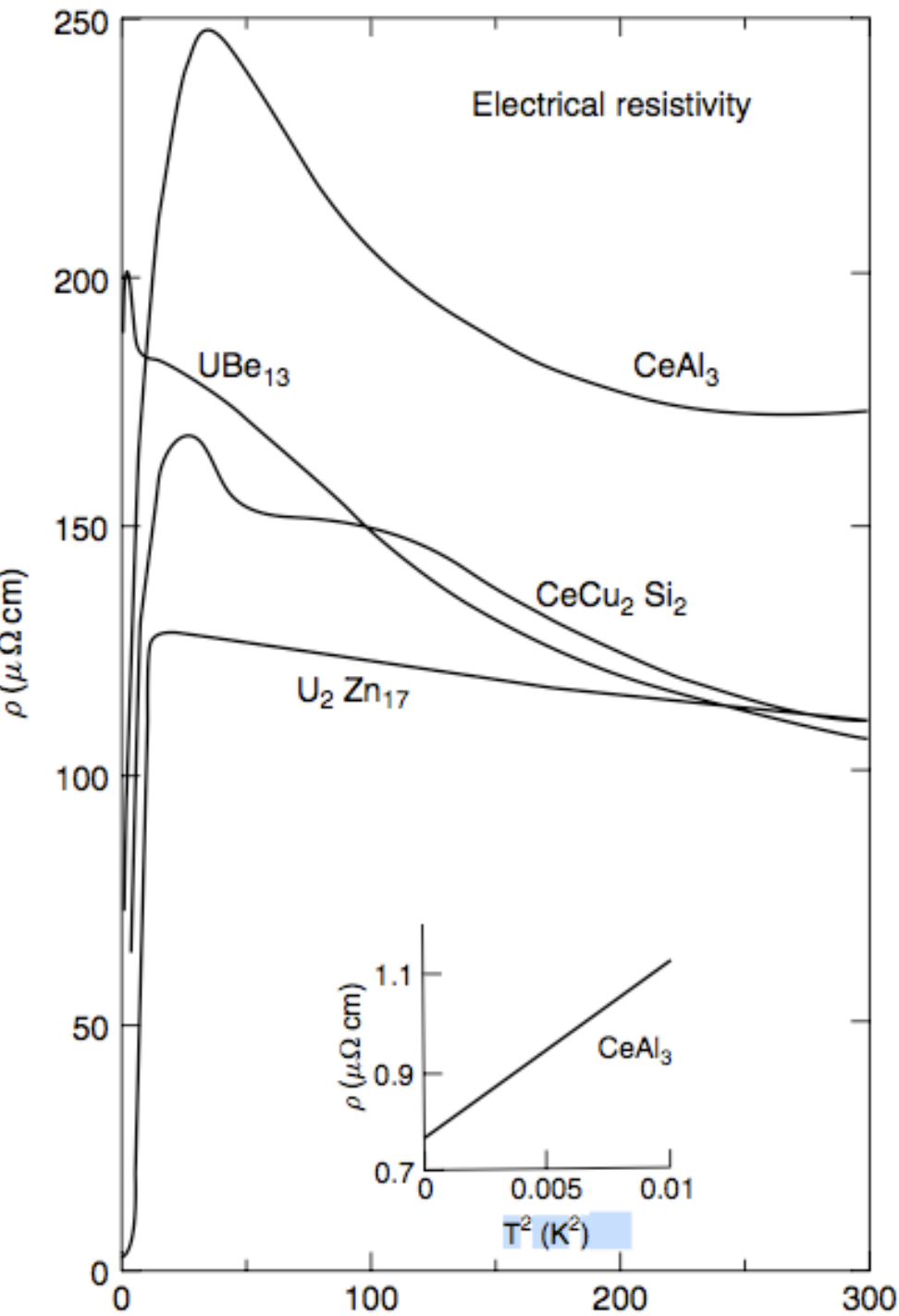
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Composite Fermion

$$\frac{J}{N} c_{j\alpha}^{\dagger} S_{\alpha\beta} \equiv \bar{V} f_{j\beta}^{\dagger}$$

Coherence and composite fermions



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