

# Exotic Phase Diagram of Multilayered Triangular Ising Model

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I will introduce the thermodynamic phase diagram of a multilayered triangular lattice Ising model (MLTIM) with a finite number  $N$  of vertically stacked layers. We will see that above a critical  $N$  there is a low temperature reentrance of one or two Berezinskii-Kosterlitz-Thouless (BKT) transitions, which results in an extended pseudo-critical disordered regime ( $\langle \sigma_{i,n} \sigma_{i+r,n} \rangle \sim r^{-\eta(T)} e^{-r/\xi}$ ) down to zero temperature. This low-temperature disordered regime has peculiar properties such as a negative value of  $d\eta/dT$  (short-range spin-spin correlations increase with temperature). I will explain these results by analyzing the RG flow of a low energy effective dimer theory that quantitatively describes the low temperature physics of the MLTIM. I will also derive qualitative features of the global phase diagram by mapping the classical spin model into the single-layer quantum Ising model.

In the 3D limit ( $N \rightarrow \infty$ ), the two upper BKT transitions collapse into a single 3D-XY critical point that signals the transition into a partially disordered antiferromagnetic state that breaks a  $Z_2 \times Z_3$  symmetry. This transition and the normal to superfluid transition of a neutral system, like  $^4\text{He}$ , are in the same universality class. Onsager and Feynman envisioned long time ago that the superfluid to normal transition can be understood as a proliferation of  $U(1)$  vortex loops. We will see that the proliferation of  $Z_6$  vortex loops that has been recently observed in  $\text{RMnO}_3$  compounds is a direct manifestation of this phenomenon in systems that have lower symmetry ( $Z_6$ ).

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