

### Solution for Problem C3

- a) (3 points) The  $\bar{p}$  is composed of three antiquarks chosen from  $\bar{u}$  (charge  $-2/3$ ) and  $\bar{d}$  (charge  $1/3$ ). The  $\bar{p}$  has charge  $-1$ , and so can be only  $\bar{u}\bar{u}\bar{d}$ . The  $\Sigma^+$  has an  $s$  quark (charge  $-1/3$ ) and charge  $+1$ , so the other two quarks must be  $u$ 's (with charge  $2/3$ ). The  $\Sigma^+$  is  $suu$ . The  $\rho^-$  is composed of a quark and antiquark, and has charge  $-1$ . It must be  $\bar{u}d$ .
- b) (4 points) The  $\pi$  and  $\rho$  mesons are low mass states, so their orbital angular momenta must be  $S$  wave (primarily). Given their spins, the quarks in the  $\pi$  meson are in a  $^1S_0$  state, and the quarks in the  $\rho$  meson are in a  $^3S_1$  state.
- c) (3 points) The members of an isospin multiplet differ only by the substitution of  $u$  for  $d$  quarks, and *vice versa*. An isospin 1 multiplet can be constructed only if there are two such quarks. The third quark is the  $c$  quark. Given that the  $c$  has charge  $2/3$ , the members of the isotriplet have charge 2 ( $cuu$ ), 1 ( $cud$ ) and 0 ( $cdd$ ).