Geometric Optics

Objective: To see how light waves interfere constructively and destructively. To observe interference and diffraction. To measure small apertures or objects from their diffraction patterns.

Apparatus: Laser, slides (single-slit, double-slit, diffraction grating), slide holder clip and stand assembly, small projection screen with white paper, meter stick

Introduction

You may have learned from lecture that light has wave properties, and that two light waves of the same frequency can add up constructively (bright areas) or destructively (dark areas) depending on the path difference (the difference in distance from each light wave to the point where they meet) or their phase (the point in the wave cycle at a particular point in time – for instance, a wave described by the sine function leads a wave by the cosine by 90 degrees).

Waves add up either when the original light wave is split up into two constituent waves (double slit interference) or when the same portions of the original light wave interfere with themselves (single slit or grating diffraction). The equations describing the position of the bright or dark sports on light coming out of a slit or grating projected upon a screen far away are summarized as follows:
Single Slit

\[ b \sin \theta = m \lambda \quad ; m = 1,2,3,... \]

Here \( b \) is the width of the single slit, \( \theta \) is the angular deflection (as measured from the central maxima, at which the path difference is zero and there is maximum addition of the two waves) of the dark areas (minima) on a screen far away. \( \lambda \) is the wavelength of the incoming light and \( m \) is the order of the minima – the higher order minima are farther from the central maxima; positive minima are to the right of the central maxima, while negative minima are to the left of the central maxima. See the diagram below:
Double Slit

\[ d \sin \theta = n \lambda \quad ; \quad m = 0, 1, 2, 3, \ldots \]

Here \( d \) is the distance between the slits, \( \theta \) is the angular deflection of the bright areas (maxima) on a screen far away. \( \lambda \) is the wavelength of the incoming light and \( m \) is the order of the minima. See the diagram below.

Note that the above diagram shows an idealized double slit, which ignores the single slit character of each of the two single slits. A true double slit would exhibit closely spaced dark and light areas (fringes), superimposed over the single slit pattern. The single slit profile is said to modulate the double slit pattern, as shown below:
The equation here is the same for the double slit case, except that $d$ represents number of grating lines per unit distance. The situation is very similar to the double slit because there are many lines interfering constructively; the resulting diffraction pattern is
therefore very sharp.

Clockwise from top left - Single Slit, Double Slit, Diffraction Grating

### SLIDE SPECIFICATIONS

**Single Slit slide:**

<table>
<thead>
<tr>
<th>PATTERN</th>
<th>A</th>
<th>B</th>
<th>C</th>
<th>D</th>
</tr>
</thead>
<tbody>
<tr>
<td>NO. SLITS</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
</tr>
<tr>
<td>SLIT WIDTH</td>
<td>.02 mm</td>
<td>.04 mm</td>
<td>.08 mm</td>
<td>.16 mm</td>
</tr>
</tbody>
</table>

**Double Slit slide:**

<table>
<thead>
<tr>
<th>PATTERN</th>
<th>A</th>
<th>B</th>
<th>C</th>
<th>D</th>
</tr>
</thead>
<tbody>
<tr>
<td>NO. SLITS</td>
<td>2</td>
<td>2</td>
<td>2</td>
<td>2</td>
</tr>
<tr>
<td>SLIT WIDTH</td>
<td>.04 mm</td>
<td>.04 mm</td>
<td>.08 mm</td>
<td>.08 mm</td>
</tr>
<tr>
<td>SLIT SPACE</td>
<td>.250 mm</td>
<td>.500 mm</td>
<td>.250 mm</td>
<td>.500 mm</td>
</tr>
</tbody>
</table>

**Diffraction Gratings:**

80, 100, 300, and 600 lines/mm. Calculate d, the line spacing for each in nanometer units.
Activities

You will use a human hair (which one lab partner will provide) and three slides (single slit, double slit, diffraction grating) to investigate interference and diffraction. Measuring the distance from the slide to the screen and the distance from the central maxima to the maxima or minima in question will give you the angle with some calculation; remember that you can utilize small angle approximations only if the distance from the slide to the screen is large compared to the distance from the minima/maxima to the central maxima.

A. Measure the thickness of a human hair

Devise an experiment to measure the thickness of a human hair. You or your one of your lab partners will have to provide the hair. Explain how your experiment will measure the thickness and show all your calculations.

B. Single Slit

Devise an experiment to measure the wavelength of the laser light using a single slit. **Use at least two single slits of different widths and average your results.** Note that in the equation, the only unknown variable is $\lambda$ while the other variables are known or measurable. Remember that the equation gives the positions of the minima.

C. Double Slit

Devise an experiment to measure the wavelength of the laser light using a double slit. **Use at least two double slits of different spacings and average your results.** Note that in the equation, the only unknown variable is $\lambda$ while the other variables are known or measurable. Remember that the equation gives the positions of the maxima and that you should measure the distances between the small dark areas inside the single slit envelope, not the large-spaced distances between the single slit envelope minima.

D. Diffraction Grating

Devise an experiment to measure the wavelength of the laser light using a diffraction grating. **Use at least two diffraction gratings of different spacings and average your results.** Note that in the equation, the only unknown variable is $\lambda$ while the other variables are known or measurable. Remember that the equation gives the positions of the maxima.