

Physics 613 Homework #5  
Due March 3, 2014 at 4:00 EST

**1:** Consider the ABC theory with  $m_A = m_B = m_C = m > 0$ . Give the lowest order nonvanishing contribution to the scattering amplitude  $A + B \rightarrow A + A + C$ . Call the initial momenta  $k_A$  and  $k_B$  and the final momenta  $p_A$  and  $p'_A$  and  $p_C$ .

Hints: The time ordering does not affect the contractions with the external creation and annihilation operators, and just places time orderings on the contractions of  $\hat{\phi}$ 's with each other, to convert them into Feynman propagators. The permutations of  $n$  space-time points from the  $n$ 'th order in the expansion of the exponential cancels the  $1/n!$  if you have a unique way of settling which point is which (*e.g.* setting which  $x_j$  contracts with which external momentum). Furthermore, the final answer must be symmetric under  $p_A \leftrightarrow p'_A$ , but this may be implemented by writing down half the amplitude and adding “ $+(p_A \leftrightarrow p'_A)$ ”.