Studying the Proton "Radius" Puzzle with $\mu p$ Scattering

1) Exciting Physics

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The Proton “Radius” Puzzle

Muonic hydrogen disagrees with ep atomic physics and scattering determinations of the slope of FF at $Q^2 = 0$. The difference (#5 vs #6) is 7σ. This is a high-profile issue – Nature paper, APS plenary & many invited talks, PSAS2012 Symposium, Trento ECT* Workshop Nov 2012

What could explain the difference?

<table>
<thead>
<tr>
<th>#</th>
<th>Extraction</th>
<th>$&lt;r_E&gt;^2$ (fm)</th>
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<tbody>
<tr>
<td>1</td>
<td>Sick</td>
<td>0.895±0.018</td>
</tr>
<tr>
<td>2</td>
<td>Bernauer Mainz</td>
<td>0.879±0.008</td>
</tr>
<tr>
<td>3</td>
<td>Zhan JLab</td>
<td>0.870±0.010</td>
</tr>
<tr>
<td>4</td>
<td>CODATA</td>
<td>0.877±0.007</td>
</tr>
<tr>
<td>5</td>
<td>Combined 2-4</td>
<td>0.876±0.005</td>
</tr>
<tr>
<td>6</td>
<td>Muonic Hydrogen</td>
<td>0.842±0.001</td>
</tr>
</tbody>
</table>

``Radius” (fm)
Possible Resolutions to the Puzzle / Critiques

The $\mu p$ result is wrong. No doubts about the experiment, but some discussion about the theory and proton structure for extracting the proton radius.

The $ep$ (scattering) results are wrong. The fit procedures are not good enough. Perhaps the data do not go to low enough $Q^2$, and there are structures in the form factors.

Proton structure issues in theory. Theory critique of theory - off-shell proton in two-photon exchange leads to enhanced effects differing between $\mu$ and $e$, or leads to theoretically unjustified sticking-in-form-factor models.

Novel beyond-Standard-Model Physics differentiates $\mu$ and $e$. But constraints on novel physics exist, and there seems to be no generally accepted solution at present.
PSI Muonic Hydrogen Measurements

R. Pohl et al., Nature 466, 09259 (2010): 2S\rightarrow 2P Lamb shift
\[ \Delta E \text{ (meV)} = 209.9779(49) - 5.2262 \, r_p^2 + 0.0347 \, r_p^3 \]
\( r_p = 0.842 \pm 0.001. \)

Possible issues: atomic theory & proton structure

Wednesday, February 22, 2012
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Possible issues: atomic theory & proton structure

Proton structure: De Rujula suggested \( r_p^3 \) could be anomalously large. Miller & Cloet and Distler, Bernauer & Walcher showed that this is inconsistent with modern form factor fits. Wu & Kao showed if you add narrow peaks in unmeasured low-\(Q^2\) regions you can get different results. There is no reason at present to believe such structures exist – and we would also expect them to affect the ep atom and scattering determinations of the radii.
Examples of Atomic Physics Calculations

Carlson & Vanderhaeghen (2011): box diagram corrections essentially agree with Pachucki and with Martynenko, although individual terms within the evaluation vary.

Hill & Paz (2011): Elastic contribution of C&V and others from SIFF model. Real part of inelastic not under good theoretical control and have nonphysical limiting behaviors in existing models. Numerical values given not all that different from others.

The SIFF criticism has also been made by Miller, Thomas, Carroll, & Rafelski, who point out that it has been made for many years.

But the issue remains under dispute.
Cross sections $\rightarrow$ corrections form factors $\rightarrow$ fits radius

Figures from J. Bernauer’s Ph.D. thesis.

0.5% absolute uncertainty proposed, few % achieved, data normalized to $G_E = 1$ at $Q^2 = 0$. 

Simulate radiation

Simulate background

Fit cross sections directly
Mainz A1 Data

From J. Bernauer's Ph.D. thesis: spline fits tend to give \( r \approx 0.875 \text{ fm} \), vs polynomial fits with \( r \approx 0.883 \text{ fm} \). Uncertainties are statistics + linearly added systematics.

Reported \( r \) is an average of these, with statistical, systematic, and model uncertainties.
Mainz A1 Data

\[ G_E(Q^2) = 1 - Q^2 r^2 / 6 + \ldots \]

- Low \( Q^2 \) Mainz data: left - raw data, right - rebinned \( G_E \)
- Conclusion: in principle, the differences between \( r = 0.84 \) and \( 0.88 \) fm are large, but a precise experiment is needed, similar to Mainz, rather than a lower precision one aimed at only at distinguishing \( r = 0.84 \) fm from \( r = 0.88 \) fm.
In the 1970s / 1980s, there were several experiments that tested whether the ep and μp interactions are equal. They found no convincing differences, once the μp data are renormalized up about 10%. In light of the proton "radius" puzzle, the experiments are not as good as one would like.

Ellsworth et al.: form factors from elastic μp

Kostoulas et al. parameterization of μp vs. ep elastic differences

Entenberg et al. DIS: $\sigma_{μp}/σ_{ep} ≈ 1.0±0.04$ ($±8.6\%$ systematics)
e-μ Universality

The $^{12}$C radius was determined with ep scattering and μC atoms. The results agree:

Cardman et al. eC: $2.472 \pm 0.015$ fm
Offermann et al. eC: $2.478 \pm 0.009$ fm
Schaller et al. μC X rays: $2.4715 \pm 0.016$ fm
Ruckstuhl et al. μC X rays: $2.483 \pm 0.002$ fm
Sanford et al. μC elastic: $2.32^{+0.13}_{-0.18}$ fm

Perhaps carbon is right, e’s and μ’s are the same.
Perhaps hydrogen is right, e’s and μ’s are different.
Perhaps both are right - opposite effects for proton and neutron cancel with carbon.
But perhaps the carbon radius is insensitive to the nucleon radius, and μd or μHe would be a better choice.
Batell, McKeen, Pospelov propose new e/μ differentiating force with ≈ 100 MeV force carriers (guage boson V + complex scalar field), leading to large PV μp scattering. Two forces are needed to keep consistency with gμ-2 data.

Barger, Chiang, Keung, Marfatia indicate that the K → μν decay which could radiate V, and constrains its parameters.
Possible Way to Resolve Puzzle: New ep Experiments

Obvious 1st guess: high energy proton beam (FNAL?) on atomic electrons, akin to low $Q^2$ pion form factor measurements - difficult - only goes to 0.01 GeV$^2$.

With MEIC/EIC, etc., obvious alternative in the longer term: use a ring with bending magnets to provide access to near 0 degree scattering - perhaps in several years.

Very low $Q^2$ JLab experiment, near 0° using ``PRIMEX'' setup: A. Gasparian, D. Dutta, H. Gao et al.
Low intensity beam in Hall B into windowless gas target.

Scattered ep and Moller electrons into HYCAL at 0°.

Lower $Q^2$ than Mainz. Very forward angle, insensitive to $2\gamma, G_M$.

Conditionally approved by August 2011 PAC: ``Testing of this result is among the most timely and important measurements in physics.'' Unlikely to run until 2016 or so (my estimate).
This proposal: \( \mu p \) Scattering at PSI

- Directly test the most interesting possibility, that \( \mu p \) and \( ep \) scattering are different:
  - to higher precision than previously,
  - in the low \( Q^2 \) region (same as Mainz and a JLab experiment now starting) for sensitivity to radius
  - with \( \mu^\pm \) to study possible 2\( \gamma \) mechanisms, but with improved sensitivity from low energy and large angle
  - measuring both \( \mu^\pm p \) and \( e^\pm p \) to have direct comparison and a robust, convincing result.

Depending on the results, 2nd generation experiments (lower \( Q^2 \), \( \mu^\pm n \), higher \( Q^2 \), ...) might be desirable or unneeded.
**The Results!**

- πM1 channel, with $p_{\text{in}} = 115, 153, \text{and } 210 \text{ MeV/c}$: PID reasons.
- Choose $\theta_{\text{scatter}} = 20 - 100^\circ$: rates, backgrounds, systematics.
- $\Delta R = 4\% \Rightarrow \Delta G' = 8\% \Rightarrow \Delta \sigma' = 16\%$.
- Statistics shown with estimated systematics lead to $\Delta R \approx 0.01 \text{ fm for } \mu^+, e^\pm$, but about $0.015 \text{ fm for } \mu^-$.
- Un-answered question: if radius differences are real, are cross section differences really this large?
More Results

Left: pseudo-random data (10° bins) showing effect of a large angle offset.

Right: Estimate of uncertainties on extracted radius - systematic uncertainties dominate

Relative e-µ radius has decreased uncertainties, estimated to be a factor of 2 or more.
Experimental Issues Studied

- **Backgrounds**: Moller & Bhabha scattering, π elastic scattering, π and μ decay in flight, scattering from cell walls.

- **Rate issues**: determining event by event properties of 10 MHz of beam particles, singles rates in detectors, trigger rates.

- **Systematic uncertainties**: angle determination, beam momentum determination, multiple scattering effects, determining flux and efficiency.

- **Detectors**: GEMs, Sci-Fis, beam Cerenkov, wire chambers, threshold Cerenkov, scintillators, certain issues in triggering and DAQ.

- **Management**: cost, time line, possible funding.
What do we need to do?

Basic goal: close to 1% experiment absolute, sub 1% relative, to minimize the amount of improvement needed in fitting out offsets

<table>
<thead>
<tr>
<th>Requirement</th>
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<tbody>
<tr>
<td>Operate at $\approx 10$ MHz beam rates w/ 50 MHz beam</td>
</tr>
<tr>
<td>Know flux of $\mu$'s and e's to $\approx 0.1%$</td>
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<tr>
<td>PID at trigger and analysis level</td>
</tr>
<tr>
<td>2nd PID method for redundancy and consistency</td>
</tr>
<tr>
<td>Know chamber orientation to $&lt; 1$ mr</td>
</tr>
<tr>
<td>Determine event scattering angle to $\leq 10$ mr event by event</td>
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<tr>
<td>Reject ghosts and accidentalst</td>
</tr>
<tr>
<td>Know average incident momentum of particles to 0.1%</td>
</tr>
<tr>
<td>Trigger off $\approx 100$ MeV/c $\mu$'s, e's, not $\pi$'s, Mollers, Bhabhas, ...</td>
</tr>
<tr>
<td>Redundancy for high and well-known efficiencies - trigger and tracking</td>
</tr>
</tbody>
</table>
Detector Cartoon

channel sci-fi array

target

sci-fi array

target

GEM chambers

spectrometer chambers

spectrometer Cerenkov

spectrometer trigger scintillators

beam Cerenkov

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Some Systematics to Control

Left: should know central momentum to tenths of a percent, but can average over a few percent bin. Can “fit this out”.

Right: should know central angle to mr level, but can average over several mr. Can “fit out” offset and correct cross sections for resolution.
πM1 Channel - Nominal Characteristics

≈100 - 500 MeV/c mixed beam of μ’s + e’s + π’s

Dispersion at IFP: 7cm/%

Beam spot (nominal):
1.5 cm X x 1 cm Y,
35 mr X’ x 75 mr Y’

Momentum acceptance: 3% resolution: 0.1%

Spots from 0.7x0.9 cm² up to 16x10 cm², and Δp/p from 0.1-3.0%, used previously.
Determining Particle Type – RF Time

μ separated from π and e

π, μ, e all separated

RF time measured here, here, and at detectors

If random (non-scattered) particle at IFP is a different particle type, the position and momentum of the triggering particle can still be determined.
Rate Considerations

- At 10 MHz rate with 50 MHz beam, 82% chance clean, 16% chance 2 particles, 2% chance >2 particles in RF bucket.
- Reduce acceptance to cut rates for +210, 153 MeV/c.
- 250 ns chamber time scale \(\Rightarrow\) 2.5 background trajectories on average each event.
- Desirable to be able to handle 2\(^{nd}\) particle in same RF bucket as \(\mu\) trigger. Not absolutely needed.

<table>
<thead>
<tr>
<th>(p) (MeV/c)</th>
<th>(\pi) (MHz)</th>
<th>(\mu) (MHz)</th>
<th>(e) (MHz)</th>
<th>(\Sigma) (MHz)</th>
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<tbody>
<tr>
<td>115 + 0.6 2 6 9</td>
<td>153 + 8 2 8 18</td>
<td>210 + 60 5 6 70</td>
<td></td>
<td></td>
</tr>
<tr>
<td>115 - 0.06 0.2 6 6</td>
<td>153 - 0.7 0.2 8 9</td>
<td>210 - 6 0.5 6 12</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>
- Count Flux
- PID with RF time for triggering
- Determine momentum at IFP
- Give TOF between two counters for PID
- Associate trajectory into target with momentum

Rutgers
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GEMs

- Determine trajectory into target for scattering angle and $Q^2$
- Third GEM to reject ghosts
- Existing GEMs at UVa and OLYMPUS
Beam Cerenkov

- Redundant PID for set up, cross checks, flux determination

channel sci-fi array

target sci-fi array

GEM chambers

spectrometer chambers

spectrometer Cerenkov

spectrometer trigger scintillators

Temple

Wednesday, February 22, 2012
Use 4-cm LH$_2$ target, $\approx 0.3$ g/cm$^2$. (0.5% $L_{\text{rad}}$)

$\approx$10x as much H as CH$_2$ target with same multiple scattering.

$\theta_{\text{MS plane}} \approx 10$ mr @ 115 MeV/c, 6.5 mr @ 153 MeV/c, 4 mr @ 210 MeV/c.

Copy recent E906 target design?

Due to E loss in target, $\mu$'s and e's average over $\approx \pm 0.5$ - 1% bin in momentum.
Scattered Particles

- $p$ vs. $\theta$ for 153 MeV/c $\mu$'s + e's + $\pi$'s incident on protons.

Rates of scattered e's and $\mu$'s of interest are small - a few 10's of Hz over the planned acceptance. PID is needed at the trigger level to keep the rate of $\pi$ triggers manageable.
$p$ vs. $\theta$ for 153 MeV/c $\mu$'s + e's + $\pi$'s incident on electrons.

Scattered electrons are low energy and generate $\approx 40$ kHz of tracks into chambers, but not triggers.
μ's from π decay go forward of detectors $\Rightarrow$ π decays near the target are not an issue. A simple GEANT gives a singles rate from 4 m of beam line in the wire chambers as 30, 150, 20 kHz. At the trigger level, these events are suppressed at least 3 orders of magnitude since they have a π RF time, and do not tend to strike two scintillator paddles that point back to the target.

At the analysis level, these events would be further suppressed by tracking back to the target, refined RF time determination, and lack of a GEM track. Their characteristics can be cross checked with empty target measurements.
μ Decay Background

Distribution of electrons from 153 MeV/c μ decay.

μ⁺ → e⁺νμν gives several kHz track rate and ≈400 Hz e⁺ background trigger rate. Rejected at analysis level by requiring tracks from the target, and μ RF time from the detector - the decay electrons will be ≈ 0.8 ns faster than μ scattering events. Rate can be directly measured with empty target.
πp scattering rates calculated with cross sections from SAID and expected luminosities, assuming 2π azimuthal acceptance. Up to a few tens of kHz chamber rates, plus a DAQ rate issue for some kinematics, if not suppressed at the trigger level.
Scattered Particle Considerations

Recoil protons $E$ loss so large that all except forward angle recoil protons stopped in target.

Large angle, very low energy Moller / Bhabha $e'$s lose large fraction of energy in target.

All the low-energy electron and proton backgrounds are ranged out in the first scintillator layer.

Scintillator $dE/dx$ plot looks the same, except curves down a factor of $\approx 2$. 
Adopting So Carolina design: 2 planes of 6 cm x 6 cm scintillator paddles with < 60 ps time resolution.

3rd plane from BLAST / OLYMPUS.

FPGA trigger to require paddles track back to target, to suppress cosmic and decay in flight backgrounds.
Threshold Cerenkov

- Additional PID to supplement SF RF time for π rejection at trigger level
- Media of quartz/lucite for 115 MeV/c, water/teflon for 153 MeV/c, pinhole dried aerogel for 210 MeV/c
• Positioned to determine tracks at 1 mr level (central), but several mr level event by event.
• Need more or less standard wire position precisions of 100 - 200 µm.
• Need chambers positions at the few tenths of mm level.
### Summary of Equipment

<table>
<thead>
<tr>
<th>Equipment</th>
<th>Location</th>
<th>Quantity</th>
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<tbody>
<tr>
<td>Beam Sci-Fi</td>
<td>Rutgers</td>
<td>100 k</td>
</tr>
<tr>
<td>Beam GEMs</td>
<td>Hampton, UVa</td>
<td>existing</td>
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<tr>
<td>Beam Cerenkov</td>
<td>Temple</td>
<td>50 k</td>
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<tr>
<td>Target</td>
<td>MIT/...</td>
<td>300 k</td>
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<tr>
<td>Wire Chambers</td>
<td>MIT</td>
<td>200 k</td>
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<tr>
<td>Cerenkovs</td>
<td>Jerusalem</td>
<td>100 k</td>
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<tr>
<td>Scintillators</td>
<td>So Carolina, Tel Aviv</td>
<td>220 k</td>
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<td>Hampton</td>
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<tr>
<td>Trigger</td>
<td>Rutgers</td>
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<tr>
<td>DAQ</td>
<td>-</td>
<td>?</td>
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### Time Line

<table>
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<th>Event</th>
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<tbody>
<tr>
<td>Feb 2012</td>
<td>Physics Approval</td>
</tr>
<tr>
<td>August 2012</td>
<td>PAC/PSI Technical Review</td>
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<tr>
<td>September 2012</td>
<td>Funding proposals to US agencies*</td>
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<tr>
<td>fall 2012</td>
<td>test measurement in πM1 beamline</td>
</tr>
<tr>
<td>spring 2013</td>
<td>finalize designs</td>
</tr>
<tr>
<td>summer 2013</td>
<td>money arrives - start construction</td>
</tr>
<tr>
<td>fall 2014</td>
<td>start assembling equipment at PSI</td>
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<tr>
<td>late 2014 /</td>
<td>experiment ready to run</td>
</tr>
<tr>
<td>early 2015</td>
<td></td>
</tr>
<tr>
<td>2015</td>
<td>6 month experiment run</td>
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</table>

* Tel Aviv + Jerusalem already applied for ERC advanced grant
Summary

The proton radius puzzle is a high-profile issue - APS plenary talk & invited sessions, PSAS2012 Symposium, Trento ECT* Workshop Nov 2012

Explanation unclear, theoretically or experimentally.

Electron scatterers interested in going to lower $Q^2$: checks $R_{ep}$ scattering, proton structure

Atomic physicists interested in other $\mu$ atoms.

PSI $\mu p$ scattering directly tests interesting possibilities: Are $\mu p$ and $ep$ interactions different? If so, does it arise from $2\gamma$ exchange effects ($\mu^+\neq\mu^-$) or BSM physics ($\mu^+\approx\mu^-\neq e^-$).

Request:

- physics approval.
- technical review about end of summer, 2012: very helpful in proposing funding.
- Test time in fall 2012, check of beam properties and plans.
Backup Slides Follow
Basics: The Proton “Radius”

The proton has several “radii”: electric, magnetic, axial, gravitational, ...

They are defined within non-relativistic quantum mechanics as root mean square (rms) radii. E.g.:

\[ r_E = (r_E^2)^{1/2} = \sqrt{\int d^3r \ r^2 \ \rho_E(r)} \]

where \( \rho_E(r) \) is the normalized charge distribution.

In relativistic QM, the radius is a model-dependent quantity – the impact parameter is not. We will ignore this issue for simplicity, and because it does not fundamentally change the physics importance of the proposal.
In NRQM, the FF is the 3d Fourier transform (FT) of the Breit frame spatial distribution, but the Breit frame is not the rest frame, and doing this confuses people who do not know better. The low $Q^2$ expansion remains.

Boost effects in relativistic theories destroy our ability to determine 3D rest frame spatial distributions. The FF is the 2d FT of the transverse spatial distribution.

The slope of the FF at $Q^2 = 0$ continues to be called the radius for reasons of history / simplicity / NRQM, but it is not the radius.

Nucleon magnetic FFs crudely follow the dipole formula, $G_D = (1+Q^2/0.71 \text{ GeV}^2)^{-2}$, which a) has the expected high $Q^2$ pQCD behavior, and b) is amusingly the 3d FT of an exponential, but c) has no theoretical significance.
Atomic Physics:

Atomic 1/r potential modified by finite size of proton, shifting energy levels.

Effect bigger for muons than electrons due to smaller size of muonic atom orbitals.

Determine transition energies and use theory to infer proton radius.

Lepton scattering:

Scattering cross section depends on form factor, the Fourier transform of spatial charge distribution.

Use corrected scattering cross section to determine form factors, and fit to determine proton radii.

For low four-momentum transfer $Q^2$:

$$F(Q^2) = 1 - Q^2 r^2 /6 + Q^4 r^4 /120 \ldots$$
ep Scattering Basics: 1

Currents
\[ J^\mu_e = \bar{u}(k')[\gamma^\mu]u(k) \]
\[ J^\mu_p = \bar{u}(p')[F_1(Q^2)\gamma^\mu + i\frac{\kappa}{2M}F_2(Q^2)\sigma^{\mu\nu}q_\nu]u(p) \]

Algebra

Cross sections
\[ \sigma_R \equiv \epsilon(1 + \tau) \frac{d\sigma/d\Omega}{d\sigma_{Mott}/d\Omega} = \epsilon G_E^2(Q^2) + \tau G_M^2(Q^2) \]

With form factors:
\[ G_E = F_1 - \tau \kappa F_2 \]
\[ G_M = F_1 + \kappa F_2 \]
\[ F_1 = \frac{G_E + \tau G_M}{1 + \tau} \]
\[ F_2 = \frac{G_M - G_E}{\kappa(1 + \tau)} \]

And kinematic factors:
\[ \tau = \frac{Q^2}{4M^2} \]
\[ \epsilon^{-1} = 1 + 2(1 + \tau) \tan^2 \frac{\theta}{2} \]
Polarizations: 1

Use polarizations for form factor ratios

\[ I_0 P_t = -2 \sqrt{\tau(1 + \tau)} G_E G_M \tan \frac{\theta_e}{2} \]

\[ I_0 P_l = \frac{E_e + E_{e'}}{M} \sqrt{\tau(1 + \tau)} G_M^2 \tan^2 \frac{\theta_e}{2} \]

\[ P_n = 0 \ (1\gamma) \]

\[ \mathcal{R} \equiv \mu_p \frac{G_E}{G_M} = -\mu_p \frac{P_t}{P_l} \frac{E_e + E_{e'}}{2M} \tan \frac{\theta_e}{2} \]

Sensitive to spin transport, insensitive to almost everything else ... but needs large statistics
Measuring two angles at the same time allows a ratio to be made, reducing sensitivity to $P_bP_t$, which can vary by 20% or more over time.
ep Scattering Procedure

- Measure cross sections
- Perform radiative corrections: (c) and (d) depend on experiment cuts, (h) is very small, (a), (b), (e), (f), (g) change cross section, not kinematics
- Do Rosenbluth separations – or – fit world data with form factor parameterization

The electron is too light!
Polarization techniques determine a ratio of electric to magnetic form factors to $\approx$1% total uncertainty.

Decreased ratio compared to earlier data prompted 2 years of systematics studies: cuts, spin transport, backgrounds, ...

Does not get to low enough $Q^2$, but suggests $r_E > r_M$.

E08-007 part 2, dedicated polarized beam – polarized target measurements to cover the range about 0.015 – 0.16 GeV$^2$ with high precision, running late Feb – May 2012.
Some tension between Mainz and JLab

Note that the JLab and Mainz experiments agree better for the FF ratio than the for individual form factors. Thus much of the difference in the FF’s must arise from Mainz vs. “world” cross sections.

Is there an issue in the FF ratio at the low $Q^2$ limit, or is it an end-point problem / statistics? We will know better once we have the polarized target results.
Two-photon exchange tests in $\mu p$ elastics

Camilleri et al. PRL 23: No evidence for two-photon exchange effects, but very poor constraints by modern standards.

No difference between $\mu^+ p$ and $\mu^- p$ elastic scattering

Rosenbluth plot is linear.
Determining Momentum at High Rate

- Need to know $p_{\text{central}}$ to 0.1% level, but can average over “large” range.
- Determine $p$ at IFP with XX’ Sci-Fi array: 7 cm / % dispersion $\Rightarrow$ need position to 7 mm. Plan to use $\approx 110$ 2 mm square fibers / layer. At 10 MHz, $\approx 0.1\%$ chance multiple tracks in same X and X’. Rate in each fiber about 0.1 MHz.
- 2$^{\text{nd}}$ particles can be rejected by RF time if it is a different type from triggering particle.
Sci-Fi Technical Details

- SF: St. Gobain
- Cladding thickness makes each layer \(\approx\)96\% efficient, offset layers allows high efficiency and its determination.
- Fibers give \(\approx\)30 photons at readout / mm thickness of fiber.

- Multi Pixel Photon Counters: Hamamatsu (Si-PMT).
- About 50\% efficiency for 400 – 500 nm photons.
- Timing: 0.25 ns FWHM for 1x1 mm\(^2\), 0.55 ns FWHM for 3x3 mm\(^2\)
- Insensitive to B fields
The Sci-Fi signals will be discriminated and sent to TDCs in the DAQ and an FPGA. We have started a conceptual design for an FPGA that will have the Sci-Fi inputs plus RF time and gate inputs, to:

- act as a scaler, counting hits in 16 1.25 ns time bins relative to the RF
- output signals for programmed time bins corresponding to the 3 different particle types, for input to the trigger

This will allow us to identify events coming from $\mu$, $e$, and $\pi$ beam particles and treat them differently. We want all $\mu$ triggers. The $e$ trigger rate is several times higher and can be suppressed if needed. The $\pi$ events are not wanted for physics, but will be sampled for determining backgrounds, etc.
The flux determined by the Sci-Fi at the IFP has to be corrected for μ decays between the counter and the target, and for trajectories that do not make it to the target, so a 2\textsuperscript{nd} Sci-Fi will be used near the target.

The decay correction is:

\[ N_{\text{target}} = N_{\text{counter}} \ e^{-t/\gamma_T} = N_{\text{counter}} \ e^{-d/\beta_Y c_T} = N_{\text{counter}} \ e^{-d_{\mu}/p c_T}. \]

About $10^{-5}$ of the muons decay per cm of flight path, or about 1% decay from the IFP array to the target. The decaying fraction can be calculated to $\approx 0.1\%$, the survival fraction much more precisely to $\approx 0.001\%$. 
Nominal emittance:
1.5 cm X x 1 cm Y,
35 mr X' x 75 mr Y'

Need central scattering angles at mr level, but event by event angles at several mr level.

Large variation in angles in secondary beam \(\Rightarrow\) incident particles need to be measured for each event. High rates \(\Rightarrow\) GEM chambers.
COMPASS GEMs routinely operated to \( \approx 2.5 \, \text{MHz/cm}^2 \).

Tests by various groups have gone up to several 10s of MHz/cm\(^2\).

We are assuming 10 MHz/1.5 cm\(^2\) = 6.7 MHz/cm\(^2\) (average) rate.

Gas avalanche is in a \( \approx 100 \, \mu\text{m} \) wide - the 1.5 cm\(^2\) πM1 beam spot is “100 x 150 pixels” in size, so the 2-3 random coincidence trajectories have negligible probability of overlap.

Angle divergence of beam leads to ghosts, which can be removed by a 3rd chamber. (Rotation not needed.)

Electronics might allow removal of particles from other RF buckets.
Available GEMs

Access to OLYMPUS (e^+p/e^-p at DESY) GEMS through Hampton. Available at end of 2012. FPGA controlled APV front-end readout (INFN Rome). Well tested and tuned. -or-

UVa has 2 GEMs available as part of JLab SBS project. New GEMS about $10,000 - $30,000 each.

Can determine absolute wire positions in Hall to 100 - 200 µm ➔ know central angle to ≈ 200 µm / 40 cm = 0.5 mr.
Hybrid gas threshold + RICH Cerenkov

Gas threshold efficiently detects electrons and can be used with PID FPGA as cross check of RF time calibration for efficient setup.

RICH likely uses JLab SOLID scheme of CsI radiator.

Dedicated Cerenkov run and prescaled readout allows RF time PID to be cross checked at analysis level for non-scattered particles.
The channel Sci-Fi + 2 GEMs are sufficient to determine the incoming momentum vector for events with one track.

For events with background tracks, a 3rd GEM resolves ghosts. But we also need to correlate the momentum and PID at the channel IFP with the trajectory at the target.

A Sci-Fi near the target with 2 mm XYU fibers ("40 pixels") can

- Measure RF time
- Measure TOF over a \( \approx 9 \) m flight path
- Correlate GEM tracks to momentum measurement in channel for essentially all particles from different RF buckets and nearly all particles from the same RF bucket.

Expect to put SciFi upstream of GEMs, but will study if SciFi array can be put downstream of the target.
Cosmic ray test of some of the 400 JLAB CLAS12 Forward Time of Flight scintillators being built at So. Carolina by R. Gothe et al.

Time Resolution with BC-404 scintillator and Hamamatsu R9779 PMT is $\sigma_{\text{avg}} = 51$ ps for 203 cm bars, 34 ps for 69 cm bars.
Scintillators

Copying the So. Carolina 6 cm x 6 cm scintillator paddle design with 2 scintillator planes 70 and 100 cm from the target requires planes made of 20 1.4-m long scintillators and 28 2-m long scintillators. The system cost is ≈220 k$.

Although the SC scintillators are highly efficient, we will add one scintillator plane from existing OLYMPUS scintillator paddles, to save cost and give redundancy & efficiency data.

For triggering, an FPGA (e.g., CAEN v1495) will require tracks that roughly point to the target, and allow for inefficiencies.

Cannot use RF time of scintillator hits for triggering. In the analysis, 60 ps resolution separates particles by RF time by > 4 ns / 60 ps ≈ 70σ. Electrons coming from muon decay in flight are separated from scattered muons by 0.4 – 1.5 ns, or 7σ – 25σ in the analysis.
Threshold Aerogel Detector

Additional suppression of pion triggers

from: M. Tabata, Japan Aerospace Exploration Agency, talk at TIPP2011, Chicago

<table>
<thead>
<tr>
<th>Beam</th>
<th>$n_{\text{threshold}}$</th>
<th>Material</th>
</tr>
</thead>
<tbody>
<tr>
<td>210</td>
<td>1.19–1.20</td>
<td>pinhole dried Aerogel</td>
</tr>
<tr>
<td>153</td>
<td>1.32–1.36</td>
<td>water / teflon</td>
</tr>
<tr>
<td>115</td>
<td>1.50–1.58</td>
<td>quartz / lucite</td>
</tr>
</tbody>
</table>

Expect design to be similar to Qweak Cerenkov
Scattered particle wire chambers have moderate total rates, about 400 khZ in total system, as long as $\theta_{\text{min}} > 20^\circ$. Most of the rate is low energy electrons / positrons from the target, and $\mu$'s from in-flight beam $\pi$ decays upstream of the target. With chambers close to the target, the wire lengths will be short, and position resolution of 100 $\mu$m and angle resolution of $<1$ mr (neglecting multiple scattering) should be achievable. The main issue being thought about it how to keep the relative angle of the GEMs and scattered particle wire chambers under control.
We have started development of a simulation of the experiment, so that backgrounds and detector design trade-offs can be better understood. It remains under development at this stage.