Orbital Selective Fermi Surface Shifts and Mechanism of High $T_c$ Superconductivity in Correlated AFeAs ($A = \text{Li, Na}$)

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Based on the dynamical mean field theory and angle resolved photoemission spectroscopy, we have investigated the mechanism of high $T_c$ superconductivity in stoichiometric LiFeAs. The calculated spectrum is in excellent agreement with the measured angle resolved photoemission spectroscopy. The Fermi surface (FS) nesting, which is predicted in the conventional density functional theory method, is suppressed due to the orbital-dependent correlation effect within the dynamical mean field theory method. We have shown that such marginal breakdown of the FS nesting is an essential condition to the spin-fluctuation mediated superconductivity, while the good FS nesting in NaFeAs induces a spin density wave ground state. Our results indicate that a fully charge self-consistent description of the correlation effect is crucial in the description of the FS nesting-driven instabilities.

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Iron pnictides have attracted much attention due to their high $T_c$ superconductivity (SC) [1]. A prime candidate for the pairing glue is the spin fluctuation (SF) mechanism. It has been argued that itinerant electrons form a spin density wave (SDW) via Fermi surface (FS) nesting, and that antiferromagnetic SFs can mediate the pairing in the vicinity of the SDW phase boundary [2]. In this scenario, a key ingredient to SC is the FS nesting property. However, the FS nesting property of iron pnictides has been controversial. Some systems are believed to possess good nesting properties [3–5], while some are not [6,7]. Also there have been many theories that emphasize the role of local Fe 3$d$ electrons [8–11].

Resolving such controversy requires accurate determination of FS topology and orbital characters. Theoretical simulations based on a first-principles method can provide such information. However, the conventional density functional theory (DFT) method often fails to describe the electronic structure due to the significant electron correlation effect in Fe-based superconductors. Calculated bands have to be renormalized by approximately 2–4 to fit the experimentally measured bandwidth, and the predicted spin magnetic moment is about twice larger than the experimental value. On the other hand, the dynamical mean field theory (DMFT) on top of the DFT showed consistent results with the measured bands, the anisotropy, and the small magnetic moment [12–17].

Even though DMFT has been shown to work well, the comparison of calculated and measured band structures, especially the FS, is still important to check the validity of the calculation. For an accurate comparison of theory and experiment, LiFeAs is the most suitable system at present. The most studied 122 systems such as BaFe$_2$As$_2$ do not have neutral cleavage planes, which affects surface sensitive techniques such as the angle resolved photoemission spectroscopy (ARPES).

On the other hand, neutral cleavage surfaces of LiFeAs allow us an accurate experimental determination of the band structure, FS topology, and quasiparticle dynamics [6]. In this respect, DMFT correction on the band structure of LiFeAs in comparison with experimental data should provide a unique opportunity to obtain accurate electronic structure information. This realistic band structure can help resolve several issues on, for example, SF scenario and anisotropic $s\pm$ wave [18–21].

For this reason, we performed both DMFT and ARPES studies on LiFeAs. Our goal is to validate the accuracy of our DMFT method by comparing with ARPES results, and to unravel the SC mechanism by analyzing the DMFT spectral function. It will be shown that the FS nesting is marginally suppressed in LiFeAs due to the selective correlation effect of each Fe 3$d$ orbital, and that this gives rise to the electron pairing mediated by the SF. Simulation on LiFeAs is based on the fully self-consistent DFT in combination with DMFT (DFT + DMFT) as
implemented in WEN2K [22–25]. The local self energy due to the correlated Fe 3d orbital is obtained with the continuous time quantum Monte Carlo impurity solver [26], where $U = 5.0$ eV and $J = 0.8$ eV are used [27–29]. Such $U$ value does not vary much across Fe-pnictides and chalco-

goensides [17], so we use the same parameter for Li and Na.

Ref. [30]. Single crystals used in the experiments were synthesized by the Sn-flux method [31].

In Figs. 1(a) and 1(b), the DFT band structures are shown by red lines. Overlayed on top of the bands are the $d_{xz,yz}$ [Fig. 1(a)] and $d_{xy}$ [Fig. 1(b)] orbital contributions, respectively, as indicated by the size of the black circles. Two small hole bands near the $\Gamma$ and one small electron band near $M$ are mostly from $d_{xz,yz}$ orbitals, while the large hole and electron bands are from the $d_{xy}$ orbital. Using the self-energy $\Sigma(\omega)$ obtained from the DFT + DMFT calculation, we compute the momentum-resolved spectral function to inspect relative changes of those bands. The result is shown in the lower panel of Fig. 1(c). The DFT band structure in Fig. 1(c) is scaled by an average renormalization factor of 2.55 for comparison. The most noticeable aspect of the data near $\Gamma$ is that two $d_{xz,yz}$ related inner hole bands are selectively lowered, while a $d_{xy}$ related outer hole band is slightly shifted up, which will be discussed.

The calculated spectrum can be compared with the ARPES data in the upper panel of Fig. 1(c) presented in the same scale. Three hole bands near $\Gamma$ are shown clearly in both theoretical and experimental spectra. Near the $M$ point, there is only one electron band in the ARPES, though the DFT + DMFT predicts two bands crossing $E_F$. The discrepancy can be ascribed to the matrix element effect. Indeed, we can see the deep electron band along the $\Gamma$ to $M$ direction with different light polarization (see Supplemental Material [32] Fig. S2). In addition, in Figs. 2(a) and 2(b), two electron FSs are clearly observed along the direction perpendicular to the $\Gamma$ to $M$ near the $M$ point. The vertical dashed lines in Fig. 1(c) denote positions of experimental Fermi wave vectors. Our theoretical predictions exhibit small deviation from experimental ones, especially for the outer electron pocket near $M$. This might be due to the usual Li deficiency in the samples. A better agreement is obtained if we lower the Fermi level by 0.01 eV as indicated by the horizontal dashed line in Fig. 1(c) (4% Li deficiency) [33]. On the contrary, a shift of the Fermi level alone does not give a good agreement between DFT (green solid lines) and experimental results. Especially, the hole bands deviate even further.

The change of the FS size due to the correlation effect affects the nesting condition. Shown in Figs. 2(a) and 2(b) are FSs at $k_z = 0$ and $\pi$, respectively. There are three hole pockets ($h_1$, $h_2$, $h_3$) near $\Gamma$ and two electron pockets ($e_1$, $e_2$) near $M$. The smallest hole pocket ($h_1$) has strong $k_z$ dependence and does not appear at $k_z = \pi$. One can see that $xz/yz$-dominant hole FSs shrink while the $xy$-dominant hole FS expands compared to the DFT results. Similar results have been recently reported for various Fe-based superconductors [13,17,34]. Our DFT + DMFT results also agree well with the experimental results in the figure on the right-hand side as well as reported ARPES data [6,18,35]. Meanwhile, we do not see a sizable difference in the electron FS size for the two methods, which results in suppression of FS nesting between hole and electron pockets in the DFT + DMFT results.

To check the nesting conditions, we show in Fig. 2(c) overlayed hole and electron FSs in the $\Gamma$-$M$-$Z$ plane. While the DFT result exhibits a good nesting between the second hole pocket and an electron pocket (left panel), nesting becomes poor for the DFT + DMFT result (right panel). Such a difference in the nesting property can influence the quantum transition behavior dramatically, as will be shown later.

A natural question is on the mechanism of the selective FS shift that increases (decreases) the $xz/yz$ ($xy$) hole FS size and affects the nesting condition. We show that it is related to the charge transfer among Fe-3d orbitals which
is done during the fully self-consistent DFT + DMFT steps. We have checked the spectral function calculated by the DMFT self energy without charge self consistency, and could not observe clear energy shifts as in the fully self-consistent case. Figure 3(a) shows the variation of the DMFT charge density from the DFT result. The electron density increases along Fe-Fe bonds (red color) whereas it decreases along Fe-As bonds (blue). Since the Cartesian $x$ and $y$ axes are chosen along Fe-Fe bonds in our calculation, the $d_{xz}/y$ orbital occupancy is increased while the $d_{xy}$ orbital occupancy is decreased. This is consistent with the downshift of $d_{xz}/y$-related bands and upshift of $d_{xy}$-related bands shown in Fig. 1.

FIG. 2 (color online). DMFT (solid lines) and DFT (dashed lines) Fermi surfaces at (a) $k_z = 0$, (b) $k_z = \pi$ are compared with the experimental FSs guided by dashed lines. For the experimental data, we applied the 2D curvature method for clarity [38]. The $k_z$ for the measured electron pockets is not exactly at 0 or $\pi$ as the data were taken on a constant total momentum surface (fixed photon energy). (c) $k_z$ dependence of FSs along the $\Gamma$-M-Z cut. To check the nesting condition, electron pockets denoted by dash-dot lines are shifted by ($\pi$, $\pi$), and plotted on top of hole pockets (solid lines). DFT and DFT + DMFT results are shown in left and right panels, respectively.

FIG. 3 (color online). (a) Isosurface plot of electron density difference between DFT and DFT + DMFT results. The red (brighter) or blue (darker) means increase or decrease of 0.003 $e/\AA^3$ upon the DMFT calculation. The Cartesian $x$ or $y$ axis is chosen along the Fe-Fe bonds, so the increase is related mainly to the $d_{xz}$ or $d_{yz}$ orbital of Fe, while the decrease to $d_{xy}$. (b) Calculated DFT and DFT + DMFT total energies against As height relative to the Fe plane.

Charge transfer from the $xy$ to the $xz/yz$ orbital can be understood to be caused by the difference in the hybridization magnitude, $t$ of each orbital. Under the common Coulomb interaction $U$, the renormalization factor, $1/Z \approx U/t$, varies from 2.1 for $z^2$ and $x^2-y^2$ to 3.9 for $xy$. $xz/yz$ has an intermediate value of 2.9. Therefore, the $xy$ orbital experiences a smaller hybridization (or larger localization) compared to $xz/yz$. It means a larger Coulomb energy cost, which favors less occupation in $xy$. Since $t_{2g}$ orbitals mainly contribute to near $E_F$ states, $xy$ electrons will be transferred to $xz/yz$ orbitals.

The charge redistribution due to the electron correlation also substantially contributes to bonding properties. The decrease in the electron density along the Fe-As bond direction makes the Fe-As bond weaker, which induces a longer Fe-As bond or higher arsenic height compared to the DFT estimation. In Fig. 3(b), we show the calculated total energy as a function of As height, $h(As)$, by DFT and DFT + DMFT methods. Compared to the experimental value of $h(As)_{exp} = 1.5$ Å Ref. [36], the DFT method predicts a position 0.1 Å lower, which indicates overestimation of the binding in the DFT method. Meanwhile, the
DFT + DMFT estimation is in good agreement with \( h(\text{As})_{\text{exp}} \).

As shown above, our DFT + DMFT results are in good agreement with the experimental measurements and shows that the nesting is marginally established. This suggests that LiFeAs is located near the SDW boundary and that the SF can be the pairing glue for the SC. In order to check such a possibility, we have performed quantitative analysis of the nesting-driven instabilities by utilizing the calculated spectral function \( A(k, \varepsilon) \). In Fig. 4(a), we compare the bare susceptibilities \( \chi_0(\mathbf{q}) \). The nesting enhancement at \( \mathbf{q} = M \) is much suppressed by including the correlation effect. It is mainly due to the size mismatch between hole and electron FSs as shown in Fig. 2(c). Since the \( A(k, \varepsilon) \) is mostly from \( xz/yz \) and \( xy \) orbitals, we focus on their contributions to \( \chi_0(\mathbf{q}) \). In addition, only the intraorbital scattering is considered because it gives the dominant contribution to the SC [21]. In Fig. 4(b), the \( xz/yz \) intraorbital contribution is significantly larger (about twice) than that of \( xy \). It is because there are more \( xz/yz \) orbital derived states near the Fermi level. The shape of \( \chi_0(\mathbf{q}) \) in Fig. 4(a) is also well reproduced by the scattering between \( xz/yz \) dominant states. Therefore, the FS nesting can be understood to be effectively between two \( xz, yz \) derived bands (hole and electron bands near \( \Gamma \) and \( M \), respectively). Note that the smallest hole pocket at \( \Gamma \) has a negligible effect on the nesting property.

Suppressed nesting predicted by the DMFT spectrum implies that the SDW phase is also suppressed and the SF driven SC ordering becomes more probable. To have a SDW phase, the following condition is satisfied for a given nesting vector \( \mathbf{Q} \).

\[ 1 < V_{\text{SDW}} \chi_0(\mathbf{Q}, T). \tag{1} \]

A similar condition follows for the SF-driven SC:

\[ 1 < \frac{1}{\beta \pi} \sum_{\mathbf{q}} [V_{\text{SF}}(\mathbf{q})]^2 \chi_{\text{SF}}(\mathbf{q}), \tag{2} \]

where \( V_{\text{SF}}(\mathbf{q}) = V_{\text{SDW}}^2 \chi_0(\mathbf{q})/[1 - V_{\text{SDW}} \chi_0(\mathbf{q})] \) denotes the singlet interaction channel, and \( \chi_{\text{SF}}(\mathbf{q}) \) is the associated SF susceptibility. Using the calculated DMFT \( xz/yz \) spectra, we compute \([1 - V_{\text{SDW}} \chi_0] \) and \( \chi_{\text{SF}} \) at the nesting vector \( \mathbf{Q} = M \) as a function of temperature in order to check the leading order between SC and SDW. Figure 4(c) shows the critical \( T_{\text{SDW}} \) with the condition in Eq. (1). Also \( T_{\text{SF}} \) is estimated from the function of \( \chi_{\text{SF}}(\mathbf{Q}) \) using the condition of Eq. (2). Note that \( \chi_{\text{SF}}(\mathbf{q}) \) is a smooth monotonic function and does not need to be positive as shown in Fig. 4(c). Since \( V_{\text{SF}}(\mathbf{q}) \) shows a singular behavior near the SDW ordering for given \( \mathbf{Q} \) and \( T_{\text{SDW}} \), the condition in Eq. (2) can be always realized when \( \chi_{\text{SF}}(\mathbf{q}) \) is positive. So \( T_{\text{SC}} \) can be defined where \( \chi_{\text{SF}}(\mathbf{Q}) \) becomes positive as decreasing temperature. In LiFeAs, \( T_{\text{SC}} \) is always estimated to be higher than \( T_{\text{SDW}} \) as shown in Fig. 4(c).

For comparison, we show in Fig. 4(d) the SC and SDW instabilities of NaFeAs which has a SDW ground state. One can see that \( T_{\text{SDW}} \) is higher than \( T_{\text{SC}} \) in NaFeAs, in agreement with experiments. Such a difference between NaFeAs and LiFeAs comes from the fact that the FS nesting is stronger in NaFeAs (in the DMFT calculation), which enhances the SDW instability and increases the \( T_{\text{SDW}} \). On the other hand, SF is suppressed due to the stable SDW phase and thus \( T_{\text{SC}} \) is decreased. As a result, our DFT + DMFT method correctly predicts both SC and SDW ground states of LiFeAs and NaFeAs, respectively. Note that the DFT spectrum does not give a SC transition because both compounds show good nesting features, resulting in a stable SDW ground state.

In summary we have shown that the inclusion of electron correlation effect is essential to correctly describe the orbital occupation, FS sizes, and As height, all which are important factors for unraveling the SC pairing mechanism [37]. Our fully self-consistent DFT + DMFT calculation has accurately described the marginal FS nesting of LiFeAs observed in ARPES experiments. Using the DFT + DMFT spectrum, we also have successfully reproduced the SF-mediated SC in LiFeAs and SDW ground state in NaFeAs.

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We used a large $U$ value compared to one in the literature because our full-electron calculation method explicitly includes all bands in the energy range of $[-10, 10]$ eV, not just the Fe 3$d$ bands for which other itinerant bands (e.g., As 4$p$ bands) screen $U$ beyond a certain energy. Therefore, $U$ is much smaller when only the Fe 3$d$ bands are considered, and increases substantially when As 4$p$ bands are explicitly taken into account in the so-called $p$-$d$ model. It increases even further when more bands are included in the model construction.


