Atomistic simulations of the incipient ferroelectric KTaO₃

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A parameterized effective Hamiltonian approach is used to investigate KTaO₃. We find that the experimentally observed anomalous dielectric response of this incipient ferroelectric is well reproduced by this approach, once quantum effects are accounted for. Quantum fluctuations suppress the paraelectric-to-ferroelectric phase transition; it is unnecessary to introduce defects to explain the dielectric behavior. The resulting quantum-induced local structure exhibits off-center atomic displacements that display longitudinal, needle-like correlations extending a few lattice constants.

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I. INTRODUCTION

Numerous experimental and theoretical studies have been carried out on the perovskite KTaO₃ over the last 40 years (see, e.g., Refs. 1–12, and references therein), making this material one of the most studied “incipient ferroelectrics.” The main reason for this interest is that the dielectric constant of KTaO₃ increases continuously with decreasing temperature down to ~10 K, but then saturates to a plateau at a large value (≈4000) at lower temperatures while remaining paraelectric and cubic all the way down to 0 K.²,³ These anomalous low-temperature features are usually thought to be caused by the suppression of a paraelectric-to-ferroelectric phase transition by zero-point quantum fluctuations²,³ (hence, the name “incipient ferroelectric” or “quantum paraelectric” used to describe KTaO₃ and other materials, such as SrTiO₃, exhibiting similar unusual dielectric and structural properties). Surprisingly, this generally accepted picture is apparently not supported by various first-principles calculations, using the density-functional theory (DFT) either in its local-density approximation (LDA),¹³ or generalized-gradient approximation (GGA).¹⁴,¹⁵ form since these simulations all predict that KTaO₃ should be paraelectric at T=0 even when neglecting zero-point motion.⁴,⁶ This raises the possibility that LDA and GGA are not accurate enough to adequately reproduce the qualitative properties of incipient ferroelectrics. An alternate explanation for this discrepancy between first-principles calculations and experiments is that the simulations assume a perfect material while real samples may contain defects such as oxygen vacancies and Fe³⁺ ions,²,⁵,⁷,⁸ that might lead to the observed anomalous properties of KTaO₃. In fact, the interpretation of various experiments⁹,¹⁰ still remains controversial as to whether they are attributable to extrinsic effects (i.e., defects induced) or intrinsic off-center atomic displacements. Furthermore, while previous studies invoke the existence of ferroelectric microregions inside the macroscopically-paraelectric KTaO₃ system to explain some of its properties,⁹,¹¹ there has never been any direct determination of the size and shape of these proposed polar regions, to the best of our knowledge. For instance, the pioneering work of Ref. 9 made several assumptions in their analysis of low-temperature Raman spectra—such as isotropy of these microregions—to extract a characteristic size ≈16 Å for these polar regions.

We use large-scale atomistic simulations to shed light on the aforementioned long-standing problems. We report calculations on KTaO₃ using a parameterized effective Hamiltonian approach. Our main findings are that (i) LDA and GGA are indeed not accurate enough to reproduce the observed anomalous properties of KTaO₃, even qualitatively; (ii) these properties can be understood without the need of introducing defects, if quantum fluctuations are present to suppress the paraelectric-to-ferroelectric transition; (iii) the low-temperature local structure of KTaO₃ is characterized by off-center atomic displacements that are longitudinally correlated, in a needle-like (and thus anisotropic) way, with a correlation length spanning a few five-atom unit cells.

The remainder of this paper is organized as follows. In Sec. II, we give a brief description of the methods we have used. Section III discusses the results on dielectric susceptibility and microscopic properties of KTaO₃. Finally, Sec. IV concludes the paper.

II. METHODOLOGY

We use the effective Hamiltonian (H_eff) approach developed in Ref. 16 to investigate finite-temperature properties of KTaO₃. Within this approach, the total energy E_tot is a function of three types of local degrees of freedom: (1) the u_i (B-site centered) local soft-mode amplitude in each five-atom cell, describing the local polarization in each cell; (2) the v_i (A-site centered) inhomogeneous strain variables; and (3) the homogeneous strain tensor. E_tot contains 18 parameters and 5 different contributions: a local-mode self energy, a long-range dipole-dipole interaction, a short-range interaction between local modes, anelastic energy, and an interaction between the local modes and strains.¹⁶ This effective Hamiltonian approach has been successfully used to model,
These CMC and PI-QMC simulations both KTaO$_3$, but reaching a much higher dielectric constant response has indeed been experimentally observed in the paraelectric ground state. A plateau for the dielectric response is seen in the simulations at temperatures decreasing down to nearly 0 K. Turning on quantum effects, we use 50 000 Monte-Carlo sweeps for thermalization and 200 000 sweeps at 3 K to accurately predict the dielectric response. (Note that we are not aware of any previous work reporting the dielectric response computed using PI-QMC.)

In PI-QMC, each five-atom cell interacts with its images at neighboring imaginary times through a spring-like potential (mimicking the zero-point phonon vibrations), while all the five-atom cells interact with each other at the same imaginary time through the internal potential associated with $E_{tot}$. The product $TP$, where $T$ is the simulated temperature and $P$ is the number of imaginary time slices (Trotter number), controls the accuracy of the PI-QMC calculation. In all our simulations we use $TP=600$, which we find leads to sufficiently converged results. Outputs of the PI-QMC simulations thus contain local modes $u_i(t)$, where $i$ indexes the five-atom unit cells of the studied supercell while the imaginary time $t$ ranges between 1 and $P$. Note that CMC simulations can be thought of as corresponding to $P=1$, so that they do not yield imaginary-time-dependent outputs.

III. RESULTS

Figure 1(a) shows the $\chi_{33}$ dielectric susceptibility—where the index 3 refers to the [001] pseudocubic direction—as predicted by the $H_{eff}$ approach, with all its parameters being derived from LDA calculations on small supercells of KTaO$_3$ at its experimental lattice constant. (Note the technical details in Ref. 5 and that these LDA-derived parameters are given in Table I.) It can be clearly seen that CMC calculations yield a $\chi_{33}$ that is continuously increasing as the temperature is decreasing down to nearly 0 K. Turning on quantum effects leads to the appearance of a plateau below 100 K with a value of $\sim 100$ for the dielectric constant. These CMC and PI-QMC simulations both predict a cubic paraelectric ground state. A plateau for the dielectric response has indeed been experimentally observed in KTaO$_3$, but reaching a much higher dielectric constant ($\sim 4000$) and over a much narrower temperature range (i.e., below 10 K) than in Fig. 1(a).

In view of these two discrepancies, we have experimented with making minor adjustments in the LDA-fitted parameters in the hope of obtaining better agreement with experimental data. We have found that this can be done by adjusting just one of the 18 parameters, namely, the parameter denoted $\kappa_2$

in Ref. 16 which describes the harmonic part of the local-mode self-energy. (In our model, reducing $\kappa_2$ favors ferroelectricity with respect to paraelectricity since it leads to a decrease of the zone-center transverse optical frequency by weakening short-range repulsions.) Figure 1(b) shows that decreasing this single $\kappa_2$ parameter by $\sim 18\%$ from its LDA value of 0.0866 a.u. (atomic units) leads to reasonable agreement between our PI-QMC simulations and measurements, not only for the value of the dielectric constant plateau, but also at temperatures above 10 K. (Note that the dielectric response was calculated using the correlation function approach of Refs. 17 and 18 for temperatures higher than 100 K.) In the latter case, we used electric fields ranging between 0 and 2 $\times 10^6$ V/m.

Furthermore, this modified $\kappa_2$ also results in a dramatic difference between the two kinds of Monte-Carlo calculations. CMC simulations yield a ferroelectric rhombohedral
ground state. The corresponding Curie temperature is around 30 K, as evidenced by the peak in dielectric response displayed in Fig. 1(b). On the other hand, PI-QMC predicts a paraelectric ground state. In other words, quantum effects suppress the paraelectric-to-ferroelectric phase transition, which is consistent with the accepted picture.\cite{2,3} Figures 1(a) and 1(b) thus reveal that extrinsic defects (such as impurities or vacancies), which have been proposed to be responsible for the anomalous properties of KTaO$_3$,\cite{2,3,7} are not needed to reproduce the experimental behavior of this material; and (ii) strongly suggest that, unlike in strongly ferroelectric perovskites,\cite{19,20} the LDA is not accurate enough for simulating KTaO$_3$.

As for GGA, Tinte et al.,\cite{6} report zone-center optical frequencies in cubic KTaO$_3$ that are all positive and close to the LDA values. According to Figs. 1(a) and 1(b), we can thus conclude that a GGA effective Hamiltonian would not provide a significant improvement over our LDA one, and will also fail in reproducing measurements. This makes KTaO$_3$ a useful test case for the development of functionals within DFT or other \textit{ab initio} methods.

We now analyze the microscopic structure of KTaO$_3$ at low temperature. Figure 2 depicts the magnitude of the local modes $u_i$, inside each $i$ fives-site cell versus the angle that these local modes make with the pseudocubic [100] direction, as obtained from a $T=3$ K snapshot among the thermally equilibrated Monte-Carlo configurations using $E_{\text{tot}}$ with the modified $\kappa_2$. (The magnitude of the local mode is directly proportional to the magnitude of the local polarization, e.g., $|u|=0.006$ and 0.026 a.u. correspond to a local polarization $\approx 0.0583$ and 0.253 C/m$^2$, respectively.) Figure 2(a) displays the CMC results, while Fig. 2(b) corresponds to PI-QMC.\cite{27}

Comparing Figs. 2(a) and 2(b) reveals how quantum effects affect the microscopic structure of KTaO$_3$: the local polarizations go from all lying close to the [111] direction (corresponding to an angle $\approx 54^\circ$) and having a relatively large magnitude, to being heavily scattered in direction and having a much smaller but nonzero magnitude. The fact that KTaO$_3$ exhibits nonzero local dipoles, even when quantum fluctuations are accounted for, is consistent with the first-order lines observed in Raman spectra and which are forbidden in the ideal cubic perovskite structure.\cite{3,10} Furthermore, an inspection of Fig. 2(b) does \textit{not} reveal any obvious polar microregions. For instance, our quantum-statistical results do not show the local-mode distributions breaking up into clusters centered along {111} directions (i.e., angles of $\approx 54^\circ$ and/or $125^\circ$) as would be expected for such polar microregions. Incidentally, Fig. 2(b) suggests an order-disorder picture (all modes are off-site) rather than a displacive one. It also reveals that the Comes’ “eight-site” model,\cite{28} is not appropriate to describe KTaO$_3$, since the local modes lie along all possible directions.

To gain further insight into the local structure of KTaO$_3$, we decided to compute an additional set of coefficients defined as

$$\theta_{\mu}(\mathbf{r}) = \sum_{i=1}^{N} \frac{u_{i,\mu}u_{i,\mu,\mathbf{r}}}{|u_{i,\mu}|^2},$$

(1)

Here $\mu$ denotes the $x$, $y$, or $z$ Cartesian axis chosen along the [100], [010], or [001] cubic directions, respectively. The index $i$ runs over all the $N$ B sites; $u_{i,\mu}$ and $u_{i,\mu,\mathbf{r}}$ are the $\mu$ components of the local modes in cell $i$, and in the cell centered at a distance $\mathbf{r}$ from cell $i$, respectively. The case in which the local dipoles all have the same (nonzero) magni-

\[ \text{TABLE I. The LDA-derived } H_{\text{eff}} \text{ parameters in atomic units for KTaO}_3 \text{ following the notation in Ref. 16.} \]

<table>
<thead>
<tr>
<th></th>
<th>$a_0$</th>
<th>Soft mode mass</th>
<th>95.6</th>
</tr>
</thead>
<tbody>
<tr>
<td>Onsite</td>
<td>$\kappa_2$</td>
<td>0.0866</td>
<td>$\alpha$</td>
</tr>
<tr>
<td>Intersite</td>
<td>$j_1$</td>
<td>-0.02417</td>
<td>$j_2$</td>
</tr>
<tr>
<td></td>
<td>$j_3$</td>
<td>0.00782</td>
<td>$j_4$</td>
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<tr>
<td></td>
<td>$j_6$</td>
<td>0.00242</td>
<td>$j_7$</td>
</tr>
<tr>
<td>Elastic</td>
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<td>6.51</td>
<td>$B_{12}$</td>
</tr>
<tr>
<td>Coupling</td>
<td>$B_{1xy}$</td>
<td>$-2.5179$</td>
<td>$B_{1yy}$</td>
</tr>
<tr>
<td>Dipole</td>
<td>$Z^*$</td>
<td>9.619</td>
<td>$\varepsilon_\infty$</td>
</tr>
</tbody>
</table>

$^a$Reference 6.

$^b$Reference 31.
their local modes—is associated with a zero value for $u_m$ obtained for all symmetry related cases, e.g., for $u_r$ increase as the magnitude of $r$ only when $r$ is along the $x$ axis. This is in good agreement with the characteristic size of 16 Å extracted from low-temperature Raman spectra of KTaO$_3$. On the other hand, our simulations go against the hypothesis of isotropic correlation made in Ref. 9. The longitudinal needle-like correlations depicted in Fig. 3(b) have also been predicted to occur in classical ferroelectrics just above the paraelectric-to-ferroelectric transition temperature. In fact, they are pre-transitional effects that are probably common to most ferroelectric perovskites, the peculiarities of quantum paraelectric KTaO$_3$ being that the phase transition does not actually occur and that the needle-like correlations result in a plateau for the dielectric response. Finally, note that these needle-like correlations are consistent with the peculiar diffuse x-ray scattering observed in Ref. 12.

IV. CONCLUSIONS

We have performed large-scale atomistic simulations to investigate the (defect-free) incipient ferroelectric KTaO$_3$ system using a parameterized effective-Hamiltonian approach. The effect of quantum-mechanical zero-point motion is investigated by comparing the results of classical and path-integral Monte Carlo simulations. We find that the fitting of all the $H_{\text{eff}}$ parameters within LDA yields a theoretical dielectric constant that is in poor quantitative agreement with experiment, strongly suggesting that LDA is inadequate for this material. Results in the literature also indicate that GGA will not improve the LDA result. On the other hand, a small modification of a single parameter in $H_{\text{eff}}$ from its LDA value is enough to obtain reasonable agreement between theory and experiment for the dielectric constant over a wide temperature range. This modified $H_{\text{eff}}$ leads to the predictions that (i) KTaO$_3$ is ferroelectric classically, but becomes paraelectric once zero-point phonon vibrations are included, and (ii) the quantum-induced local structure of KTaO$_3$ is characterized by nonzero local dipoles that have longitudinal, needle-like correlations with a correlation length spanning a few unit cells. Finally, our work provides a basis for a theoretical framework to tackle compositionally disordered alloys, based on incipient ferroelectrics, which do exhibit ferroelectric phases.

ACKNOWLEDGMENTS

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27 Starting from the path-integral form of the partition function, it can be shown that the local modes $u_i(t)$ are to be averaged over imaginary time before computing static quantities such as the local mode distributions of Fig. 2(b) or the correlations defined by Eq. (1). Hence, it is not correct to compute these quantities at different imaginary times and then average over $t$.