## Errata for

# Berry Phases in Electronic Structure Theory: <br> Electric Polarization, Orbital Magnetization <br> and Topological Insulators 

David Vanderbilt
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p. viii: On line 25, "topics topics" should be replaced by "topics".
p. 12: Caption of Fig. 1.3: "(a)" should be removed in the first line.
p. 41: Two lines below Eq. (2.15), $H_{\mathrm{KS}}$ should be replaced by $V_{\mathrm{KS}}$.
p. 49: Below Eq. (2.45), "any one-particle operator $\mathcal{O}$ " should be replaced by "any cell-periodic one-particle operator $\mathcal{O}$ ".
p. 61: Below Eq. (2.75), "secular equation" should be "eigenvalue equation".
p. 77: In Eq. (3.3), there is a small right bracket that should be enlarged to match the left bracket.
p. 86: Exercise 3.2 should read as follows:

Exercise 3.2 In Sec. 3.1.1 we constructed the parallel-transport gauge of Eq. (3.9) for the system described by Eq. (3.2). Show that Eq. (3.2) corresponds to a twisted parallel-transport gauge. There are two other choices for a twisted parallel-transport gauge starting from the same $\left|\bar{u}_{a}\right\rangle$. What are they?
p. 86: In Ex. 3.4, "under the cyclic series of distortions shown there" should be replaced by "under the continuous cycle passing through the stages shown there". In (a), "mesh of $\varphi$ values and save them in an array" should be replaced by "mesh of $\varphi$ values, and increase the mesh density until you obtain a converged result".
p. 95: On the left-hand side of the last line of (3.43), $t_{23}$ should be $t_{20}$.
p. 97: On the left-hand side of the last line of $(3.44), t_{23}$ should be $t_{20}$.
p. 102: In Ex. 3.10(d), $d \mathbf{d} / d t$ should be $d\langle\mathbf{d}\rangle / d t$.
p. 111: In Ex. 3.11, subscripts $\mathbf{k}$ should be $k$ since we are in 1D.
p. 111: Ex. $3.12(\mathrm{~b})$ should ask to show that $\bar{\Omega}=\frac{1}{2} \epsilon_{i j} B_{\mu i} B_{\nu j} \Omega_{\mu \nu}$.
p. 111: In Ex. 3.14(b), chain_alt_bp should be chain_alt_bp.py .
p. 126: In the first paragraph, the sentence "Expand the set of functions to include the periodic images $\left|t_{n \mathbf{R}}\right\rangle$, and then construct $\left|\chi_{n \mathbf{k}}\right\rangle=\sum_{\mathbf{R}} e^{i \mathbf{k} \cdot \mathbf{R}}\left|t_{n \mathbf{R}}\right\rangle$ in analogy with Eq. (3.80b)" should be replaced by "Construct the band-projected Bloch-like states $\left|\chi_{n \mathbf{k}}\right\rangle=\sum_{m}\left|\psi_{m \mathbf{k}}\right\rangle\left\langle\psi_{m \mathbf{k}} \mid t_{n}\right\rangle$ at each $\mathbf{k}$, where $m$ runs over occupied Bloch eigenstates".
p. 127: In the line below Eq. (3.108), $\left\langle\tilde{\psi}_{n \mathbf{k}}\right| H\left|\tilde{\psi}_{n \mathbf{k}}\right\rangle$ should be $\left\langle\tilde{\psi}_{m \mathbf{k}}\right| H\left|\tilde{\psi}_{n \mathbf{k}}\right\rangle$.
p. 127: In Eq. (3.112), the factor $e^{-i \mathbf{k} \cdot \mathbf{R}}$ should be removed.
p. 128: In the first line of the last paragraph, "MLWfs" should be "MLWFs".
pp. 131-2: The ket $\left|\tilde{u}_{n k}\right\rangle$ should be changed to $\left|\bar{u}_{n k}^{\prime}\right\rangle$ in the third line of Sec. 3.6.3, the left-hand side of Eq. (3.123), and in the first and second lines below Eq. (3.123). Similarly, the ket $\left|\tilde{u}_{n k_{j}}\right\rangle$ should be changed to $\left|\bar{u}_{n k_{j}}^{\prime}\right\rangle$ on the left-hand side of Eq. (3.124), in the top line on p. 132, and in Eq. (3.125).
p. 145: In the last sentence of the first paragraph, $\left|\psi_{n \mathbf{k}}(\mathbf{r})\right|$ should be $\left|\psi_{n \mathbf{k}}(\mathbf{r})\right|^{2}$.
p. 149: In Eq. (4.25), the factor of $2 i$ should be replaced by -2 in the second line.
p. 151: In Eq. (4.29), the group velocity vector should be $\mathbf{v}_{\mathbf{k}}$ (i.e., in bold font).
p. 158: 4.2(b) should be replaced by

Show that $\left\langle u_{n \mathbf{k}}\right| \mathbf{v}_{\mathbf{k}}\left|u_{n^{\prime} \mathbf{k}}\right\rangle=\left\langle u_{n \mathbf{k}}\right| \mathbf{p}\left|u_{n^{\prime} \mathbf{k}}\right\rangle / m$ for different bands $n \neq n^{\prime}$.
p. 161: In Eq. (4.51), $d^{3} k$ should be replaced by $d^{3} \kappa$.
p. 171: In Eq. (4.69), the prefactor on the right-hand side should be $e^{i \mathbf{q} \cdot \boldsymbol{R}_{j}}$, not $e^{i \mathbf{q} \cdot \mathbf{r}_{j}}$.
p. 171: Two lines below Eq. (4.69), the text should read "... for a Hamiltonian $H_{\mathbf{q}}=$ $e^{-i \mathbf{q} \cdot \hat{\mathbf{r}}} H e^{i \mathbf{q} \cdot \hat{\mathbf{r}}}$, where $\hat{\mathbf{r}}$ is the coordinate operator; this plays a role ...".
p. 172: In Ex. 4.8, the displayed equation at the bottom of the page should be

$$
p_{j}=\frac{-e}{2 \pi} \bar{\phi}^{\left(\kappa_{j}\right)}
$$

and the last text line of the problem on p. 173 should read "as $p_{j}=(e / 2 \pi) \operatorname{Im} \ln \operatorname{det} M$, where".
p. 181, Ex. 4.9, the problem should have been posed in the context of the electronic polarization only (i.e., without the ionic contribution).
p. 190: In Eq. (4.93), the sin and cos should be interchanged so that it reads

$$
\begin{aligned}
\delta & =\delta_{0} \sin \lambda \\
\Delta & =\Delta_{0} \cos \lambda
\end{aligned}
$$

p. 190: Four lines below Eq. (4.93), $\delta$ should be $\delta_{0}$.
p. 203: In the last line of the caption of Fig. 5.1, " $\mathbf{b}_{1}$ and $\mathbf{b}_{1}$ " should be " $\mathbf{b}_{1}$ and $\mathbf{b}_{2}$ ". p. 208: In the 4th line from the top, " $\mathbb{Z}$ index" should be replaced by "Chern index $C^{\prime \prime}$.
p. 209: In the second line of Sec. 5.1.3, "Fig. 5.4(b)" should be "Fig. 5.4(d)".
p. 218: In Eq. (5.10), the sum over bands $n$ should be over all bands.
p. 219: In the 6th line of the 2 nd paragraph, $\rho_{x x}$ should be $\sigma_{x x}$.
p. 222: In the 8 th line of the 2nd paragraph, "It fact" should be "In fact".
p. 222: In the last paragraph, the sentence "In Ni the calculated value was only about $30 \%$ of the experimental one" should have the words "calculated" and "experimental" interchanged.
p. 224: In Exercise 5.4 part (c), last sentence, "in part (c)?" should be "in part (b)?".
p. 230: On 3rd line from the bottom, "imagin e" should be "imagine".
p. 246: In the caption of Fig. 5.17, primed and unprimed indices were interchanged. Thus, the last part of the caption should read:

$$
\begin{aligned}
& \text { (d) } \nu_{1}=1, \nu_{1}^{\prime}=0, \nu_{2}=1, \nu_{2}^{\prime}=0 \text {. (e) } \nu_{1}=0, \nu_{1}^{\prime}=1, \nu_{2}=0, \nu_{2}^{\prime}=1 \text {. (f) } \nu_{1}=0, \\
& \nu_{1}^{\prime}=1, \nu_{2}=1, \nu_{2}^{\prime}=0 .
\end{aligned}
$$

p. 247: In the caption of Fig. 5.18, " $E_{\mathrm{F} 1}$ and $E_{\mathrm{F} 1}$ " should be " $E_{\mathrm{F} 1}$ and $E_{\mathrm{F} 2}$ ".
p. 250: The sentence ending "approximately 0.3 eV ." in the last paragraph should be followed by "The experimental results are shown in Fig. 5.20."
p. 250: There is an erroneous reference to "Xia et al. (2009)" five lines from the bottom of the page. The citation should have been to "Zhang et al. (2009)".
p. 252: In Ex. 5.12, "Fig. 5.15(e-g)" should be "Fig. 5.15(e-h)".
p. 254: Six lines below Eq. (5.29), $\sqrt{f_{1}^{2}+f_{3}^{2}+f_{3}^{2}}$ should be $\sqrt{f_{1}^{2}+f_{2}^{2}+f_{3}^{2}}$.
p. 255: Ten lines above Eq. (5.31), " $2 \pi \chi$ " should be replaced by " $\chi$ ".
p. 257: The last part of the caption of Fig. 5.22 should read "(a) Positive chirality, $\chi=+1$. (b) Negative chirality, $\chi=-1$."
p. 257: Three lines above Eq. (5.34), the sentence ending "upper bands, respectively" should be extended with ", as shown in Fig. 5.22."
p. 260: The sign of $\chi$ is reversed in several of the lines below Eq. (5.36): in the $4^{\text {th }}$ and $11^{\text {th }}$ lines, $-\chi$ should be $\chi$; and in the $12^{\text {th }}$ line, $\chi=C_{a}-C_{b}$ should be $\chi=C_{b}-C_{a}$. (Here Chern indices are defined with respect to the outward normal, unlike in Eq. (5.34).)
p. 267: Ex. 5.20 should have asked to "show that the AHC is $\sigma_{\mathrm{AHC}}=-e^{2} k_{0} / h c$ ".
p. 282: In Eqs. (6.16-17), the "Im" should be moved inside the integral for the purposes of Ex. 6.2 on p. 285.
p. 282: Eq. (6.18) should have $d^{2} k$ inserted at the end.
p. 283: In Eq. (6.22), $M_{\text {DOS }}$ should be $\mathrm{M}_{\text {DOS }}$.
p. 290: In Fig. 6.5, $\theta$ should be replaced by $-\theta$ in the boxed equation at top right.
p. 293: Eq. (6.32) was missing a factor of $\mathcal{E}_{\nu}$; it should read

$$
\left|u_{n \mathbf{k}}\right\rangle=\left(1+i \hbar e \mathcal{E}_{\nu} T_{n \mathbf{k}}^{2} v_{\mathbf{k}, \nu}\right)\left|u_{n \mathbf{k}}^{0}\right\rangle
$$

p. 295: In Eq. (6.42), $-e$ should be $-e^{2}$ in the numerator just after the equal sign.
p. 296: In Eq. (6.46), $\widetilde{A}$ should be $\widetilde{A}_{\mu}$.
p. 302: In the third line from the bottom of the paragraph beginning "Conversely," "if is not" should be "if not".
p. 304: In the middle paragraph, bold $\mathbf{k}$ should be italic $k$ in two places.
p. 314: In the caption of Fig. 6.9, "electromagnetic" should be "magnetoelectric".
p. 328: On the 8th line from the bottom, matlib should be MATLAB.
p. 373: The following item was omitted from the list of references:

Zhang, H., Liu, C.-X., Qi, X.-L., Dai, X., Fang, Z., and Zhang, S.-C.
2009. Topological insulators in $\mathrm{Bi}_{2} \mathrm{Se}_{3}, \mathrm{Bi}_{2} \mathrm{Te}_{3}$ and $\mathrm{Sb}_{2} \mathrm{Te}_{3}$ with a single Dirac cone on the surface. Nat. Phys. 5, 438.
p. 383: In the index entry for "weak index", the final " $\mathbb{Z}_{2}$ " should be removed.

## To the reader:

If you discover additional errors, please email dhv@physics.rutgers.edu to report them.
I have also prepared a list of revisions intended to clarify the presentation and provide some missing details. As these go beyond the typical scope of errata, I have provided them separately at https://www.physics.rutgers.edu/~dhv/book-revisions.pdf. (If copy-pasting, replace the apparent tilde with a true tilde.)

