Physics 228 - Final Exam Solutions May 9, 2006 Prof. Coleman, Dr. Francis, Prof. Bronzan, Prof. Glashausser, and Prof. Madey

- 1. Which of the following quantities remains *unchanged* when light passes from a vacuum into a slab of glass with a 45° angle of incidence?
 - a) its frequency
 - b) its wavelength
 - c) its speed
 - d) its direction of travel
 - e) none of these

Solution:

The frequency remains unchanged. The speed changes because the index of refraction of glass is not 1.0, like the vacuum. Since the speed changes and the frequency remains fixed, the wavelength changes. The direction of travel changes according to Snell's law. 2. A converging and a diverging lens, each with a focal length of 30 cm, are arranged so that they are separated by 60 cm. If a candle is placed 90 cm to the left of the converging lens, where is the image produced by the diverging lens?



- a) 30 cm to the right of the diverging lens
- b) 10 cm to the left of the diverging lens
- c) 18 cm to the left of the diverging lens
- d) 30 cm to the left of the diverging lens
- e) 90 cm to the right of the diverging lens

- 3. In a Young's double-slit experiment, light of wavelength 500 nm illuminates two slits which are separated by 1 mm. The separation between adjacent bright fringes on a screen 5 m from the slits is:
 - a) 0.10 cm b) 0.50 cm c) 1.0 cm
 - d) 0.05 cm e) **0.25 cm**

Solution



4. A glass (n = 1.6) lens is coated with a thin film (n = 1.3) to minimize reflection of certain incident light. If $\lambda_{air} = 500$ nm is the wavelength of the light in air, the least film thickness is:

a)	78 nm		b) 96 nm	c)	$162~\mathrm{nm}$
d)	$200~\mathrm{nm}$	e)	250 nm		

We want to find the solution for the first *destructive* interference fringe. Since $n_{air} < n_{glass}$, there will be a phase shift at each reflection, so the relative phase shift between the light reflected from the film and the light reflected from the glass will be zero. This means we can use

$$2t = \frac{1}{2} \lambda_{film} = \frac{\lambda_{air}}{2 n_{film}}$$

which gives us $t = \lambda_{air}/(4 n_{film}) = 96$ nm

5. Consider two polarizers as shown. Light traveling along the z-axis passes through the pair. One of the polarizer is rotated with an angular frequency ω . The intensity of light transmitted through the pair, I_t, is periodic with frequency:



Solution:





i Light à bournatter with internety beat it possibile with frequency Zw. 6. A spacecraft in its own rest frame is shaped like an ellipse, with one axis twice as long as the other axis. How fast and in what direction should you move to make the craft appear circular?



Solution

An observer traveling with speed v in the y direction sees a contracted spacecraft in that direction. To make it appear circular, the contraction should be 50%. Thus γ must be 2.0, and $\beta = v/c$ must be 0.866. There is no contraction in the x direction.

7. A nucleus of mass M is at rest in the center-of-mass frame of reference. It spontaneously fissions into two pieces of equal mass m, each moving at speed 0.8c in opposite directions in the same center-of-mass system. What is the mass m of either fragment, in terms of M?

a) 0.18 M b) 0.83 M c) 0.79 M e) 0.50 M

d) 0.30 M



- The figure shows a schematic plot of intensity I of blackbody 8. radiation versus wavelength λ at temperature T_0 . When the temperature increases above T_0 the wavelength corresponding to the maximum intensity will:
 - a) increase

e)

- decrease b)
- increase initially, c) and eventually decrease
- d) decrease initially and eventually increase remains the same



- 9. The stopping potential for electrons ejected by 6.8×10^{14} -Hz electromagnetic radiation incident on a certain sample is 1.8 V. The kinetic energy, K, of the most energetic electrons ejected and the work function, ϕ , of the sample, respectively, are:
 - a) $K = 1.8 \text{ eV}, \quad \phi = 2.8 \text{ eV}$ b) $\mathbf{K} = \mathbf{1.8} \text{ eV}, \quad \phi = \mathbf{1.0} \text{ eV}$ c) $K = 1.8 \text{ eV}, \quad \phi = 4.6 \text{ eV}$ d) $K = 2.8 \text{ eV}, \quad \phi = 1.0 \text{ eV}$
 - e) $K = 1.0 \text{ eV}, \quad \phi = 4.6 \text{ eV}$

Solution:

The stopping potential and the maximum kinetic energy are related as $K_{max} = eV$, so that $K_{max} = 1.8$ eV. Using the photoelectric equation

$$eV = hf - \phi \quad \rightarrow \quad \phi = hf - K_{max}$$

gives us $\phi = 1.0$ eV.

10. In Compton scattering from stationary electrons, the largest amount of energy will be imparted to the electron when the photon is scattered through:

a) 0° b) 45° c) 90° d) **180^{\circ}** e) 270°

$$\sum_{i=1}^{n} e^{i\theta_{i}\theta_{i}} = \sum_{i=1}^{n} \sum_{i=1}^{n} e^{i\theta_{i}\theta_{i}} = \sum_{i=1}^{n} e^{i\theta_{i}\theta$$

11. The binding energy of an electron in the n=2 state in a hydrogen atom is about:

 a)
 3.4 eV b)
 13.6 eV
 c)
 10.2 eV

 d)
 1.0 eV
 e)
 27.2 eV

The total energy of the hydrogen atom in the n = 2 state is -3.4 eV (ic, -13.6/4). Thus it takes 3.4 eV to separate the electron in this state from the proton in the H atom, ic, its binding energy is 3.4 eV.

- 12. A ruby laser delivers a 1-ns pulse of 1.0 MW average power. If the light has a wavelength of 694.3 nm, how many photons are contained in the pulse?
 - a) 3.5×10^{24}
 - b) 5.5×10^{14}
 - $\dot{\mathrm{c})} \quad 3.5 \times 10^{15}$
 - d) 7.3×10^{15}
 - e) 1.7×10^{24}

Solution:

The energy in the pulse in $(1.0 \times 10^{\circ} \text{ J/s}) \times (1.0 \times 10^{-9} \text{s}) =$ 1.0 × 10⁻³ J. The energy carried by each photon is $hf = hc/\lambda$ = 2.87 × 10⁻¹⁹ J/photon. Thus the number of photons is 1.0 × 10⁻³ J)/(2.87 × 10⁻¹⁹ J/photon)= 3.49 × 10¹⁵ photons. 13. An electron is confined in an infinite, one dimensional, square potential well of width 0.200 nm.

 $V = \begin{cases} \infty \text{ for } x < 0 \text{ and } x > 0.200 \text{nm} \\ 0 \text{ for } 0 < x < 0.200 \text{nm} \end{cases}$

The energy of the ground state is:

a)	0.142 eV
b)	$1.50~{\rm eV}$
c)	$9.40 \ \mathrm{eV}$
d)	$13.6~{\rm eV}$
e)	54.4 eV

Solution



14. An electron is in a one-dimensional potential well of width L with zero potential energy in the interior and infinite potential energy at the walls. A graph of its wave function $\psi(x)$ versus x is shown. The value of quantum number n is:



Solution:

Since the wavefunction for a particle in a box is

$$\Psi_n(x) \propto \sin\left(rac{n\pi}{L}x
ight)$$

for n = 1, 2, 3, ..., we can determine n out by looking at the picture. One and one-half wavelengths are fit into the box, so the wavelength is $\lambda = 2L/3$. Since each half-wavelength corresponds to one energy level, this means the quantum energy number is 3. 15. If we think of an electron in a hydrogen atom as being a standing wave, then in the ground state of radius, a_0 , what is the electron's de Broglie wavelength?

a)
$$2\pi a_0$$

b) $h/(m^2 v^2)$
c) $a_0/(\hbar c)$
d) a_0
e) $\hbar/(mv)$

16. The maximum number of electrons that can be accommodated in an orbital with quantum number $\ell = 3$ is:

a) 2 b) 3 c) 7 d) 9 e) **14**

17. Sodium has an unpaired electron in its outer 4s subshell. If a large collection of sodium atoms are subjected to a 1 T magnetic field, what is the size of the split in the energy level of this electron?

- b) $5.8 \times 10^{-5} \text{ eV}$
- c) $1.2 \times 10^{-4} eV$
- d) $2.3 \times 10^{-4} \text{ eV}$
- e) $2.9 \times 10^{-5} \text{ eV}$

Solution

The energy of a spin magnetic moment in a magnetic field is $E(m_s) = g(e\hbar)/(2m)Bm_s$. The energy splitting $\Delta E = E(1/2) - E(-1/2)$ To two significant figures, $(2-1.00, \text{ so } \Delta E = (e\hbar B)/(2\pi m) = (1.85 \times 10^{-23} \text{ J})/(1.60 \times 10^{-19} \text{ J/eV}) = 1.16 \times 10^{-4} \text{ eV}$.

- 18. What is the correct ground-state electron configuration of Mg (Z = 12)?
 - a) $1s^22s^22p^63s^2$
 - b) $1s^2 2p^6 2d^4$
 - c) $1s^2 2s^2 2p^6 2d^2$
 - d) $1s^2 2s^2 3s^2 3p^6$
 - e) $1s^2 2s^2 3s^2 4s^2 2p^4$

- 19. The energy gap for silicon at 300 K is 1.14 eV. What is the wavelength of the lowest energy photon that will promote an electron from the valence band to the conduction band?
 - a) 1.14 nm
 - b) 263 nm
 - c) **1.09 µm**
 - d) 1.24 μm
 - e) 342 nm





a) 0 b) 5.0×10^{-9} c) 5.0×10^{-6} d) 5.0×10^{-3} e) **1**



21. Consider the nuclear reaction: ${}^{9}_{4}\text{Be} + \alpha \rightarrow n + {}^{12}_{6}\text{C}$

(Note: $M({}^{9}_{4}Be) = 9.012183u; M(\alpha) = 4.002603u;$ $M(n) = 1.008665u; M({}^{12}_{6}C) = 12.000000u)$

This reaction:

- a) cannot occur because it violates charge conservation.
- b) will not proceed unless the reactants have a total kinetic energy of 6.3 MeV.
- c) will release energy.
- d) is used in carbon dating.
- e) cannot proceed because it violates conservation of baryon number

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Solution:
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Total mass before the reaction is
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9.012183 + 4.002603 = 13.014786u
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Total mass after the reaction is

1.008665 + 12.000000 = 13.008665u

The extra mass before the reaction is converted into kinetic energy of the outgoing particles.

- 22. The half-life of radium is about 1600 years. If a rock initially contains 1 gram of radium, the amount left after 8000 years will be about:
 - a) 200 mg
 - b) 63 mg
 - c) **31 mg**
 - d) 16 mg
 - e) less than 1 mg
 - Solution

8000 years is 5 half lives. The amount of radium remaining after 8000 years is $2^{-5} \times 1$ g = 31 mg.

- 23. A large collection of nuclei is undergoing alpha decay. The rate of decay at any instant is:
 - a) proportional to the number of undecayed nuclei present at that instant
 - b) proportional to the time since the decays started
 - c) proportional to the time remaining before all have decayed
 - d) proportional to the half-life of the decay
 - e) a universal constant

olution

iven that the number of particles at a given time is

$$N(t) = N(0) \mathrm{e}^{-\lambda t}$$

the rate is

$$\frac{\mathrm{d}N(t)}{\mathrm{d}t} = -\lambda N(0)\mathrm{e}^{-\lambda t} = -\lambda N(t)$$

the rate of decay is proportional to the number of nucleipresent. 24. In a certain nuclear fission process,

$$_{0}^{1}n+_{92}^{235}U\rightarrow_{56}^{141}Ba+_{36}^{92}Kr+3_{0}^{1}n$$

Where: $m\binom{235}{92}U) = 235.043924 \text{ u}$ $m\binom{141}{56}Ba) = 140.9139 \text{ u}$ $m\binom{92}{36}Kr) = 91.8973 \text{ u}$ $m\binom{0}{1}n) = 1.008665 \text{ u}$

The energy released in this process is about:

a)	$86 { m MeV}$		b) 200 MeV	c)	$2.19~{\rm GeV}$
d)	$79 \mathrm{MeV}$	e)	$120 { m GeV}$		

Solution:

The energy released is going to be due to the mass difference between the original nucleus (and the catalyst neutron) and the final products:

$$Q = M_{LHS}c^2 - M_{RHS}c^2$$

$$= (m({}^{235}_{92}\text{U}) + m(\text{n}))c^2 - (m({}^{141}_{56}\text{Ba}) + m({}^{32}_{36}\text{Kr}) + 2m(\text{n})))$$

- $= (m(^{235}_{92}\text{U}) m(^{141}_{56}\text{Ba}) + m(^{92}_{36}\text{Kr}) + 2 m(n))c^2$
- = 200 MeV

25. Each of the following reactions is forbidden. Determine a conservation law that is violated for each reaction.

I. $\pi^- + p^+ \to p^+ + \pi^+$ II. $p^+ + p^+ \to p^+ + \pi^+$ III. $p^+ + \mu^+ \to p^+ + p^+ + \bar{\nu}_{\mu}$

- a) I. charge, II. baryon number, III. baryon number
- b) I. charge, II. lepton number, III. baryon number
- c) I. charge, II. baryon number, III. lepton number
- d) I. charge, II. lepton number, III. lepton number
- e) I. lepton number, II. baryon number, III. baryon number

Solution:



- 26. Consider the following reaction: $\pi^- + p \rightarrow K^o + (?)$; which in terms of quarks is: $(\bar{u}d) + (uud) \rightarrow (d\bar{s}) + (?)$ Which of the following is a candidate for the unknown product?
 - a) $\bar{p} = (\bar{u}\bar{u}\bar{d})$
 - b) $\bar{K}^o = (\bar{d}s)$ c) $\Xi^o = (uss)$
 - d) $\Sigma^- = (dds)$
 - e) $\Lambda^{\mathbf{o}} = (\mathbf{uds})$

Solution:



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? = uds = N°

27. A telescope has a diffraction grating with 750 slits per centimeter. Two different wavelengths of radiation, $\lambda_1 = 900$ nm and $\lambda_2 = 700$ nm fall on the grating. How far apart are their first maxima, in degrees?

a)	0°	b) $(1.5 \times 10^{-10})^{\circ}$	c)	0.0086°
d)	0.015°	e) 0.86 °		

Grating with 750 db \rightarrow distance between slits d. $\frac{1}{2}$ for distance $\frac{1}{2}$ is 22 x 10² fm. $\frac{1}{2}$ in 0 = ncd $\frac{1}{2}$ $0 = arcsin (\frac{nd}{2})$ 0 rances $(\frac{1}{2}, \frac{1}{2}, \frac{1}{2},$

- 28. Which of the following statements about the "Standard Model" of particle physics is *false*?
 - a) Bosons are the matter constituents. Fermions mediate the forces between particles.
 - b) The weak force is short-ranged because of the large mass of the Z and W particles.
 - c) Strangeness is not conserved by the weak interaction.
 - d) There are three known generations of leptons and quarks.
 - e) Hadrons are bound states of quarks, or antiquarks.

osons mediate the force between particles

29. Protons are accelerated in a cyclotron with internal field of 0.2 T. If beam exits at a radius of 2 m from the center of the cyclotron, what is the energy of the protons?

a) **7.67 MeV** b) 14 GeV c) 38.3 MeV d) 1.92 MeV e) 15.3 MeV

Solution:

The cyclotron angular frequency is

 $\omega = rac{eB}{m} = rac{(1.60 imes 10^{-19} \text{ C})(0.200 \text{ T})}{1.67 imes 10^{-27} \text{ kg}} = 1.92 imes 10^7 \text{ rad/sec.}$

The speed of the exiting protons is $v = \omega R = (1.92 \times 10^7 \text{ rad/sec})$ (2.00 m)= 3.84 × 10⁷ m/sec. The kinetic energy of the protons is

$$K = \frac{1}{2}mv^2 = \frac{1}{2}(1.67 \times 10^{-27} \text{ kg})(3.84 \times 10^7 \text{ m/sec})^2$$
$$= \frac{1.23 \times 10^{-12} \text{ J}}{1.60 \times 10^{-13} \text{ J/MeV}} = 7.67 \text{ MeV}.$$

30. An electron in an atom has quantum numbers n = 2, $\ell = 1$, $m_{\ell} = -1$, and $m_s = +1/2$. What is the magnitude of the *orbital* angular momentum of this electron?

a) 0 b) $-\hbar$ c) $\sqrt{3}\hbar/2$ d) $\hbar/2$ e) $\sqrt{2}\hbar$

n=2, L=1, m2=-L, m2=+L Orbitel angular momentum L= VI(L+1) to (tere, L=VI(L+1) to L=V2 to