Physics 227 – Final Exam
Tuesdya, December 20, 2016, 4:00 - 7:00 PM
CAC Gym (A-J), CAC Gym Annex (K-R) and
Scott Hall 135 (S-Z)

$\Rightarrow$ [box] $\Leftarrow$

Your **exam code**

SIGN HERE

1. Use a #2 pencil to mark entries on the answer sheet. *Enter the following ID information now, before the exam starts.*
2. **In the section labeled NAME (Last, First, M.I.) enter your last name, then fill in the empty circle for a blank, then enter your first name, another blank, and finally your middle initial.**
3. **Under STUDENT # enter your 9-digit RUID Number.**
4. **Under CODE enter the exam code given above.**
5. Enter 227 under COURSE. You do not need to write anything else on the answer sheet for now, but you may continue to read the instructions.
6. During the exam, you are allowed three (3) handwritten sheets of paper, 8.5 x 11 inches in size, handwritten on both sides. NO Calculators. NO Cell phones. NO smart watches.
7. The exam consists of 30 multiple-choice questions. For each multiple-choice question mark only **ONE** answer. There is no deduction of points for an incorrect answer, so even if you cannot work out the answer to a question, you should make an educated guess.
8. If you have questions or problems during the exam, you may raise your hand and a proctor will assist you. We wil provide the value of physical constants that are needed. It is your responsibility to know the relevant equations.
9. You are not allowed to help any other student, ask for help from anyone but a proctor, change your seat without permission from a proctor or use any electronic device. Doing so will result in a zero score for the exam.
10. **When you are done with the exam, show your student ID to a proctor, hand in only this cover sheet and your answer sheet.**
11. **Please sign above by the name sticker to indicate that you have read and understood these instructions.**

Possibly useful constants:
$\epsilon_0 = 1/\mu_0 c^2 = 8.85 \times 10^{-12}$ C^2/N·m^2
$k = 1/4\pi\epsilon_0 = 8.99 \times 10^9$ N·m^2/C^2
$\mu_0 = 4\pi \times 10^{-7}$ T·m/A $= 12.57 \times 10^{-7}$ T·m/A
$c =$ speed of light $= 3.00 \times 10^8$ m/s
$-q_{electron} = q_{proton} = 1.602 \times 10^{-19}$ C
$m_{electron} =$ electron mass $= 9.11 \times 10^{-31}$ kg
$m_{proton} =$ proton mass $= 1.67 \times 10^{-27}$ kg
1 eV $= 1.602 \times 10^{-19}$ J

Circumference of a circle $=2\pi r$; area of a circle is πr^2
Surface area of a sphere $= 4\pi r^2$; Volume of a sphere $= \frac{4}{3}\pi r^3$
Surface area of a cylinder $= 2\pi rh + 2\pi r^2$; Volume of cylinder $= \pi r^2 h$
$\sin(0°)= \cos(90°) = 0$
$\sin(90°)= \cos(0°) = 1$
$\sin(30°)= \cos(60°) = 1/2$
$\sin(60°)=\cos(30°) = \sqrt{3}/2$
$\sin(45°)= \cos(45°) = \sqrt{2}/2$
$\tan(30°) = 1/\sqrt{3}$
$\tan(60°) = \sqrt{3}$
$\tan\theta=\sin\theta/\cos\theta$
$\cos\theta = 1/\sqrt{(1 + \tan^2\theta)}$

$$\frac{d}{dx}x^n = nx^{n-1}$$

$\int x^n dx = \frac{1}{n+1}x^{n+1}$ except when $n = -1$. For $n = -1$, $\int dx/x = \ln x$

$\frac{d}{dx}\sin(ax) = a\cos(ax)$

$\frac{d}{dx}\cos(ax) = -a\sin(ax)$

$\int \sin(ax)dx = -\cos(ax)/a$
$\int \cos(ax)dx = \sin(ax)/a$

Some metric prefixes:
f = femto = 10^{-15}
p = pico = 10^{-12}
n = nano = 10^{-9}
μ = micro = 10^{-6}
m = milli = 10^{-3}
k = kilo = 10^3
M = mega = 10^6
G = giga = 10^9

1. The electric field for a plane electromagnetic wave in vacuum is given by $E = 2100$ (N/C) $\times \sin[-0.6$ m$^{-1} z + (0.01$ rad/s$)t]$ $\hat{x}$. In what direction does the wave propagate?

    a) The wave propagates in the $+x$ direction.
    b) The wave propagates in the $-z$ direction.
    c) The wave propagates in the $+z$ direction.
    d) The wave propagates in the $-x$ direction.
    e) The wave propagates in the $+y$ direction.

2. The intensity of a planar electromagnetic wave is $I = 2$ W/m^2. What is the maximum value of the magnetic field B of this wave?

    a) $B = 2\mu_0$ in units of T
    b) $B = 2\epsilon_0$ in units of T
    c) $B = 2/c$ in units of T
    d) $B = (2\mu_0/c)^{1/2}$ in units of T
   e) $B = 2(\mu_0/c)^{1/2}$ in units of T

3. A toroidal inductor is created when a long solenoid that is much longer than its radius is bent into a circle so that its ends meet. (Its external shape is then that of a very skinny doughnut.) The solenoid cross sectional area is A, its length is D and it is wound with N turns of wire. What is the inductance L of this toroidal inductor?

    a) $L = \mu_0 N^2 A / 2\pi D$
    b) $L = \mu_0 N^2 A / D^2$
    c) $L = \mu_0 N^2 A / D$
    d) $L = \mu_0 N A / D$
    e) $L = \mu_0 N A / 2\pi D$

4. A small conducting spherical shell with inner radius a and outer radius b is concentric with a larger conducting spherical shell with inner radius c and outer radius d. The inner shell has a total charge $+2q$, and the outer shell has a total charge $-2q$. What is the total charge Q_1 on the inner surface of the large shell and the total charge Q_2 on the outer surface of the large shell?

    a) $Q_1 = +2q$ and $Q_2 = +2q$
    b) $Q_1 = -2q$ and $Q_2 = -2q$
    c) $Q_1 = +2q$ and $Q_2 = 0$
    d) $Q_1 = -2q$ and $Q_2 = 0$
    e) $Q_1 = 0$ and $Q_2 = -2q$
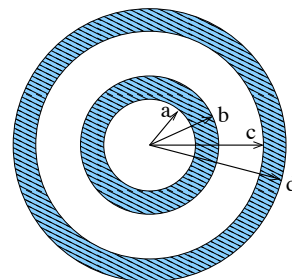
5. In the figure, at the top is a charge $+q$ and you are given 2 outer charges $-3Q$ and an inner charge $+Q$. At what angle θ is the net force F on the positive charge $+q$ at the top equal to zero? (Assume $0° \leq \theta \leq 90°$.)

a) The force F can never be equal to zero.
b) $F = 0$ when $\theta = 0°$.
c) $F = 0$ when $\theta = 90°$.
d) $F = 0$ when $\sin \theta = 1/6$.
e) $F = 0$ when $\cos \theta = 1/6$.
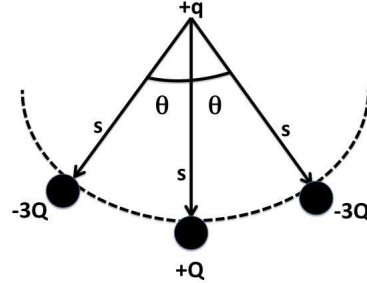
6. Consider the flux through the Gaussian cylinder shown in the figure, with the top and bottom surfaces labeled A and C, respectively, and the curved side is surface B. If $\Phi_A = -10$ Nm^2/C and $\Phi_C = +2$ Nm^2/C, what is Φ_B?

a) Not enough information is provided to determine Φ_B.
b) $\Phi_B = +8$ Nm^2/C
c) $\Phi_B = -8$ Nm^2/C
d) $\Phi_B = +12$ Nm^2/C
e) $\Phi_B = -12$ Nm^2/C

7. A circular conducting ring with radius r_0 lies in the xy-plane in a region of a uniform magnetic field $B(t) = B_0[1 - 3t^2 + 2t^3]\hat{k}$ where B_0 is constant. What is the magnitude of the induced EMF ε in the ring?

a) $\varepsilon = B_0[-6t + 6t^2]$
b) $\varepsilon = $ zero
c) $\varepsilon = B_0\pi r_0^2[-6t + 6t^2]$
d) $\varepsilon = 2B_0\pi r[-6t + 6t^2]$
e) $\varepsilon = B_0\pi r_0^2[1 - 3t^2 + 2t^3]$

8. The electric field E of an electromagnetic wave traveling in the positive x direction is illustrated in the figure. For the magnetic field, what are the direction and the phase relative to the electric field at a point where the electric field is in the negative y direction?
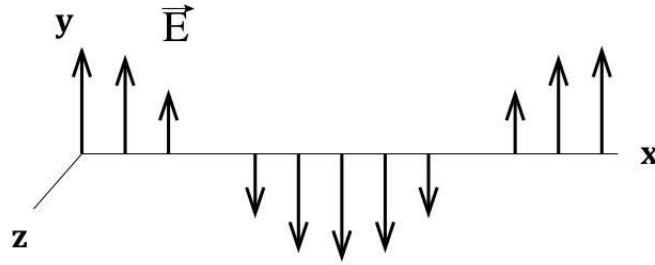

a) The $\vec{B}$ field is in the $-z$ direction and in phase with the $\vec{E}$ field.
b) The $\vec{B}$ field is in the $+z$ direction and 90° out of phase with the $\vec{E}$ field.
c) The $\vec{B}$ field is in the $-z$ direction and 90° out of phase with the $\vec{E}$ field.
d) The $\vec{B}$ field is in the $+z$ direction and in phase with the $\vec{E}$ field.
e) The $\vec{B}$ field is in the $+y$ direction and in phase with the $\vec{E}$ field.

9. An electromagnetic wave in vacuum traveling in the $+x$ direction generated by a variable soure initially has an angular frequency ω and a maximum electric field E_{max} in the $+y$ direction. If the period of the wave is doubled, what could be the equation of the resulting magnetic field component of the wave?

a) $\vec{B} = (cE_{max}) \cos(kx/2 - \omega t/2) \hat{z}$
b) $\vec{B} = (E_{max}/c) \cos(kx - \omega t) \hat{x}$
c) $\vec{B} = (E_{max}/c) \cos(kx/2 - \omega t/2) \hat{y}$
d) $\vec{B} = (E_{max}/c) \cos(kx/2 - \omega t/2) \hat{z}$
e) $\vec{B} = (cE_{max}) \cos(kx - \omega t/2) \hat{y}$

10. A current of 4.0 A is running through a series LR circuit containing a 2.0 Ω resistor and a 10 mH inductor. If the emf driving the current is suddenly switched off, which expression can be used to calculate the time it takes for the current to drop down to 1.0 A?

   a) $I = I_0 e^{-t/\tau}$ where $I_0 = 4.0$ A and $\tau = 20$ ms.
   b) $I = I_0 e^{-t/\tau}$ where $I_0 = 1.0$ A and $\tau = 5$ ms.
   c) $I = I_0 e^{-t/\tau}$ where $I_0 = 4.0$ A and $\tau = 5$ ms.
   d) $I = I_0(1 - e^{-t/\tau})$ where $I_0 = 4.0$ A and $\tau = 5$ s.
   e) $I = I_0 e^{-t/\tau}$ where $I_0 = 4.0$ A and $\tau = 5$ s.

11. In the figure, which is the correct expression for the time dependence of the charge q in an $R-C$ circuit with EMF V when the capacitor is charging?

   a) $q = Q_f(1 - \exp(-t/\tau))$ where $\tau = 1/RC$ and $Q_f = CV$
   b) $q = Q_f(1 - \exp(-t/\tau))$ where $\tau = RC$ and $Q_f = CV$
   c) $q = Q_f(\exp(-t/\tau))$ where $\tau = RC$ and $Q_f = V/C$
   d) $q = Q_f(\exp(-t/\tau))$ where $\tau = 1/RC$ and $Q_f = V/C$
   e) $q = Q_f(1 - \exp(-t/\tau))$ where $\tau = RC$ and $Q_f = V/C$
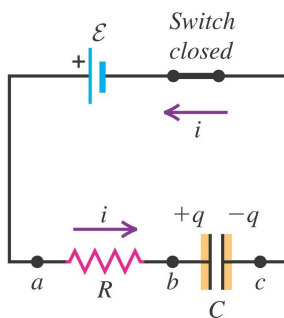
12. Consider a source charge $Q = +5$ C, fixed in place at the origin that creates an electric field in the surrounding region. You bring a small test charge $q = -5\mu$C, from infinite distance to a distance $r = 5$ meters from the source charge. How much work W is done by the electric field on the test charge in bringing the test charge from infinite distance to a distance r away from the source charge? [Answer in terms of $k = 1/(4\pi\epsilon_0)$]

   a) $W = + k(5 \times 10^{-6})$ J
   b) $W = - k(5 \times 10^{-6})$ J
   c) $W = + k(1 \times 10^{-6})$ J
   d) $W = - k(1 \times 10^{-6})$ J
   e) $W = + k(25 \times 10^{-6})$ J

13. A cylindrical wire has a resistance R_1 and resistivity ρ. If its length and diameter are BOTH cut in half, what will be its resistance R_2?

   a) $R_2 = R_1$
   b) $R_2 = 4R_1$
   c) $R_2 = R_1/4$
   d) $R_2 = R_1/2$
   e) $R_2 = 2R_1$

14. Point charges $q_1 = -5$ nC and $q_2 = +5$ nC are separated by a distance $d = 1.0$ mm, forming an electric dipole. The charges are in a uniform electric field whose direction has an angle of $\theta = 30°$ with the line connecting the charges. If the torque exerted on the dipole has magnitude $\tau = 10 \times 10^{-9}$ N·m, what is the magnitude of the electric field E?

   a) $E = 4000$ N/C
   b) $E = 4000\sqrt{3}$ N/C
   c) $E = 2000$ N/C
   d) $E = 2000\sqrt{3}$ N/C
   e) $E = 4$ N/C

15.   The figure displays a series circuit containing a resistor of resistance R and an inductor of inductance L connected to a source of EMF ε with negligible internal resistance. The wires are also assumed to have zero resistance. Immediately after the switch is closed, which of the following are correct for the voltage drop across the inductor V_L, the voltage drop across the resistor, V_R, and the initial current $I_{initial}$?
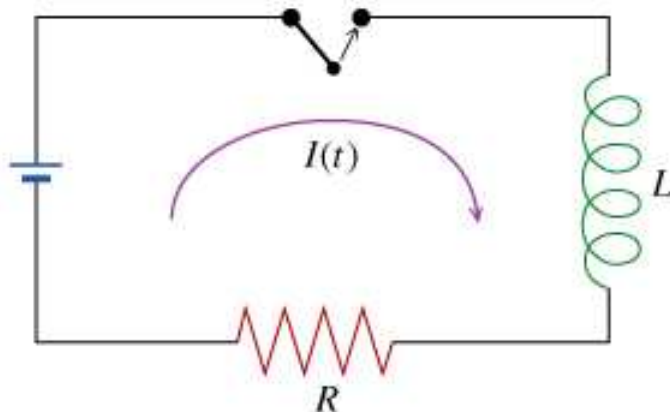

a) $V_L = \varepsilon$, $V_R = \varepsilon$, $I_{initial} = \varepsilon/R$
b) $V_L = \varepsilon$, $V_R = \varepsilon$, $I_{initial} = 0$
c) $V_L = \varepsilon$, $V_R = 0$, $I_{initial} = 0$
d) $V_L = \varepsilon/2$, $V_R = \varepsilon/2$, $I_{initial} = \varepsilon/R$
e) $V_L = 0$, $V_R = \varepsilon$, $I_{initial} = \varepsilon/R$

16.   Which of the following is TRUE?

a) We can think of the energy stored in a parallel plate capacitor as being stored in the electric field between the plates.
b) Energy cannot be stored in a vacuum.
c) Electric fields require a dielectric, and do not develop in a perfect vacuum.
d) The electric field $\vec{E} = \vec{F}_0/q_0$ measured at a point in space diverges as the test charge q_0 is sent to zero.
e) In general, electric field and electric potential are directly proportional to one another.

17.   A plane sinusoidal electromagnetic wave in air has an electric field ampli-
tude of E_0. What average force F does this radiation exert on a totally
absorbing surface with area A perpendicular to the direction of propaga-
tion?

    a) $F = $ zero, because area is perpendicular to the direction of propa-
gation.
    b) $F = \frac{1}{2}\epsilon_0 E_{max}^2 A$
    c) $F = \epsilon_0 E_{max}^2 A$
    d) $F = \frac{1}{2}\epsilon_0 E_{max} A$
    e) $F = \epsilon_0 E_{max} A$

18.   An inductor with $L = 10$ mH is connected across an ac source that has a
voltage amplitude $V_0 = 40$ V. What value for the frequency f of the source
results in a current amplitude of $I_0 = 4$ A?

    a) $f = 500/\pi$ Hz
    b) $f = 5/\pi$ Hz
    c) $f = 500$ Hz
    d) $f = 100/$ Hz
    e) $f = 100/\pi$ Hz

19.   An air-filled parallel-plate capacitor has plate area A and plate separation
d. The capacitor is connected to a battery that creates a constant voltage
V. The energy stored in the capacitor is U_1. While the capacitor stays
connected to the battery, a dielectric plate with thickness d and dielectric
constant K, is slowly moved into the capacitor until it fills only the left half
of the space between the plates. What is the new energy U_2 now stored in
the capacitor?

    a) $U_2 = U_1/2$
    b) $U_2 = KU_1$
    c) $U_2 = (K+1)U_1$
    d) $U_2 = (K+1)U_1/2$
   e) $U_2 = U_1/[2(K+1)]$

20. A very long, hollow, thin-walled conducting cylindrical shell (like a pipe) of radius R carries a current along its length uniformly distributed throughout the thin shell. Which one of the graphs shown in the figure most accurately describes the magnitude B of the magnetic field produced by this current as a function of the distance r from the central axis?
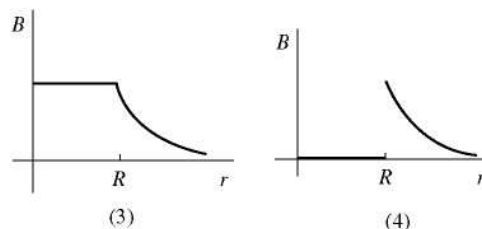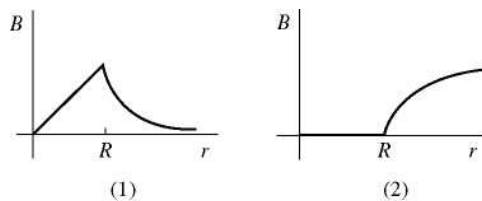

a) Graph (3) best represents B as a function of r.
b) Graph (5) best represents B as a function of r.
c) Graph (4) best represents B as a function of r.
d) Graph (2) best represents B as a function of r.
e) Graph (1) best represents B as a function of r.
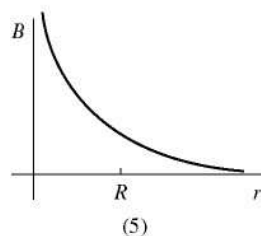
21. A light bulb is connected in the circuit shown in the bottom figure with the switch S open and the capacitor uncharged. The battery has no appreciable internal resistance. Which one of the following graphs best describes the brightness $B(t)$ of the bulb as a function of time t after closing the switch?

B
1

t

B
2

t

B
3

t

B
4

t

B
5

t

Bulb
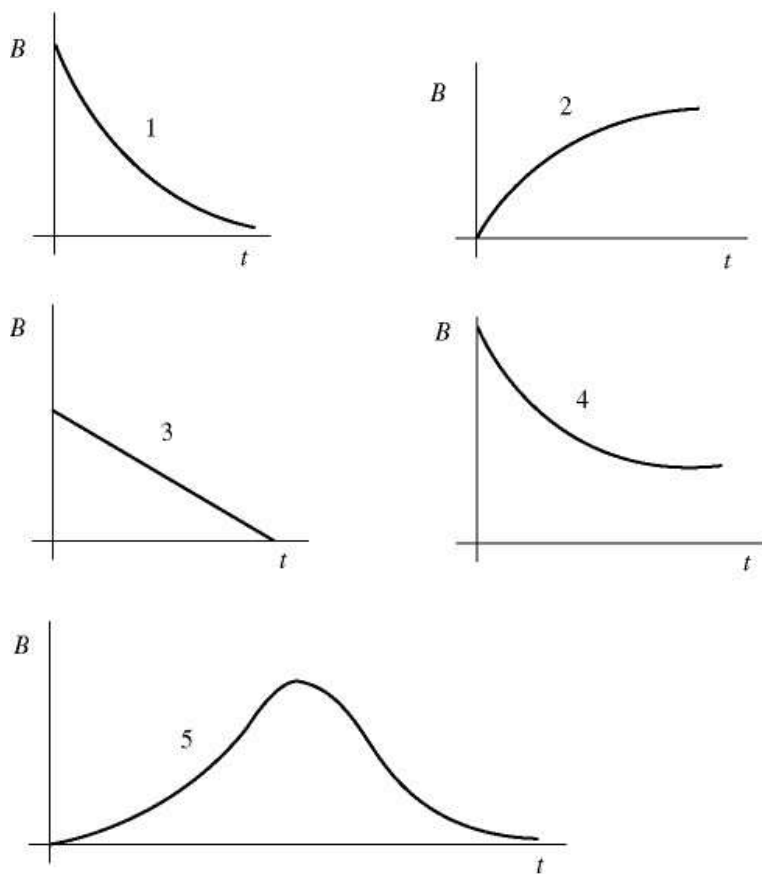
a) Graph **3** best describes the brightness $B(t)$.

b) Graph **1** best describes the brightness $B(t)$.

c) Graph **5** best describes the brightness $B(t)$.

d) Graph **4** best describes the brightness $B(t)$.

e) Graph **2** best describes the brightness $B(t)$.

R

C

S
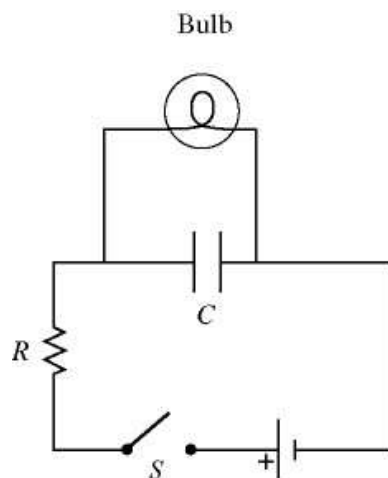
22. The electric potential as a function of x is shown in the graph in the figure. What statement about the electric field is TRUE?
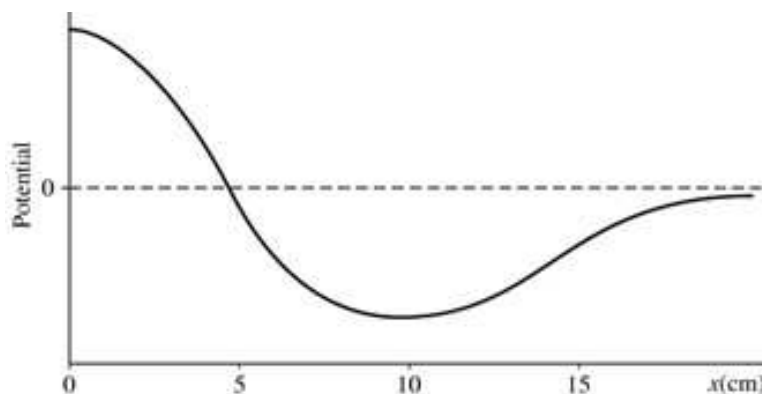
a) The electric field is zero at $x = 0$, its magnitude is at a maximum at $x = 5$ cm, and the electric field is directed to the right at $x = 5$ cm.
b) The electric field is zero at $x = 0$, its magnitude is at a maximum at $x = 5$ cm, and the electric field is directed to the left at $x = 5$ cm.
c) The electric field is zero at $x = 0$ cm, its magnitude is at a maximum at $x = 15$ cm, and the electric field is directed to the right at $x = 15$ cm.
d) The electric field is zero at $x = 5$ cm, its magnitude is at a maximum at $x = 0$, and the electric field is directed to the right at $x = 0$.
e) The electric field is zero at $x = 10$, its magnitude is at a maximum at $x = 5$ cm, and the electric field is directed to the left at $x = 5$ cm.

23. At what rate would the current in a 100-mH inductor have to change to induce an EMF of magnitude 100 V in the inductor?

a) The rate should be 10 A/s
b) The rate should be 1000 A/s
c) The rate should be 0.1 A/s
d) The rate should be 1 A/s
e) The rate should be 100 A/s

24. You are given a reactance of an inductor $X_L=100$ Ω, reactance of a capacitor $X_C=10$ Ω, and frequency $= 100$ Hz. Which of the following is correct?

a) The inductance $L = 2/\pi$ H
b) The capacitance $C = 5/\pi$ F
c) The inductance $L = 1$ H
d) The capacitance $C = 10^{-3}$ F
e) The capacitance $C = 10^{-3}/2\pi$ F

25. You are given four series $R - L - C$ circuits where R is the resistance, L is the inductance and C is the capacitance of the circuits. Each circuit is driven at its resonance frequency by a 1000 V_{rms} AC power supply. Rank these circuits on the basis of their maximum current I_{max}.

Circuit A: $R = 1000$ Ω, $C = 0.5$ μF, $L = 2.0$ H
Circuit B: $R = 500$ Ω, $C = 4.0$ μF, $L = 1.0$ H
Circuit C: $R = 500$ Ω, $C = 1.0$ μF, $L = 1.5$ H
Circuit D: $R = 2000$ Ω, $C = 4.0$ μF, $L = 1.0$ H

   a) $I_D = I_A > I_C > I_B$
   b) $I_C > I_B > I_D > I_A$
   c) $I_B = I_C > I_A > I_D$
   d) $I_A > I_B > I_C > I_D$
   e) $I_D > I_A > I_B = I_C$

26. A charge is accelerated from rest through a potential difference V_1 and then enters a uniform magnetic field oriented perpendicular to its path. The field deflects the particle into a circular arc of radius R_1. If the accelerating potential is tripled to $V_2 = 3V_1$, what will be the radius R_2 of the circular arc?

   a) $R_2 = R_1/\sqrt{3}$
   b) $R_2 = 9R_1$
   c) $R_2 = R_1\sqrt{3}$
   d) $R_2 = 3R_1$
   e) $R_2 = R_1/9$

27. The figure shows three long, parallel current-carrying wires. The magnitudes of the currents are equal and their directions are indicated in the figure. Which of the arrows drawn near the wire carrying current I_1 correctly indicates the direction of the magnetic force acting on that wire?
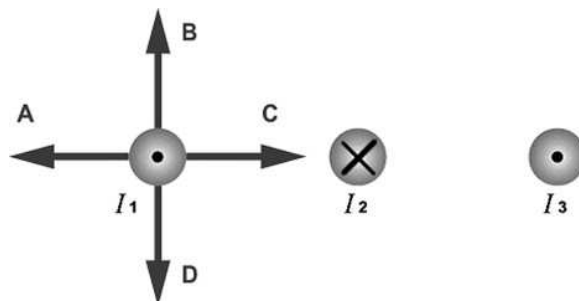

a) The magnetic force on the wire carrying current I_1 is zero.
b) The direction of the magnetic force on the wire carrying current I_1 is in direction A.
c) The direction of the magnetic force on the wire carrying current I_1 is in direction C.
d) The direction of the magnetic force on the wire carrying current I_1 is in direction B.
e) The direction of the magnetic force on the wire carrying current I_1 is in direction D.

28. The flux of the magnetic field in the square wire loop on the left varies as a function of time as shown in the figure on the right. Which dependence(s) of $\Phi_B(t)$ correspond(s) to the largest magnitude of the induced current $I_{induced}$.
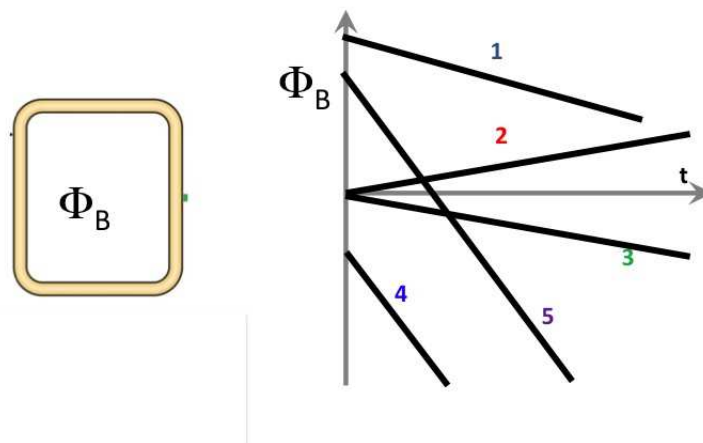
a) The magnitude of $I_{induced}$ is largest for curve 5.
b) The magnitude of $I_{induced}$ is largest for curve 1.
c) The magnitude of $I_{induced}$ is largest for curve 2 and curve 3.
d) The magnitude of $I_{induced}$ is largest for curve 4 and curve 5.
e) The magnitude of $I_{induced}$ is largest for curve 4.

29. What is the equivalent resistance (measured in Ω) of the segment of a circuit in the figure if $R_1 = 2R$ and $R_2 = R_3 = R_4 = R$?
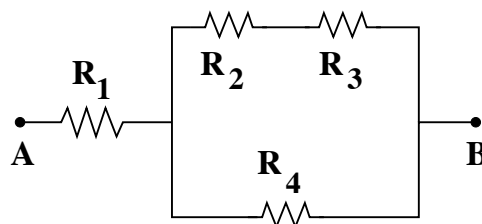
a) $5R/3$
b) $8R/3$
c) $3R/8$
d) $5R$
e) $5R/2$

30. Two coils are close to each other, with one connected to a current source which produces a current of $I_1(t) = 3t^2 + 5$ amps, where t is expressed in seconds. If at time $t = 3$ seconds the voltage $V_2 = 0.18$ V, what is the mutual inductance M of the two coils?

$I_1(t)$

a) $M = 5.6$ mH
b) $M = 10$ mH
c) $M = 20$ mH
d) $M = 30$ mH
e) $M = 60$ mH

V_2