

# **Buried Higgs**

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with  
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## Preview

- Found a SUSY model, where:
  - Weird higgs decays automatic
  - Higgs could be below “LEP bound”
  - No little hierarchy
  - Lots of new particles at LHC, but higgs buried in QCD background
  - Could discover “fake higgs”

# Outline

- The little hierarchy of the MSSM and pGB higgses
- The simplest supersymmetric pGB higgs: 5 Goldstones  $h + \eta$
- $h$ -decays and  $\eta$  decays: higgs could be  $< 114$  GeV
- A “flipped” matter content: charming higgs

## Little hierarchy in the MSSM

- SUSY solves hierarchy problem, but
  - Log divergences remain
  - Need a large  $\Delta\lambda$  to push higgs above 114 GeV
- Generic Higgs potential

$$V(H_u, H_d) = (m_{H_u}^2 + \mu^2)|H_u|^2 + (m_{H_d}^2 + \mu^2)|H_d|^2 - B\mu(H_u H_d + \text{h.c.}) + \frac{g^2}{2}(H_u^\dagger \vec{\tau} H_u + H_d^\dagger \vec{\tau} H_d)^2 + \frac{g'^2}{2}(H_u^\dagger H_u - H_d^\dagger H_d)^2$$

- For minimum we need

$$M_Z^2 = 2 \left( \frac{m_{H_d}^2 - m_{H_u}^2 \tan^2 \beta}{\tan^2 \beta - 1} - \mu^2 \right)$$

- For large  $\tan \beta$   $M_Z^2 \sim -2m_{H_u}^2$

$$m_{H_u}^2 = m_0^2 - \frac{3\lambda_t^2 m_{\tilde{t}}^2}{4\pi^2} \log \frac{\Lambda_{UV}^2}{m_{\tilde{t}}^2}$$

- But the expression for the Higgs mass is:

$$m_{Higgs}^2 = M_Z^2 + \frac{3m_t^2 \lambda_t^2}{4\pi^2} \log \frac{m_{\tilde{t}}}{m_t}$$

- To push Higgs mass above 114 GeV: need  $m_{\text{stop}} \gtrsim 1$  TeV, but then need 1% or less tuning for  $M_Z$

- Main idea: SUSY Higgs as pseudo-Goldstone boson (=super-little Higgs, doubly protected Higgs)

(Birkedal, Chacko, Gaillard; Chankowski, Falkowski, Pokorski, Wagner)

- A global symmetry broken at  $f \sim 500$  GeV produces Goldstones, softens Higgs potential further

- In these models higgs potential completely finite

$$m_{H_u}^2 = -\frac{3\lambda_t^2 m_{\tilde{t}}^2}{4\pi^2} \log \frac{f^2}{m_{\tilde{t}}^2}$$

- Fine tuning reduced

- BUT: global symmetry (presence of top partners) also reduced shift in quartic
- Usually VERY difficult to achieve  $m_{\text{Higgs}} > 114 \text{ GeV}$
- Models quite complicated (Berezhiani, Chankowski, Falkowski, Pokorski; Roy, Schmaltz; C.C., Marandella, Shirman, Strumia)
- Main new idea here: in simplest model (susy version of Schmaltz's simplest little Higgs) ad'l Goldstone  $\eta$  automatic
- $h \rightarrow \eta\eta$  decay can avoid LEP bounds, don't need to push quartic, can get simple natural model with interesting phenomenology

# Higgs sector and Goldstones

- Higgses:

(Same as Schmaltz simplest LH)

	$SU(3)_C$	$SU(3)_W$	$U(1)_X$
$\mathcal{H}_u, \Phi_u$	1	3	1/3
$\mathcal{H}_d, \Phi_d$	1	$\bar{3}$	-1/3

- Assume no  $\Phi\mathcal{H}$  terms in the superpotential:  $SU(3)_\Phi \times SU(3)_\mathcal{H}$  global symmetry

- One sector will get a VEV  $F \sim 10$  TeV

$$\langle \Phi_u \rangle^T = \langle \Phi_d \rangle = (0, 0, F/\sqrt{2})$$

- Embedding of hypercharge:  $Y = T_8/\sqrt{3} + X$ , where  $T_8 = 1/(2\sqrt{3}) \text{diag}(1, 1, -2)$



- Below F theory effectively MSSM with  $SU(3)_{\mathcal{H}}$  global symmetry
- $SU(3)$  breaking from  $\langle \mathcal{H} \rangle \sim f \sim 400 \text{ GeV}$
- The parameterization of the Higgses:

$$\mathcal{H}_u = e^{i\Pi/f} f \sin \beta \begin{pmatrix} 0 \\ 0 \\ 1 \end{pmatrix}, \quad \mathcal{H}_d = e^{-i\Pi/f} f \cos \beta \begin{pmatrix} 0 \\ 0 \\ 1 \end{pmatrix}$$

- Where  $\Pi$  is the pion matrix containing the 5 Goldstones:

$$\Pi = \begin{pmatrix} & | & H \\ \hline H^\dagger & | & \frac{\tilde{\eta}}{\sqrt{2}} \end{pmatrix}$$

- The Higgs fields  $H$  can be thought of as angles between the triplet VEVs  $\langle \Phi \rangle$  and  $\langle \mathcal{H} \rangle$ . Together  $SU(3) \times U(1) \rightarrow U(1)_{\text{QED}}$

- The result is:

$$\mathcal{H}_{u,d} = f_{u,d} \begin{pmatrix} \sin H/f \\ e^{\pm i\frac{\eta}{f}} \cos |H|/f \end{pmatrix}$$

- In terms of the uneaten fields  $\tilde{h}$  and  $\tilde{\eta}$  (before shifting VEVs)

$$\mathcal{H}_u = f \sin \beta \begin{pmatrix} 0 \\ \sin(\tilde{h}/\sqrt{2}f) \\ e^{i\tilde{\eta}/\sqrt{2}f} \cos(\tilde{h}/\sqrt{2}f) \end{pmatrix} \quad \mathcal{H}_d^T = f \cos \beta \begin{pmatrix} 0 \\ \sin(\tilde{h}/\sqrt{2}f) \\ e^{-i\tilde{\eta}/\sqrt{2}f} \cos(\tilde{h}/\sqrt{2}f) \end{pmatrix}$$

- After Higgs gets VEV

where  $v_{EW}=174$  GeV

we shift fields as usual

$$\langle \tilde{h} \rangle = \sqrt{2}\tilde{v}$$

with

$$v_{EW} = f \sin(\tilde{v}/f)$$

$$\tilde{h} = \sqrt{2}\tilde{v} + h, \quad \tilde{\eta} = \eta / \cos(\tilde{v}/f)$$

## $h \rightarrow \eta\eta$ vs. $h \rightarrow b\bar{b}$

- In order to make  $h \rightarrow \eta\eta$  the leading mode need to win over  $\lambda_b$ : not that hard, v/f suppression OK.

- The Goldstone kinetic term contains derivative interaction

$$\mathcal{L}_{pGB} \approx \frac{1}{2}(\partial_\mu \tilde{h})^2 + \frac{1}{2} \cos^2(\tilde{h}/\sqrt{2}f)(\partial_\mu \tilde{\eta})^2$$

- After shifting VEV get cubic interaction:

$$\mathcal{L}_{h\eta^2} \approx -h(\partial_\mu \eta)^2 \frac{\tan(\tilde{v}/f)}{\sqrt{2}f}$$

(Ideas suggested by Dermisek, Gunion; Chang, Fox, Weiner;...)

- The  $h \rightarrow \eta\eta$  rate is:

$$\Gamma_{h \rightarrow \eta\eta} \approx \frac{1}{64\pi} \left( 1 - \frac{v_{EW}^2}{f^2} \right)^{-1} \frac{m_h^3 v_{EW}^2}{f^4}$$

- Compare to the usual fermionic width with extra  $(1-v^2/f^2)$  suppression:

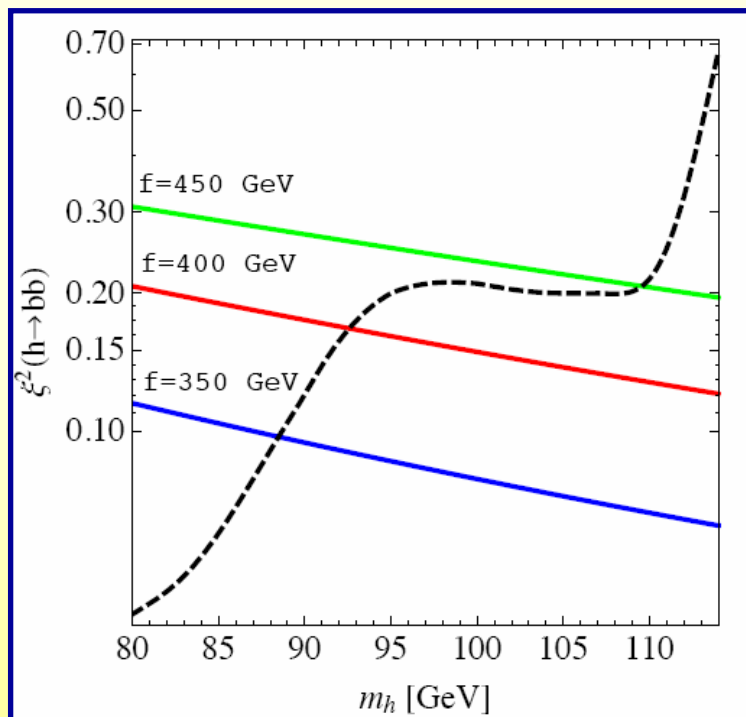
$$\Gamma_{h \rightarrow f\bar{f}} = \left( 1 - \frac{v_{EW}^2}{f^2} \right) \Gamma_{h \rightarrow f\bar{f}}^{SM} = c_{QCD} \frac{N_c}{16\pi} \left( 1 - \frac{v_{EW}^2}{f^2} \right) \frac{m_h m_f^2}{v_{EW}^2}$$

- Relevant quantity for suppression of the  $h \rightarrow b\bar{b}$  compared to SM is  $\xi^2$ :

$$\xi_{h \rightarrow b\bar{b}}^2 \equiv \frac{\sigma(e^+e^- \rightarrow Zh)}{\sigma_{SM}(e^+e^- \rightarrow Zh)} BR(h \rightarrow b\bar{b}) = \frac{\Gamma_{h \rightarrow b\bar{b}}^{SM}}{\Gamma_{h \rightarrow \eta\eta} + \left(1 - \frac{v_{EW}^2}{f^2}\right) \sum_f \Gamma_{h \rightarrow f\bar{f}}^{SM}} \left(1 - \frac{v_{EW}^2}{f^2}\right)^2$$

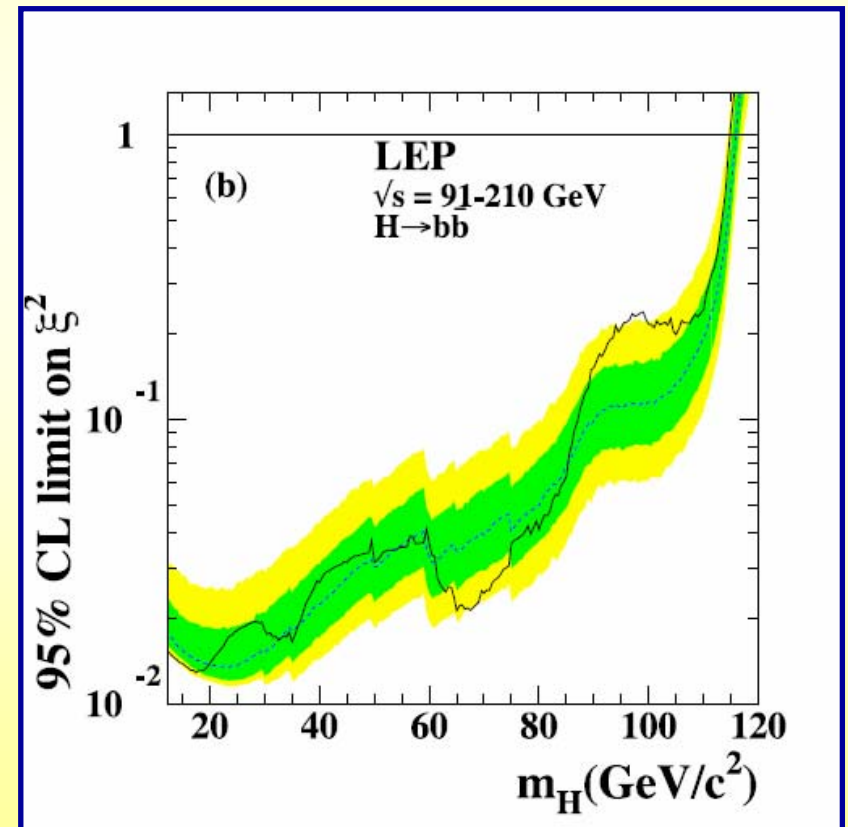
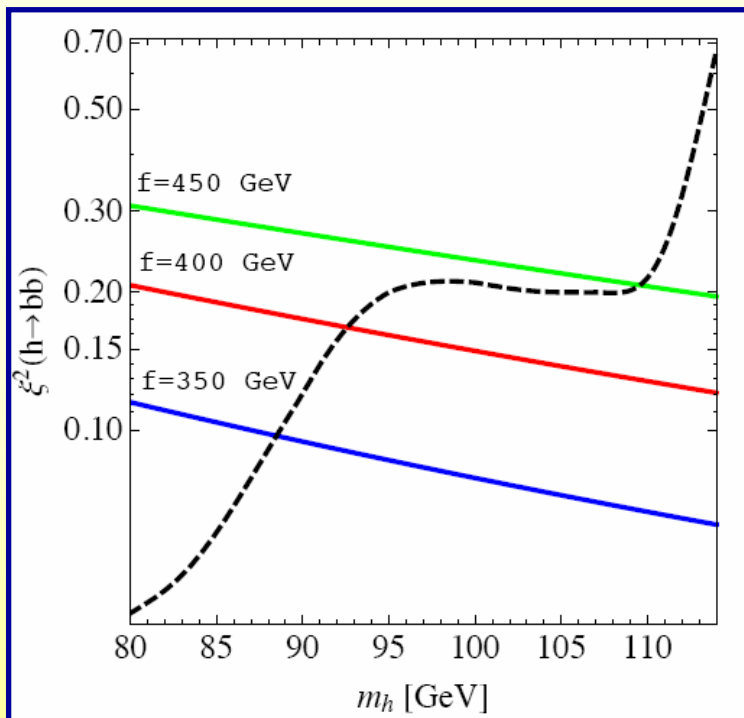
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The LEP bound

- To actually hide higgs at LEP, need to make sure  $\eta$  decays are allowed and weird, since bounds:

Decay channel	Limit (GeV)
$h \rightarrow b\bar{b}, \tau\bar{\tau}$	115
$h \rightarrow jj$	113
$h \rightarrow \gamma\gamma$	117
$h \rightarrow WW^*, ZZ^*$	110
$h \rightarrow \text{invisible}$	115
$h \rightarrow \eta\eta \rightarrow 4b$	110
$h \rightarrow \eta\eta \rightarrow 4\tau, 4c, 4g$	86
model indep.	82



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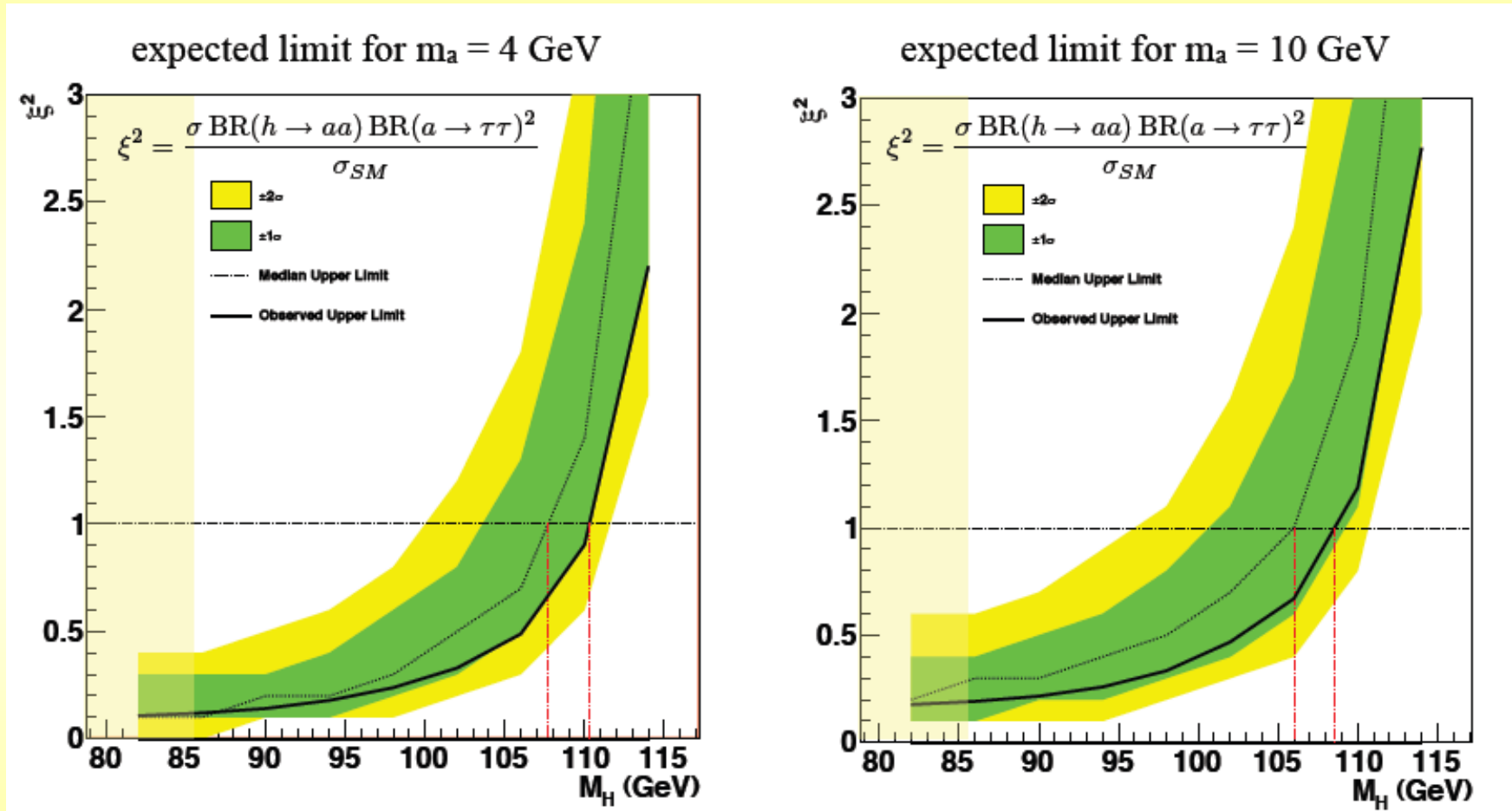
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New LEP  
result!

# ALEPH bound on $h \rightarrow 4\tau$ of order 105-110 GeV!



Talk by K. Cranmer on 11/3/09

(Cranmer, Yavin, Beacham, Spagnolo, ALEPH collab.)

- To actually hide higgs at LEP, need to make sure  $\eta$  decays are allowed and weird, since bounds:

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- To find out which case need fermion embeddings...

# The matter content and Yukawas

	$SU(3)_C$	$SU(3)_W$	$U(1)_X$
$Q = (t^Q, b^Q, \hat{b}^Q)$	3	3	0
$V = (b^V, t^V, \hat{t}^V)$	3	$\bar{3}$	1/3
$V_c = (b_c^V, t_c^V, \hat{t}_c^V)$	$\bar{3}$	3	-1/3
$t_c$	$\bar{3}$	1	-2/3
$b_c^{1,2}$	$\bar{3}$	1	1/3
$L_{1,2} = (\tau_{1,2}^L, \nu_{1,2}^L, \hat{\nu}_{1,2}^L)$	1	$\bar{3}$	-1/3
$E_c = (\nu_c^E, \tau_c^E, \hat{\tau}_c^E)$	1	$\bar{3}$	2/3
$\nu_c^{1,2,3}$	1	1	0

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•Why?????

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$\nu_c^{1,2,3}$	1	1	0

- Cancels anomalies
- Contains MSSM chiral generation
- Obtain from  $SU(6)$  matter content

- Quark Yukawas (including a  $\mu$ -term for  $VV_c$ ):

$$y_1 t_c V \Phi_u + y_2 \mathcal{H}_u V_c Q + \mu_V V V_c + y_{b1} \Phi_d Q b_c^1 + y_{b2} \mathcal{H}_d Q b_c^2$$

- Not the most general superpotential, could also add

$$\tilde{y}_1 t_c V \mathcal{H}_u + \tilde{y}_2 \Phi_u V_c Q + \tilde{y}_{b1} \mathcal{H}_d Q b_c^1 + \tilde{y}_{b2} \Phi_d Q b_c^2$$

- Original superpotential collective
- In top sector need  $y_1, y_2$  and  $\mu_V$  to break  $SU(3)_H$

$$m_t \sim y_1 y_2 \mu_V, \text{ corrections OK if } \mu_V < \text{TeV}.$$

- In bottom sector need  $y_{b1}$  and  $y_{b2}$  to break  $SU(3)_H$
- Since  $y_{b1} F$  is one of bottom masses, need  $y_{b1} \lesssim 0.1$  to avoid large logs in higgs mass



# Higgs potential, fine tuning

- Both  $f/F$  and  $v/f$  can be radiatively generated from Yukawa interactions
- $f$  generated due to potential for triplet  $\mathcal{H}_u$ :

$$m_{\mathcal{H}_u}^2 \approx -\frac{3y_2^2 \sin^2 \beta}{2\pi^2} M_{\text{soft}}^2 \log(\Lambda/M_T)$$
$$\lambda_{\mathcal{H}_u} \approx \frac{3y_2^4 \sin^4 \beta}{8\pi^2} \log((M_{\text{soft}}^2 + M_T^2)/M_T^2)$$

- Here  $m_T$  top partner mass

$$M_T = \sqrt{\mu_V^2 + \sin^2 \beta y_2^2 f^2}$$

- Generates “radion” mass

$$m_r^2 \sim 4\lambda_{\mathcal{H}_u} f^2$$

- Fine tuning from f/F hierarchy:

$$FT_3 = \frac{m_r^2/2}{|m_{\mathcal{H}_u}^2|} \sim \frac{y_2^2 f^2}{M_{soft}^2} \frac{\log \frac{M_{soft}^2 + M_T^2}{M_T^2}}{\log \frac{\Lambda^2}{M_T^2}}$$

- Similar to MSSM expression, except:
  - $m_r$  can be heavier than Higgs
  - $y_2$  can be bigger than  $y_t$
- Typical fine tuning 5-10%

- Usual MSSM fine tuning completely absent

$$FT_2 = \frac{m_h^2/2}{|\Delta m^2|}$$

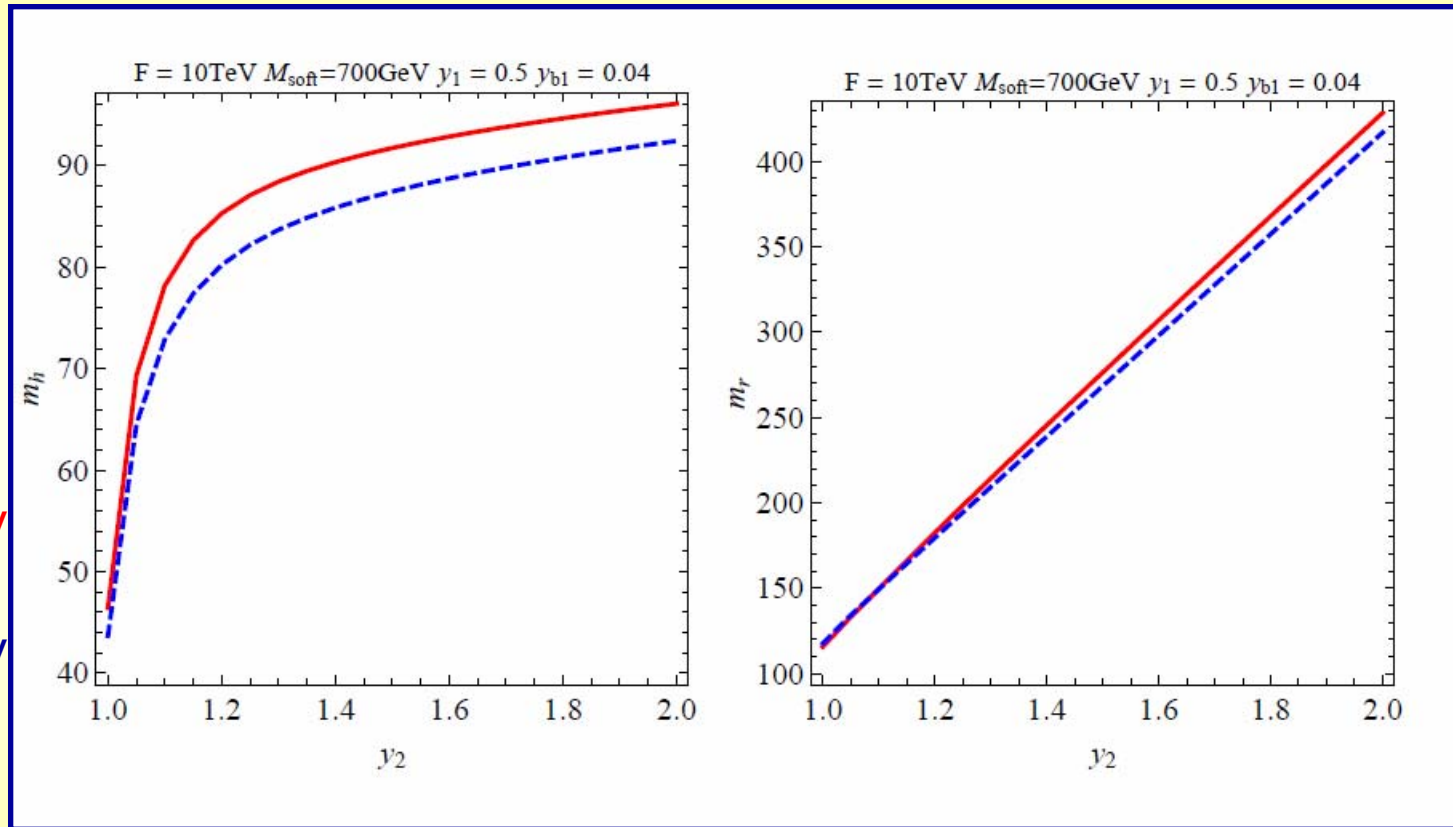
- Higgs mass parameter shift finite

$$\Delta m^2 \approx -\frac{3m_t^2}{8\pi^2 v_{EW}^2} \left[ M_T^2 \log \frac{M_{\text{soft}}^2 + M_T^2}{M_T^2} + M_{\text{soft}}^2 \log \frac{M_{\text{soft}}^2 + M_T^2}{M_{\text{soft}}^2} \right]$$

- Physical higgs mass:

$$m_h^2 = \left( 1 - \frac{v_{EW}^2}{f^2} \right) \left\{ m_Z^2 \cos^2(2\beta) + \frac{3m_t^4}{4\pi^2 v_{EW}^2} \left[ \log \left( \frac{M_{\text{soft}}^2 M_T^2}{m_t^2 (M_{\text{soft}}^2 + M_T^2)} \right) - 2 \frac{M_{\text{soft}}^2}{M_T^2} \log \left( \frac{M_{\text{soft}}^2 + M_T^2}{M_{\text{soft}}^2} \right) \right] \right\}$$

- A slice of the higgs and radial masses



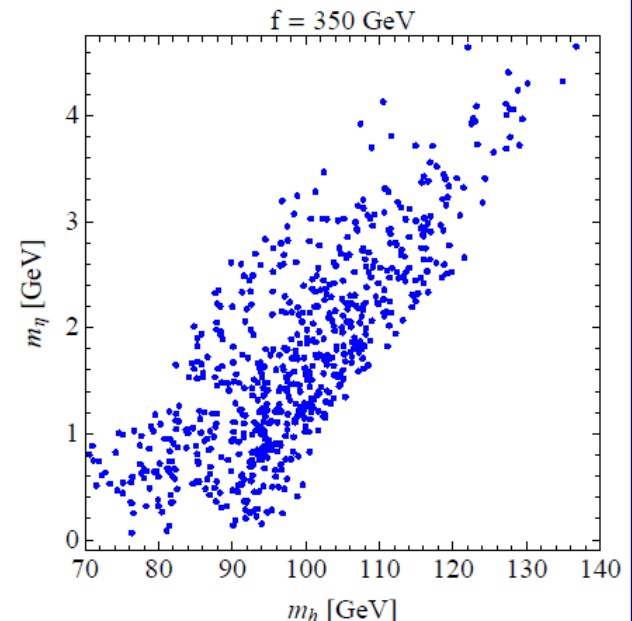
- From 1-loop Coleman Weinberg, including higgs-radial mixing

## $\eta$ mass

- For collective Yukawas,  $f/F \rightarrow 0$   $\eta$  exactly massless – can be removed by phase redefinitions
- To leading order in  $f/F$ :

$$m_\eta^2 \approx \frac{3v_{EW}^2 y_2^2}{8\pi^2} \frac{M_{\text{soft}}^2}{F^2} \left[ \log \left( \frac{y_{b1}^2 F^2}{2(M_T^2 + M_{\text{soft}}^2)} \right) - \frac{M_T^2}{M_{\text{soft}}^2} \log \left( \frac{M_T^2 + M_{\text{soft}}^2}{M_T^2} \right) + 1 \right]$$

- Generates small  $m_\eta$  in the few GeV range:



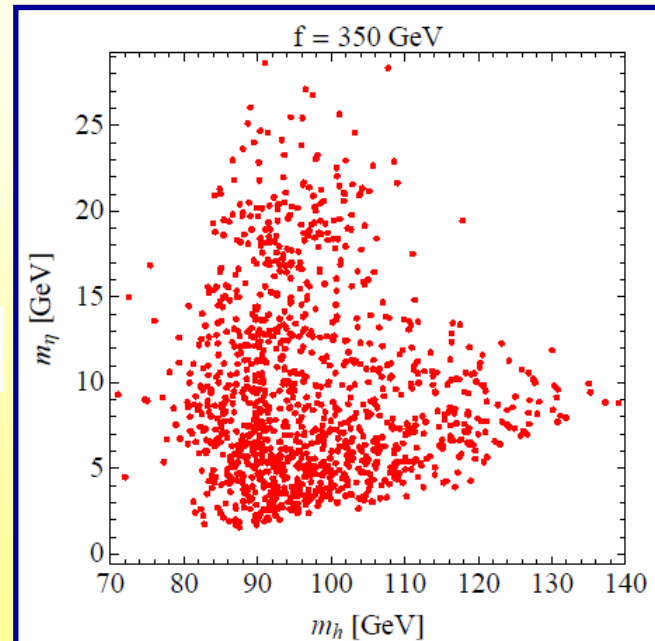
- To get bigger  $m_\eta$  can turn on small non-collective coupling

$$\tilde{y}_{b1} \mathcal{H}_d Q b_c^1 + \tilde{y}_{b2} \Phi_d Q b_c^2$$

$$m_\eta^2 = \cos \beta \frac{N_c}{4\pi} \frac{F}{f} (y_{b1} \tilde{y}_{b1} + y_{b2} \tilde{y}_{b2}) M_{soft}^2 \log \frac{\Lambda}{F}$$

- A scatter plot for the achievable masses for a particular point:

$f = 350, F = \sqrt{2} \cdot 10^4, \Lambda = 10^7$  GeV for both plots, and scanned the remaining parameters in the regions  $0.02 < y_1 < 0.3, 1 < y_2 < 3, 0.02 < y_{b1} < 0.12$  and  $300 < M_{soft} < 1500$  GeV.



# Parameter scans (f=350 GeV)

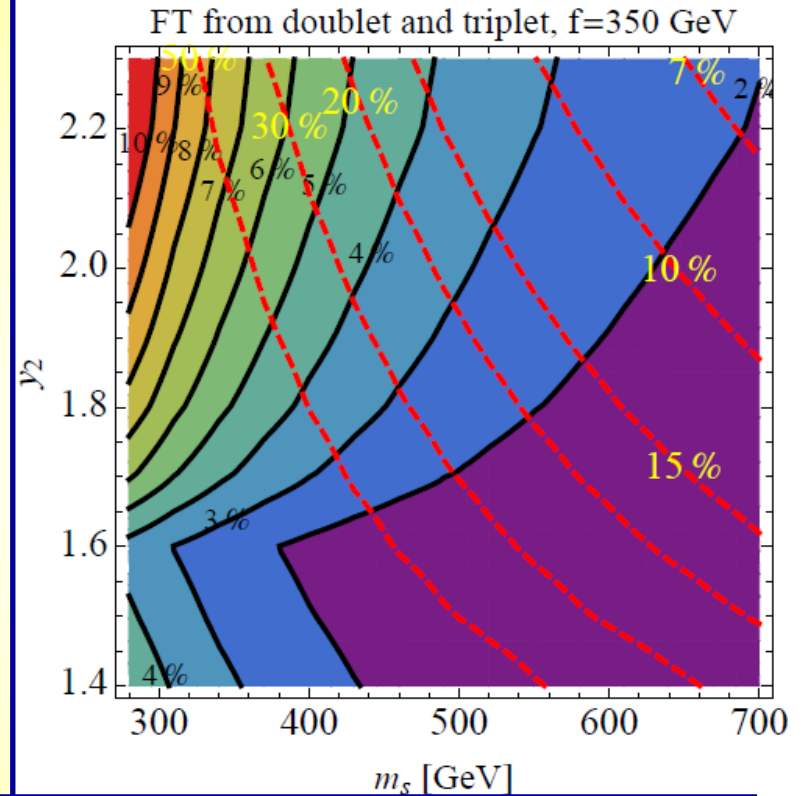
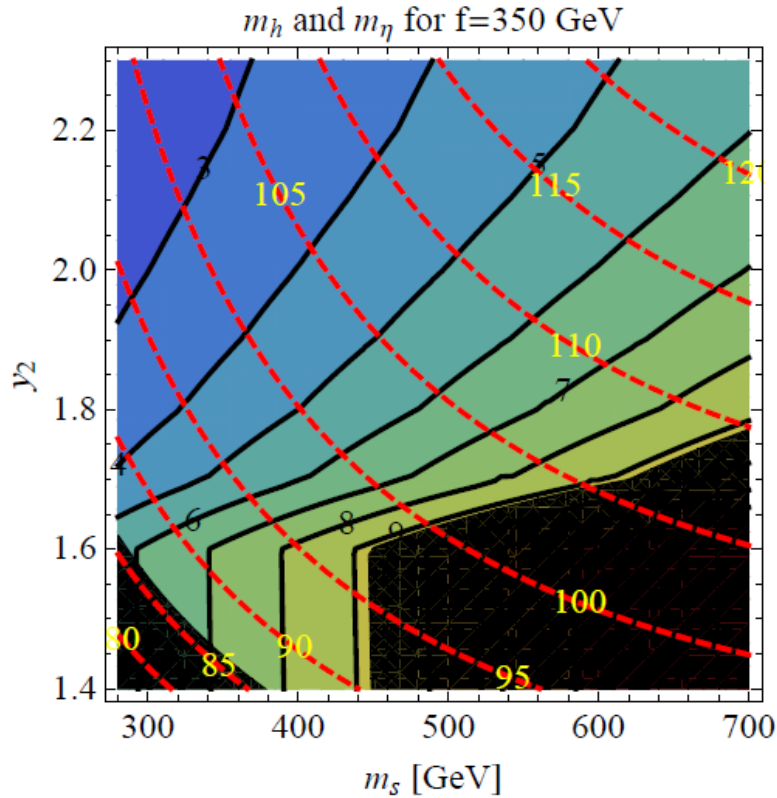
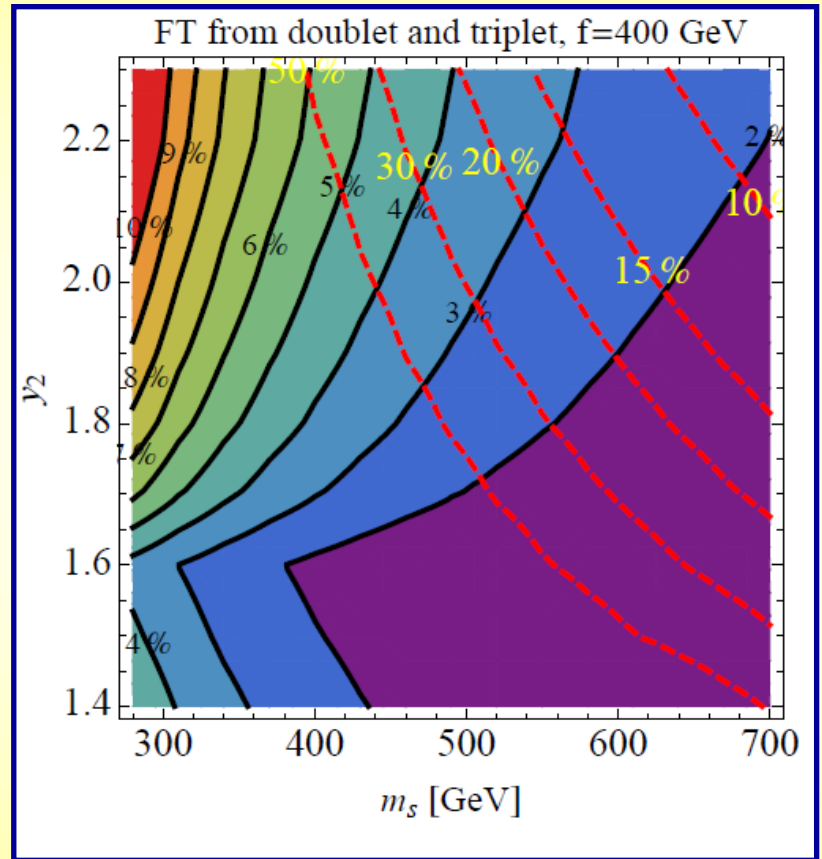
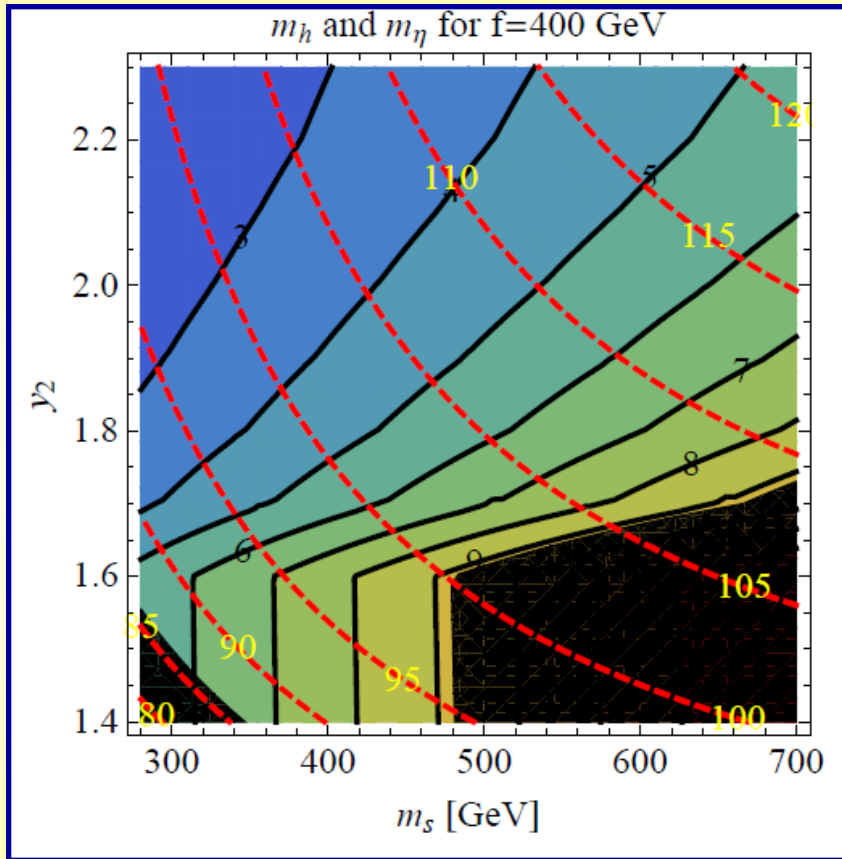


Figure 4: On the left the contours of the Higgs mass (dashed red line) and the  $\eta$  mass (solid black lines) as function of the universal soft breaking mass  $M_{soft}$  and the top Yukawa  $y_2$ . On the right, the necessary fine tunings  $FT_3$  (solid black) and  $FT_2$  (dashed red) in percent. These plots are based on the full numerical 1-loop Coleman-Weinberg potential, with  $f = 350$  GeV,  $y_1 = 0.29$ ,  $y_{b1} = 0.1$ ,  $y_{b2} = 0$ ,  $\tilde{y}_{b1} = 0.001$ ,  $\tan \beta = 10$ ,  $F = \sqrt{2} \cdot 10^4$  and  $\tilde{y}_{b2} = 0$ . The region in the lower left is excluded by the LEP  $\xi^2$  bound and in the lower right because  $m_\eta > 2m_b$ .

# Parameter scans (f=400 GeV)



- Perturbativity: SU(3) Landau pole at  $\Lambda \sim 10^8$  TeV
- For  $y_2=1.64$   $\Lambda_{\text{quartic}}=10^8$  TeV, while for  $y_2=1.83$   $\Lambda_{\text{quartic}}=10^4$  TeV



## $\eta$ decays

- If  $m_\eta > 2 m_b$  then  $\eta \rightarrow bb$  will dominate. But then  $h \rightarrow 4b$  which is strongly constrained by LEP ( $m_h > 110$  GeV)

- Will require  $m_\eta < 2 m_b$ . In this case decays to  $\tau$ ,  $c$ ,  $\gamma$  or gluon are relevant.

- Decay to  $\tau$ :  $h \rightarrow 2\eta \rightarrow 4\tau$  from coupling

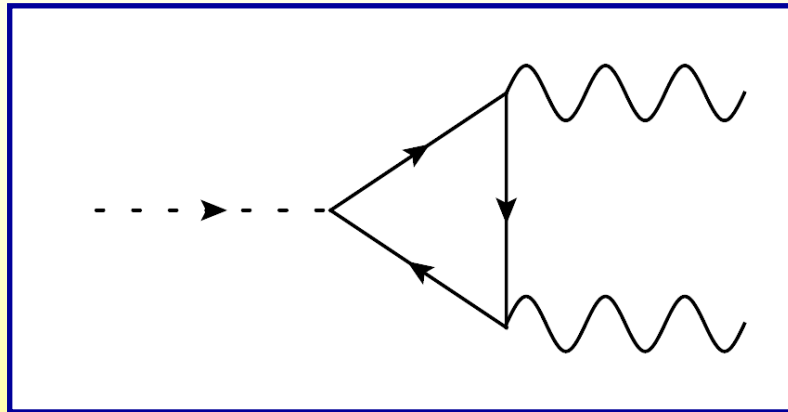
$$i\tilde{y}_\tau(\bar{\tau}\gamma_5\tau)\eta \quad \tilde{y}_\tau \simeq \frac{m_\tau^3 f}{\sqrt{2}M_\tau^2 v_{EW}^2}$$

- Strongly suppressed because  $\tau$  mixing  $\propto m_\tau^2/M_\tau^2$

- Width for decays to  $\tau$

$$\Gamma_{\eta \rightarrow \tau\tau} \approx \frac{1}{16\pi} \sqrt{1 - 4m_\tau^2/m_\eta^2} \frac{m_\eta m_\tau^6 f^2}{v_{EW}^4 M_\tau^4}$$

- Very small  $\sim 10^{-13}$  GeV, mm decay length...
- Dominant decay will be through loops to  $2g$ ,  $2\gamma$ :



- The loop induced decays:

$$\kappa^g \eta \epsilon^{\mu\nu\rho\sigma} G_{\mu\nu}^a G_{\rho\sigma}^a, \quad \kappa^g = \frac{g^2}{32\pi^2} \sum_{\psi} \frac{\tilde{y}_{\psi}}{m_{\psi}} c_2(\psi) \tau_{\psi} f(\tau_{\psi})$$

- $f(\tau)$  is the usual triangle function,  $\tau = 4 m_{\psi}^2/m_{\eta}^2$ :

$$f(\tau) = \begin{cases} \arcsin^2[\tau^{-1/2}] \\ -\frac{1}{4} \left( \log[(1 + \sqrt{1 - \tau})/(1 - \sqrt{1 - \tau})] - i\pi \right)^2 \end{cases}$$

- Leading term:  $\eta G \tilde{G} \sim \sum \tilde{y}_{\psi}/m_{\psi} \approx \mathcal{O}(1/F^2)$   
vanishes due to anomaly cancellation

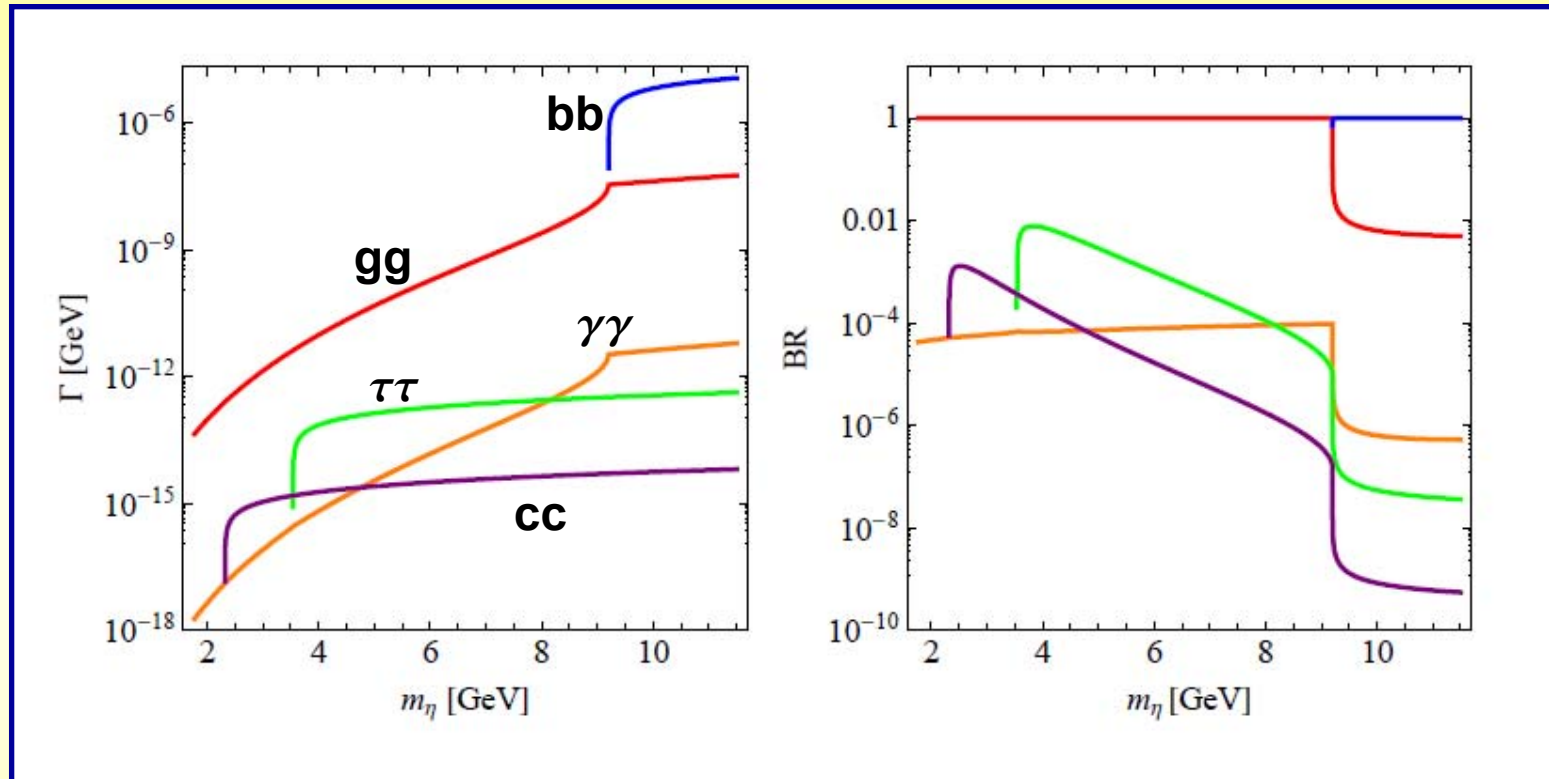
- Actual leading operator  $\square \eta G \tilde{G}$   
 $\sim \sum \tilde{y}_{\psi} m_{\eta}^2/m_{\psi}^3$  dominated by bottom

- The  $\eta \rightarrow gg$  decay width:

$$\kappa^g \simeq \frac{1}{12\sqrt{2}} \frac{g_s^2(m_\eta)}{64\pi^2} \frac{m_\eta^2}{m_b^2} \frac{m_t^2 f}{\mu_V^2 v_{EW}^2}$$

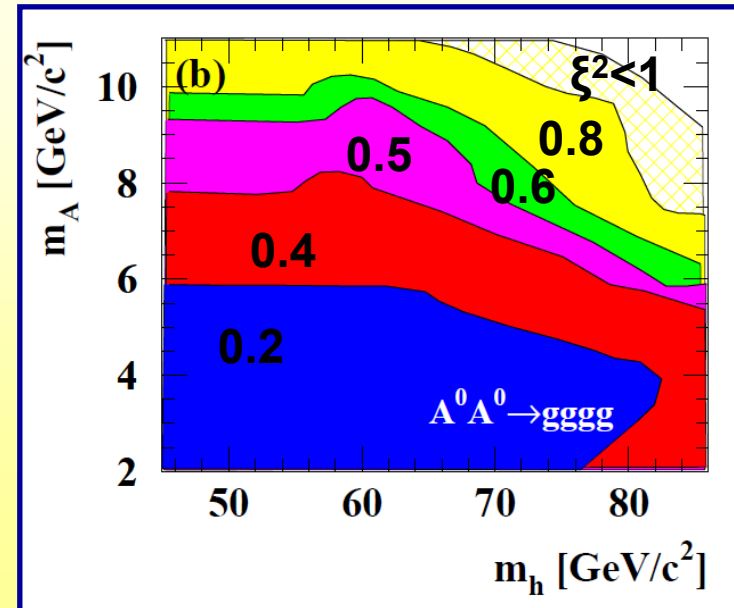
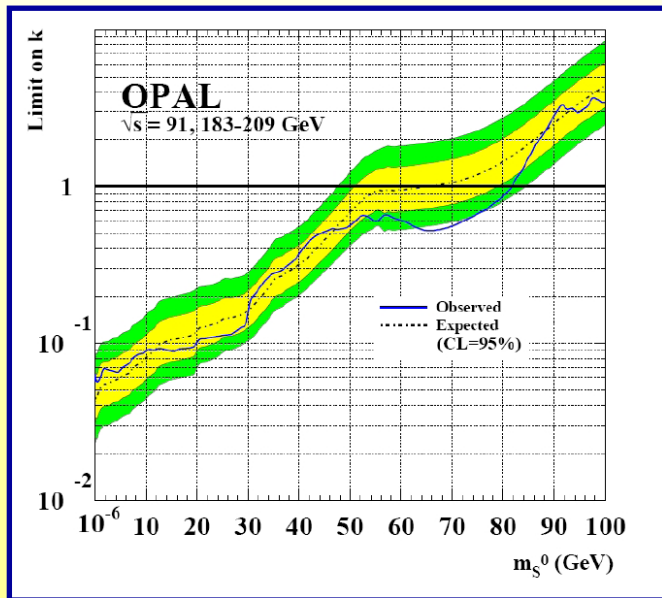
- Will be leading mode
- $h \rightarrow 2\eta \rightarrow 4g$  will be main decay chain
- Hard to find at hadron colliders – higgs buried under QCD background

# The $\eta$ decays



$$f = 350 \text{ GeV}, \mu_V = 500 \text{ GeV}, M_c = 400 \text{ GeV}, M_\tau = 200 \text{ GeV}$$

- $h \rightarrow 4g$  almost 100 %
- $h \rightarrow \gamma\gamma gg$  of order  $10^{-4}$
- $h \rightarrow \tau\tau gg$  of order  $10^{-3} - 10^{-5}$
- $h \rightarrow 4\mu$  and  $h \rightarrow \tau\tau\mu\mu$  very suppressed...
- LEP bound: model indep.  $m_h > 78$  GeV
- OPAL  $h \rightarrow 2\eta \rightarrow 4j$  analysis (assuming  $m_h < 86$  GeV):

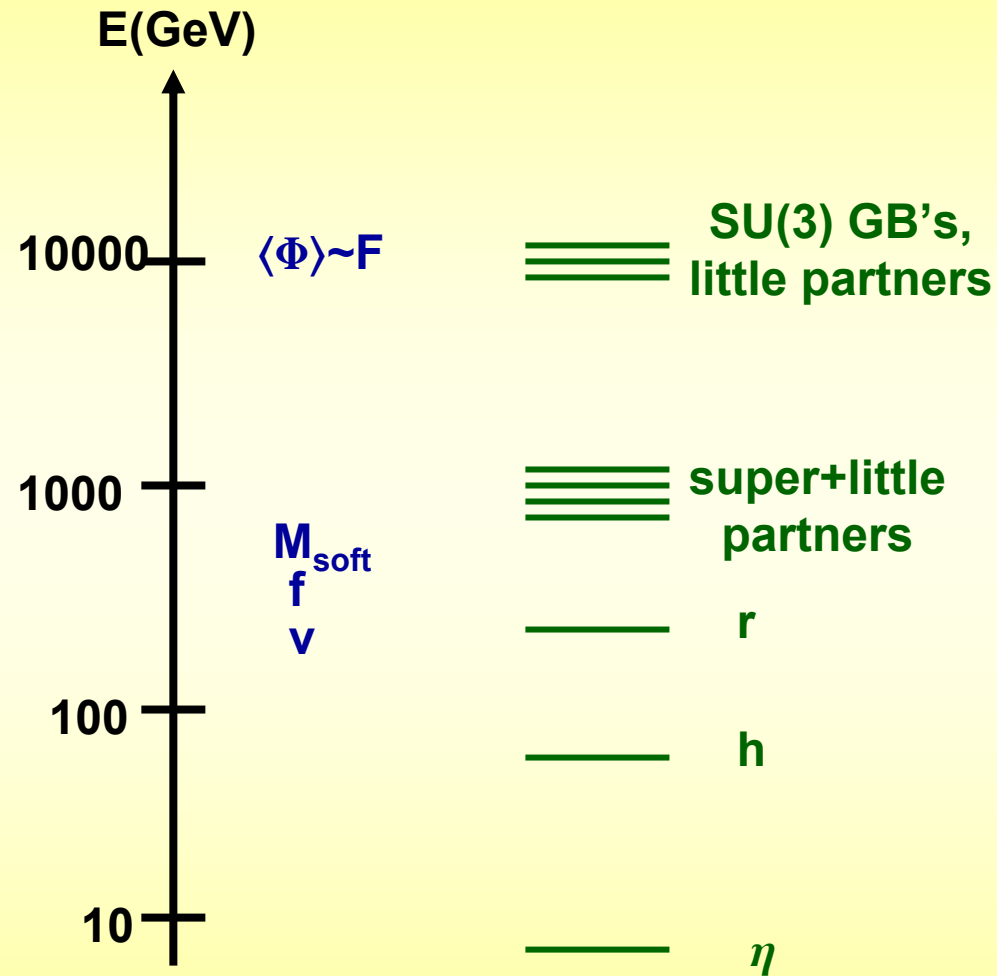


- LEP exclusion: for  $78 \text{ GeV} < m_h < 86 \text{ GeV}$   
we need  $6 \text{ GeV} < m_\eta < 9.2 \text{ GeV}$

- Reason: opening angle between jets  $\sim 4m_\eta/m_h$ , for  
very small  $m_\eta$  not 4 jets but 2 jets, restrictive search...

- Would need to know what genuine 4 jet analysis  
gives at LEP...

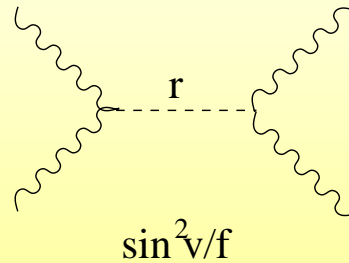
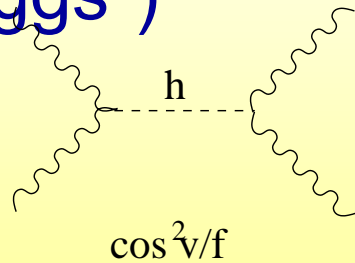
# The particle spectrum





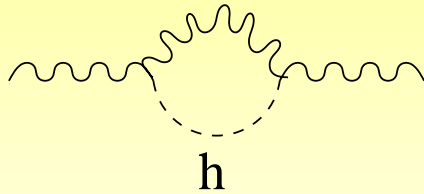
## Radial mode, unitarity, EWP

- Radial mode:  $m_r \sim 300\text{-}400\text{ GeV}$
- Couples just like the higgs, with  $\sin v/f$  suppression
- Should be observable in  $Z \rightarrow Z+r \rightarrow Z+ZZ \rightarrow Z+4l$  mode, or just gluon fusion  $gg \rightarrow r \rightarrow ZZ \rightarrow 4l$
- But will have wrong coupling for unitarity, EWP: wrong higgs (“fake higgs”)

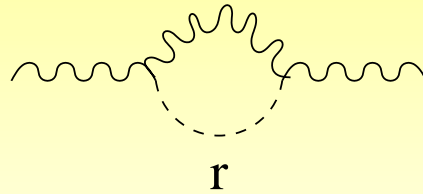


- Unitarity:
- As long as  $m_h, m_r < \text{TeV}$  unitarity OK

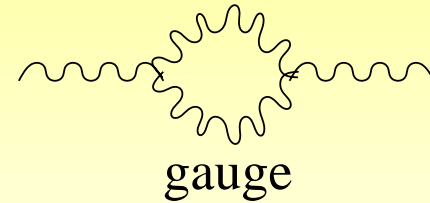
- Electroweak precision (S, T):



$$\sim \cos^2 v/f \log m_h/\Lambda$$



$$\sim \sin^2 v/f \log m_r/\Lambda$$



$$\sim \log \Lambda/m_W$$

- $m_h^{\text{eff}} = m_h (m_r/m_h)^{\sin^2 v/f} \sim 120 \text{ GeV}$

- Still within allowed region, but NOT at  $\chi^2$  minimum...

## The Charming Higgs

- Simple variation of model by changing fermion matter content
- To get real little Higgs, need top partner in triplet
- Need to exchange up- and down-type quarks
- Can get another anomaly free matter content that does this!

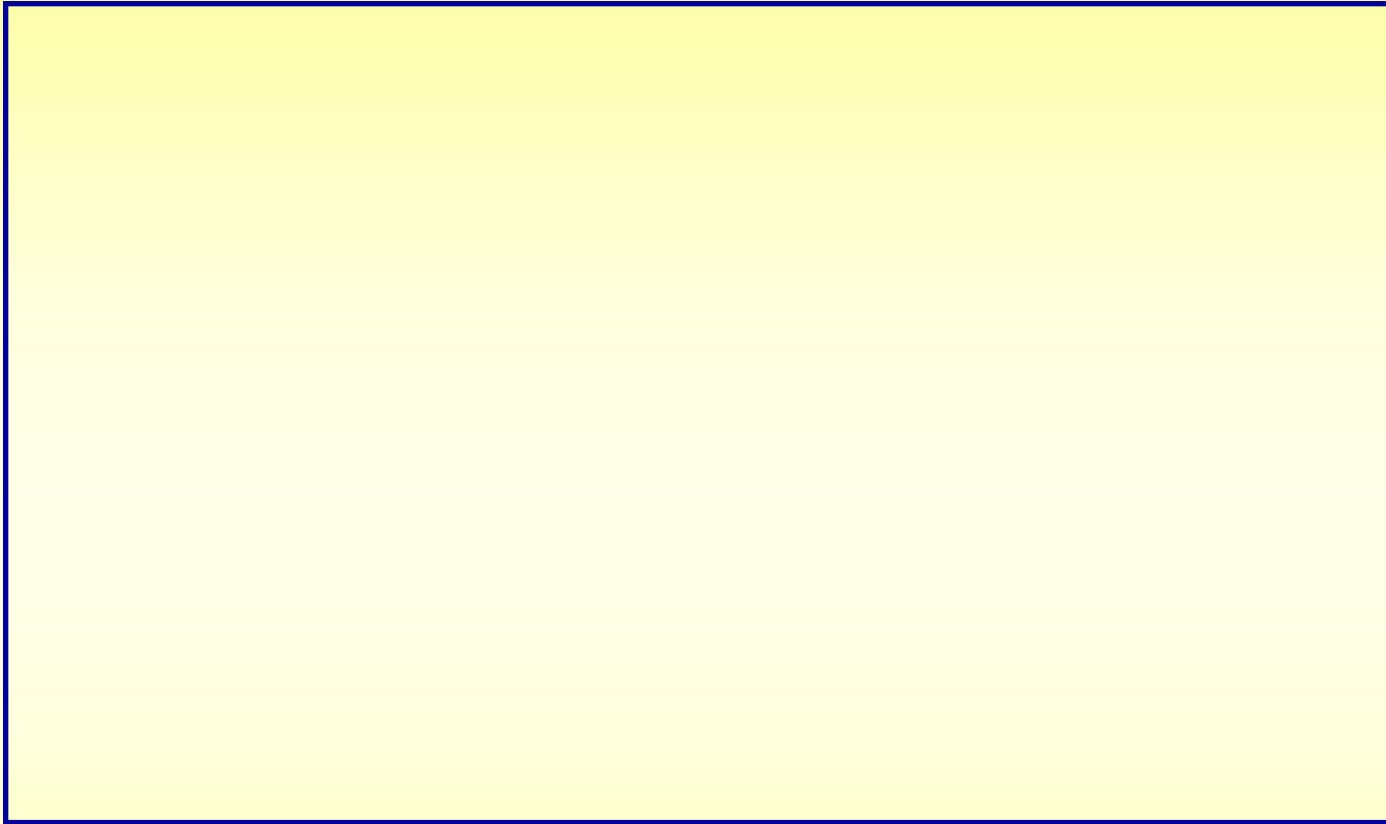
# How to get the anomaly free matter?

- Original model:  $SU(3) \times SU(3) \times U(1) \subset SU(6)$
- $SU(6)$  matter:  $\square + 2 \bar{\square}$  , just decompose to subgroup
- Another possibility: “flipped  $SU(N)$ ”

	$SU(N)$	$U(1)_X$
1	$\square$	$N - 4$
$(N - 4)$	$\bar{\square}$	$-(N - 2)$
$\frac{(N-4)(N-3)}{2}$	1	$N$

- Decomposing this (for  $N=6$ ) gives new fermion matter

## The flipped matter content



- Quark sector now like little Higgs (can add  $\mu_V VV_c$  mass, now  $\mu_V$  does not have to be  $\sim \text{TeV}$ ...

# Gauge and global symmetry (almost) same

	$SU(3)_C$	$SU(3)_W$	$U(1)_X$
$\mathcal{H}_u, \Phi_u$	1	$\bar{3}$	1/3
$\mathcal{H}_d, \Phi_d$	1	3	-1/3

•Goldstones:

$$\mathcal{H}_u^T = f s_b \begin{pmatrix} \sin(\tilde{h}/\sqrt{2}f) \\ 0 \\ e^{i\tilde{\eta}/\sqrt{2}f} \cos(\tilde{h}/\sqrt{2}f) \end{pmatrix},$$

$$\mathcal{H}_d = f c_b \begin{pmatrix} \sin(\tilde{h}/\sqrt{2}f) \\ 0 \\ e^{-i\tilde{\eta}/\sqrt{2}f} \cos(\tilde{h}/\sqrt{2}f) \end{pmatrix}.$$

•Hypercharge  $Y = -T_8/\sqrt{3} + X$

# Yukawas

- Collective for quarks:

$$y_1 t_c^1 \Phi_u Q + y_2 t_c^2 \mathcal{H}_u Q + \mu_V V_c V + y_{b1} V_c Q \Phi_d + y_{b2} b_c^1 V \mathcal{H}_d$$

- $\mu_V$  large limit easy:

$$y_1 t_c^1 \Phi_u Q + y_2 t_c^2 \mathcal{H}_u Q + \frac{y_{b1} y_{b2}}{\mu_V} b_c^1 Q \Phi_d \mathcal{H}_d$$

- Top and charm mass:

$$m_t \approx \frac{s_b y_1 y_2 F}{\sqrt{(y_1 F)^2 + 2(s_b y_2 f)^2}} v_{EW}$$

$$m_c = \frac{s_b y_{c1} y_{c2} F}{\sqrt{(y_{c1} F)^2 + 2(s_b y_{c2} f)^2}} v_{EW}$$

- Bottom mass:

$$m_b \approx y_{b1} y_{b2} c_b v_{EW} F / \sqrt{2} \mu_V$$

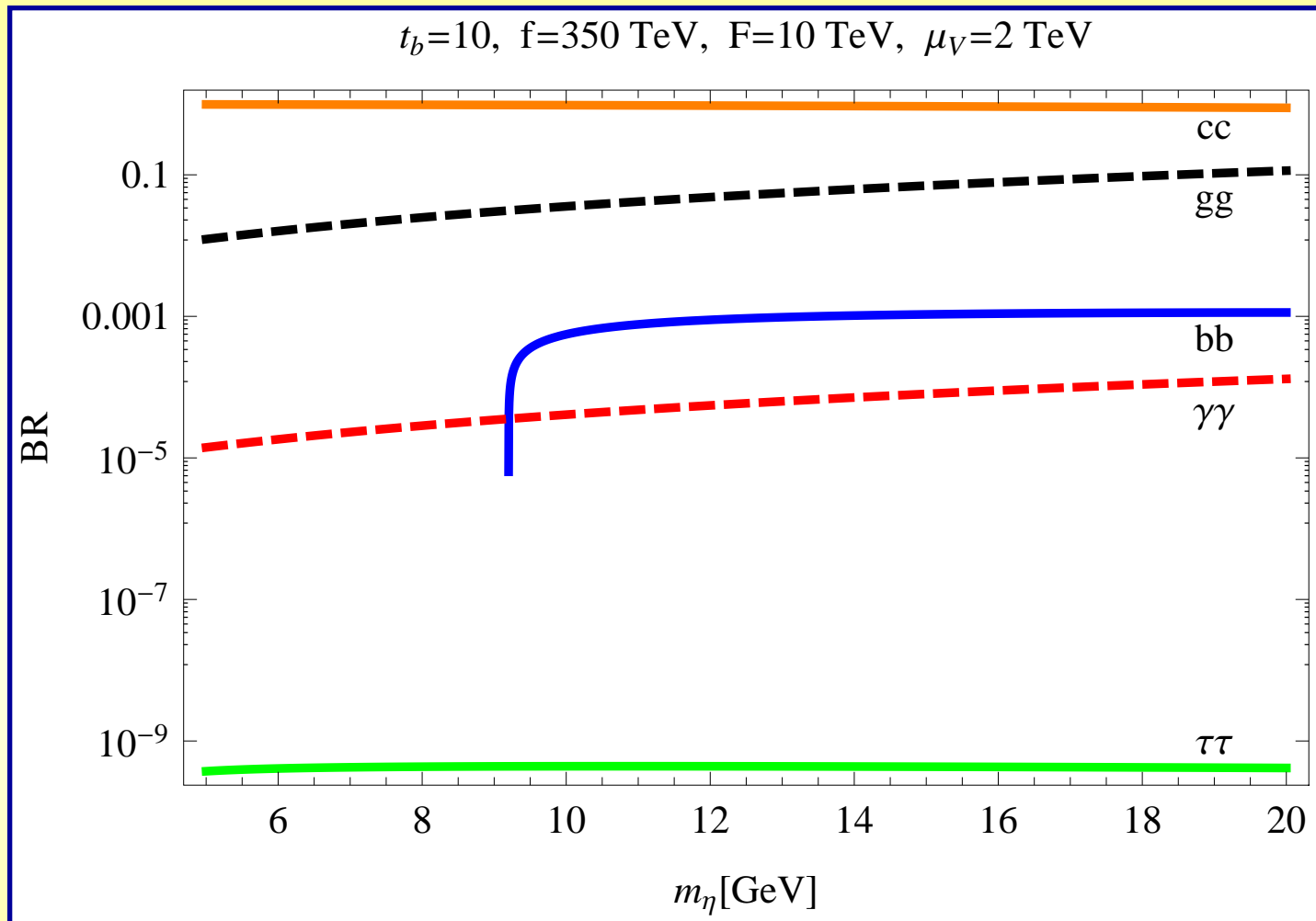
## $\eta$ decays

- Important difference: coupling to down-type quarks suppressed by  $m_b^2/\mu_V^2$  – very suppressed even if kinematically allowed
- $\tau$  coupling still suppressed
- will mostly decay to charm or gluon

$$\tilde{y}_c \approx \frac{m_c}{\sqrt{2}f} \quad \tilde{y}_\tau \sim \frac{m_\tau}{\sqrt{2}f} \frac{m_\tau^2}{M_\tau^2}$$

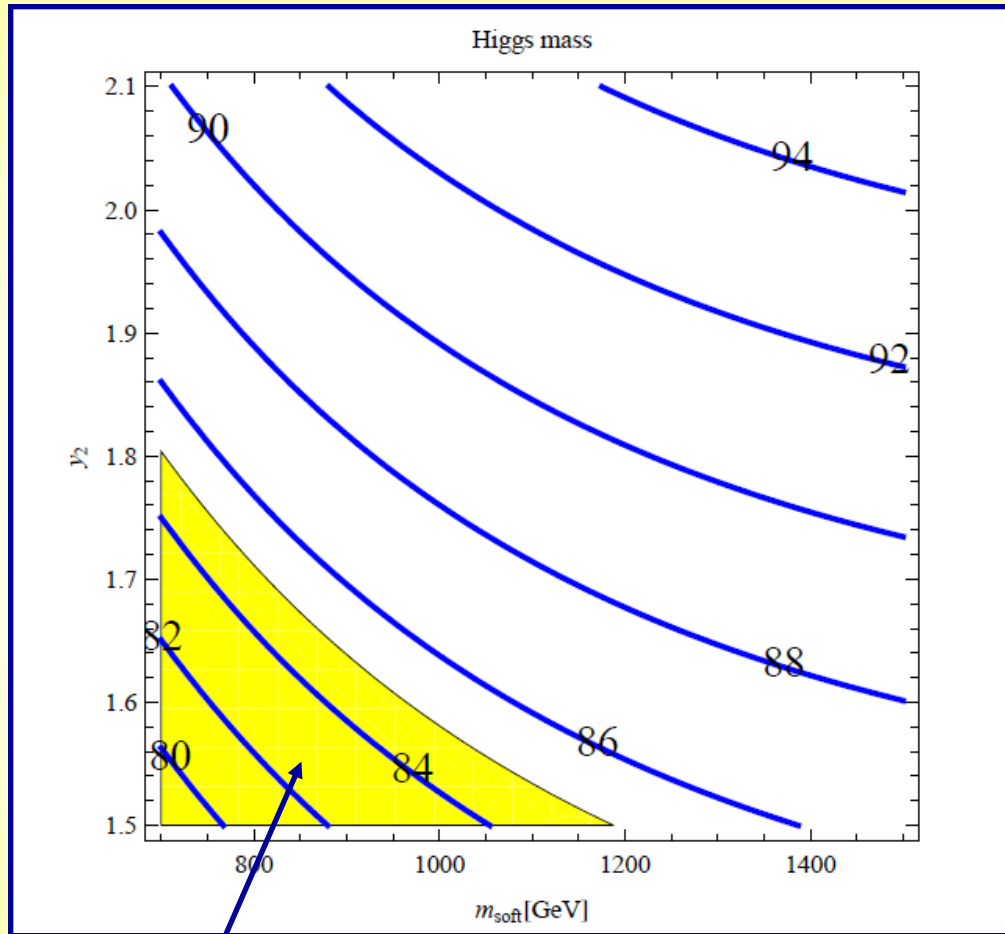


# $\eta$ decays



- Note: size of loop induced  $\eta bb$  coupling estimated

# Achievable Higgs masses



Region excluded by LEP  $h \rightarrow b\bar{b}$

## Summary

- An extension of the MSSM, where:
  - $h \rightarrow 2\eta \rightarrow 4j$  cascade is natural
  - higgs below LEP bound
  - no little hierarchy
  - $h$  and  $\eta$  both Goldstones (little Higgs)
  - super and little partners available at LHC
  - Higgs buried (?) in QCD at LHC
  - Fake higgs readily available
  - All scales radiatively generated
- A really cool model of EWSB!