

Using $\int_0^\infty d\alpha \alpha^{\gamma-1} e^{-\alpha p^2} = \Gamma(\gamma) (p^2)^{-\gamma}$ (twice), one can easily show that

$$\int d^D p |p^2|^{-\gamma} e^{i(p \cdot x)}$$

$$= \frac{(4\pi)^{D/2} \Gamma(\frac{D}{2} - \gamma)}{4^\gamma \Gamma(\gamma)} |x^2|^{\gamma - \frac{D}{2}}$$

First use this with $\gamma = 1$ to get the ^{massless} propagator in x -space ~~with~~

$$\Delta \sim |x^2|^{-\frac{D}{2}}$$

Now in




the parallel x -space propagators multiply to give

$$\sim |x^2|^{3 - \frac{3D}{2}}$$

Then use the formula with $\gamma = \cancel{\frac{3D}{2}} \frac{3D}{2} - 3$ to get in p -space

$$\sim \Gamma(3-D) |p^2|^{D-3},$$

multiplied by easily calculable trivial factors, such as $(2\pi)^{-D}$.

This trick can also be used to calculate  $\sim \Gamma(2 - \frac{D}{2}) |p^2|^{\frac{D}{2} - 2}$ and reduce



to



General rule: series multiply in p -space, parallel in x -space.

[There is also a trick for turning ^{some} loops into trees by writing rules for the dual diagram, i.e. vertices \Rightarrow loops, lines rotated 90° .]