Physics 619

HOMEWORK # 5

DUE DECEMBER 8, 2016

Problem I (10 pt) : Peskin, Schroeder: Problem 16.1

Problem II (10 pt)

Let T^i be operators which satisfy

$$[T^i, T^j] = \mathrm{i} f^{ijk} T^k ,$$

where f^{ijk} are structure constants of a Lie algebra. Let c_i and c_j^{\dagger} be operators which obey

$$\{c_i, c_j^{\dagger}\} = \delta_{ij} , \quad \{c_i, c_j\} = \{c_i^{\dagger}, c_j^{\dagger}\} = 0 , \quad [c_i, T^j] = [c_i^{\dagger}, T_j] = 0 .$$

 \mathbf{If}

$$Q = T^i c_i - \frac{\mathrm{i}}{2} f^{ijk} c_i c_j c_k^{\dagger}$$

show that

 $Q^2 = 0 .$

Problem III (10 pt) : Peskin, Schroeder: Problem 16.2