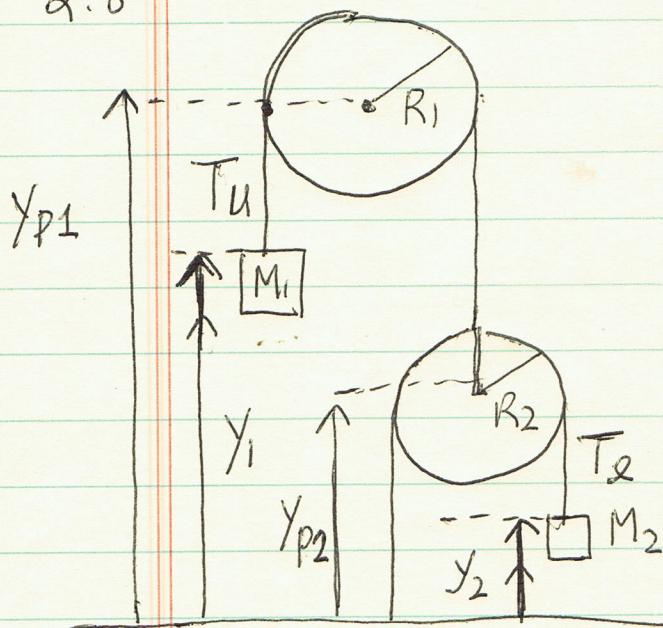


2.8



Constraints

With this choice of coordinates, let's write the expressions for the two string lengths

upper string L , lower string ℓ

$$y_{P1} - y_1 + y_{P1} - y_{P2} + \pi R = L$$

and

$$y_{P2} + y_{P2} - y_2 + \pi R = \ell$$

for the acceleration, differentiate:

$$-a_1 - a_{P2} = 0$$

$$a_{P2} + a_{P2} - a_2 = 0 = 2a_{P2} - a_2$$

eliminate a_{P2} to get constraint connecting a_1 and a_2

$$-a_1 - a_2/2 = 0$$

$$\Rightarrow a_2 = -2a_1$$

Force diagrams

$$\begin{array}{c} \uparrow T_u \\ \bullet \\ \begin{array}{l} M_1 : \\ T_u - M_1 g = M_1 a_1 \\ \downarrow M_1 g \end{array} \end{array}$$

$$\begin{array}{c} \uparrow T_l \\ \bullet \\ \begin{array}{l} M_2 : \\ T_l - M_2 g = M_2 a_2 \\ \downarrow M_2 g \end{array} \end{array}$$

Lower pulley

$$\begin{array}{c} \uparrow T_u \\ \uparrow T_u \\ T_u = 2T_l \\ \downarrow 2T_l \end{array}$$

$$2T - M_1 g = M_1 a_1$$

$$T - M_2 g = -2M_2 a_1$$

$$\frac{(-M_1 + 2M_2)g}{(-M_1 + 2M_2)g} = (M_1 + 4M_2)a_1$$

eliminate T

$$a_1 = \frac{(-M_1 + 2M_2)g}{M_1 + 4M_2}$$